## MisterNumbers Pattern Play Math Playsheets



### **Exciting time for Pattern Play Math expanding in two directions**

The idea of playing with numbers goes against the serious nature of most math teaching, but it is actually much more effective than grind memorization. Kids get excited, have fun, generate a positive attitude about math, develop curiosity and learn to see and look for underlying patterns everywhere: the basis for learning for a lifetime.

### **SQUARES**

This is an exciting time for Pattern Play Math expanding in two directions. The revolutionary video on Squaring any Number Mentally just came out and is below. There is much more on using the system for finding Square Roots, creating the 20x20 Times Table, and multiplying numbers mentally.

Squares go right through the biggest numbers on the times tables and make it easy to multiply the larger numbers together, which is where students tend to struggle most. And it is all done with addition, not multiplication.

### ADDITION ON THE NUMBER WHEEL

But I am also excited about the other direction: New Patterns for Basic Addition on Number Wheels. I found many high school students struggle with basic addition and found some fascinating and powerful images using number wheels that could help pre-school through 2<sup>nd</sup> graders have fun memorizing addition/subtraction facts. This is great because when they come to multiplication/division, they are already comfortable with the simple number wheels.

Addition direction came AFTER squares. Creating Squares is a ADDITION process, and creating the multiplication tables or individual math facts both also involve addition. As I worked with students, even Calculus students, I found that many of them struggled with basic addition. Relying on cell phones as calculators may be one reason basic math is suffering.

The two tools using Number Wheels for anchoring addition are ways to add 5 to any number, and Number Wheels that show the cool patterns of numbers that add up (in the Ones) to 10-9-8-7-6-5-4-3-2-1. The Ten-Adds are Horizontal parallel lines and Five-Adds are Vertical parallel lines. ALL ADDITION is within 2 of these lines. If a student can "see" the numbers on the wheel and their relative position, they can "see" the Ones part of the answer.

### MisterNumbers Pattern Play Math Playsheets

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Inservice



### Tom Biesanz M.S. a.k.a. MisterNumbers Taking the "numb" out of numbers <a href="https://www.PatternPlayMath.com">www.PatternPlayMath.com</a>

### Inservice for Schools and School Districts

PRESENTATION: Learning on the Fun, Visual, and Effective Pattern Play Math Path

Tom Biesanz, MisterNumbers on Youtube (with 2 million 5-star views) and author of Right Brain Math and more. He has over 14,000 subscribers.

Do your students struggle with math or have a negative attitude about it, or themselves? Do your kids and teachers suffer in the learning process?

Experience Tom Biesanz, MisterNumbers, and discover cool tools that will amaze your teachers (and you) while they learn powerful ways to present math. Your teachers will encourage students to learn how to learn by playing with patterns.

Here is what your teachers will learn:

- ✓ This Pattern Play Math approach is visual, playful, right-brained, and students get physically involved and have fun
- ✓ Uses simple techniques that makes numbers twice as easy and makes kids comfortable.
- ✓ Uses fascinating patterns like Number Wheels, the EZ Times Table, and Tic-Tac-Toe Squares with comes with worksheets that students enjoy.
- ✓ Ways for students to quickly and easily master the Eights times table, literally almost as easy as learning the Twos.
- ✓ How teachers can lead students to follow the patterns they see, which will reveal their learning style while improving attitude about school and themselves.

Math doesn't have to feel like a 4-letter word. Confidence and competence are so important to our students' school experience, and has lasting effects throughout their lives.

www.PatternPlayMath.com/ Tom@PatternPlayMath.com call toll-free 805-967-0469



### Introducing Tom Biesanz

Creator of Pattern Play Math, Tom Biesanz is changing math into a more fun and easy activity, with a WOW factor. Curriculum Review magazine says it "does make math fun! ... a revolutionary visual and auditory introduction to math – a welcome resource in a time when U.S.math scores are falling behind other countries."

He has done Inservice work with individual schools and school districts.

As MisterNumbers on Youtube, he has freely shared his lessons with 2 million Youtube viewers. Many of his videos are animated and are rated 5 stars. He generated that many views because dozens of reputable websites like Encyclopedia.com, HomeSchoolNews.com, WorldNews.com, WatchKnow.com share his videos as valuable teaching tools.

Tom is the author of Right Brain Math and Amazing Calendar Math Magic. He created the MisterNumbers Companion DVD for the Right Brain Math book and also 5 fascinating iphone math apps that are free.

Many math teachers have given rave reviews to his presentations at several California Math Council conventions.

Parents and teachers, as well as students, enjoy Tom's approach. He is an inspiring presenter with 7 years of Toastmaster experience and was selected as "Toastmaster of the Year" in 2011 by his club.

Education is a deep love for Tom. His mother was a teacher and five of his brothers and sisters also have been teachers. His personal connection to fun learning also includes his five grandkids

Parent Tiffany Hart says: "LOVE IT, LOVE IT, LOVE IT, LOVE IT......I have a third grader and this is working like a charm. I, myself have learned the times tables better. I'm going to send this information to my daughter's school. Thank you so very much."

Parent Jenny Adams says, "Thank you! No tears doing homework tonight! I have the hardest time trying to explain math to my child because she thinks so much differently than I do, and teachers just send home drill-and-practice worksheets that are pure torture for us. She totally got these patterns and had FUN doing it!"

Tom is the expert who can assist you in helping your kids love and understand math. They will appreciate what you are sharing with them

# Square Deal on Numbers

# Value of Being Able to Square Numbers easily in your Head

squares 1-20 in a day, to create most of the 20x20 Times Table facts in their head. In the 20x20 chart you can see that the squares give answers to the AND using the patterns learned in the 20x20 Chart (see the first chart and following instructions), you can know that 27 x 25 is accurately 26 squarec Why learn to square numbers even if it is easy? Another benefit to squaring number include estimating multiplying two numbers together. Say you -1 or 675. The pattern is not limited by the chart. Using the patterns learned in the 20x20 chart allows a third grade student who easily learned the want to estimate  $27 \times 25$ . If you mentally square the number in the middle  $(26 \times 26 = 676)$  You know that will be very close. toughest multiplication facts, and all multiplication facts near them.

# Table showing how the Tens jump when you are finding squares of a number

This allows you to jump in anywhere to square any number. An example would be 32, nearest 0 or 5 is 30.30/5 = 6. See chart below. Squares Pattern in Tens goes up by the nearest number ending in 0 or 5, divided by 5

est 0 or 5	5	10	15	20	25	30	35	40	45	20	55	09	9	70	75	80	85	06	95	100
nwob ro di	1	2	ж	4	5	9	7	8	6	10	11	12	13	14	15	16	17	18	19	20

Remember numbers ending in 3 or 7 can go from 0 or 5, and you get the right answer either way. Most kids prefer to start at a zero. So the tens would start at 90 (30x30 = 900 and the tens would be 90 and the Ones would be 0). Add two sixes to get to 90+12=102

### Square a number ending in 0

Let us square 50 as an example. 50x50=?

We square the tens digits first. Tens digit is 5 so 5x5 = 25. Easy.

Second we add the two zeros at the end. 25 00 or 2500 or 2,500

 $1600 \ 40x40 = 1600 \ \text{or} \ 1,600.$ 30x30 = 900. 900. 3x3=9 and add two zeros. 4x4=16 and add two zeros. So 30 squared would be 30x30=?40 squared would be 40x40=?

# Square a number ending in 5

Take the Tens number in front of the five, call it T. Multiply T x (T+1) and write 25 after it. That is your answer. Take T (here is 9) x (T+1) 10. 9x10=90 and write 25 after it. 9025. 95x95=9025Take T (here is 3) x (T+1) 4. 3x4=12 and write 25 after it. 1225. 35x35=1225Take T (here is 2) x (T+1) 3. 2x3=6 and write 25 after it. 625. 25x25=625To square a number like 15, 25, 35, 45, 55, 65, 75, 85, 95, 105, etc., use a cool trick. Example: 95 squared. Example: 35 squared. Example: 25 squared.

### Writing out the Squares of 1 to 50 EASILY

Watch how to make the Squares on MisterNumbers video at: https://goo.gl/wUIDs0 This is a fun and effective way to create the squares. You create the ONES (right) and TENS (left) with different patterns. Do this on a 1-50 or the 20x20 Times Table sheet (yellow squares). No multiplying and no carrying, yet this easy pattern with adding numbers up to 10 is fun, fascinating, and effective.

### **ONES:**

#	TENS	ONES	Directions
1		1	1-2-3-4 squared are 1-4-9-16, and may already done for you.
2		4	Notice the ONES pattern of 1-4-9-6 on the right, because it is like magic, and will repeat after each zero.
3		9	Just remember 1, 2, 3, 4 squared is 1-4-9-6 in the ONES.
4	1	6	Any number like 10 squared will end in zero, so go ahead and put a 0 in
5	2	5	the ONES column after 10-20-30-40-50, and then repeat the 1-
6	3	6	4-9-6
7	4	9	below each 0 on the right.  Now for more magic: Start at 50 and go up the ONES with 1-
8	6	4	4-9-6. You can see that it is true from 1-10 on the left.
9	8	1	The only ONES that are not filled in are squaring a number ending in 5, and 5x5 is 25 so the ONES will always be 5. Fill
10	10	0	in these 5s and you have completed the ONES column. You are half-way done.

### **TENS:**

The TENS are a really cool pattern. Notice that each 9 in the ONES has

a DARK LINE under it. If not, put a line under each 9 in the Ones. Squaring numbers ending in 3 and 7 create 9s and the lines are where the pattern changes for the Tens on the left.

Complete the squares down to 10x10=100. Look for patterns in the TENS between the lines.

The pattern is 1-2-3-4 and then (starting with the 4) 4-6-8-10. You are

not at the dark line yet, so what do you think will complete the pattern?

Yup. The first pattern was going up by 1: 1-2-3-4. The second pattern goes up by 2: 4-6-8-10-12-14-16.

Now you are at another dark line and the pattern changes. What do you think the new pattern will be?

If you guessed the new pattern will go up by 3, you are right! (starting with 16): 16-19-22-25-28.

And yes the TENS pattern goes up by 1 after each dark line. By 1-2-3-4-5-6-7-8-9-10.

Continue down creating the TENS, so at 50, the TENS are going up by 10.

The last four TENS are 220-230-240-250. It is that simple.

I HOPE YOU HAVE COMPLETED THE SQUARES FROM 1-50 EASILY.

You may notice that 50 is the tenth multiple of 5 (50/5=10).

And each number on the left ending with 5 or 0 divided by 5 IS the number that the TENS are going up. This is an easy way to square any single number from 1-50 (or higher) by starting from the closest 5.

But that is another page.

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#	TENS	ONES	Directions for creating Squares of numbers 1-50				
1		1	Watch how to make the Squares on MisterNumbers video at: https://goo.gl/wUIDs0				
2		4	This is a fun and effective way to create the squares.				
3		9	You create the ONES (right) and TENS (left) with different patterns.				
4	1	6	· - · · · · · · · · · · · · · · · · · ·				
5			No multiplying and no carrying, yet this easy pattern with adding				
6			numbers up to 10 is fun, fascinating, and effective.				
7			ONES:				
8			1-2-3-4 are already done for you. Notice the ONES pattern of 1-4-9-6 on				
9			the right, because it is like magic, and will repeat after each zero.				
10			Just remember 1, 2, 3, 4 squared is 1-4-9-6.				
11			Any number like 10 equared will and in zero, as go about and put a 0 in				
12 13			Any number like 10 squared will end in zero, so go ahead and put a 0 in the ONES column after 10-20-30-40-50, and then repeat the 1-4-9-6				
14			below each 0 on the right.				
15							
16			Now for more magic: Start at 50 and go up the ONES with 1-4-9-6. You				
17			will later see that it is true.				
18			The only ONES that are not filled in are squaring a number ending in 5,				
19			and 5x5 is 25 so the ONES will always be 5. Fill in these 5s and you				
20			have completed the ONES column. You are half-way done.				
21			TENO				
22			TENS: The TENS are a really cool pattern. Notice that each 9 in the ONES has				
23			a DARK LINE under it. Squaring numbers ending in 3 and 7 create 9s				
24			and the dark lines are where the pattern changes for the Tens on the left.				
25							
26			Complete the squares down to 10x10=100. Look for patterns in the				
27			TENS between the lines.				
28			The pattern is 1-2-3-4 and then (starting with the 4) 4-6-8-10. You are				
29			not at the dark line yet, so what do you think will complete the pattern?				
30			Yup. The first pattern was going up by 1: 1-2-3-4. The second pattern				
31 32			goes up by 2: 4-6-8-10-12-14-16.				
33							
34			Now you are at another dark line and the pattern changes. What do you				
35			think the new pattern will be?  If you guessed the new pattern will go up by 3, you are right! (starting				
36			with 16): 16-19-22-25-28.				
37							
38			And yes the TENS pattern goes up 1 after each dark line.				
39			Continue down creating the TENS, so at 50, the TENS are going up by				
40			10.				
41			The last four TENS are 220-230-240-250. It is that simple.				
42			I HOPE YOU HAVE COMPLETED THE SQUARES FROM 1-50 EASILY.				
43			Volumey notice that E0 is the tenth multiple of 5 (50/5 40)				
44			You may notice that 50 is the tenth multiple of 5 (50/5=10).  And each number on the left ending with 5 or 0 divided by 5 IS the				
45			number that the TENS are going up. This is an easy way to square any				
46	<u> </u>		single number from 1-50 (or higher) by starting from the closest 5.				
47			But that is another page.				
48							
49			O Mistrally 1 D 11 Di 11 II				
50	<u> </u>	<u> </u>	© MisterNumbers Pattern Play Math 2015				

#	TENS	ONES	#	TENS	ONES		#	TENS	ONES
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2		4	2		4		2 3		4
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4	1	6	4	1	6		4	1	6
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6			6				6		
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			30	<u> </u>	<u> </u>	□ @ 201		umbers Pattern	Play Math

### MisterNumbers Squares Playsheet: a fun adventure!

To create the Ones-Digits: Copy 0's and 5's to right of line. See video: http://goo.gl/h8l1XH Put 1-4-9-6 below each zero to right of line. Put 1-4-9-6 above each zero going UP. Draw Lines under Nines (done). Number the sections between lines starting with 0. (write 0-1-2-3-4-5-6-7-8-9-10 etc.)

To create the Tens-Digits: Tens go up by 1 after each line starting at 0. They start with (up by 0): 0-0-0-0, (up by ones): 1-2-3-4, (up by twos): 6-8-10-12-14-16, (up by threes): 19-22-25-28, etc.

**About:** Thanks to Kelly Enser for the original ideal. Squares are created quickly with simple patterns and simple addition. **This can be done on a blank sheet.** The pattern holds no matter how high you go. Many Patterns show up. How many can you see? "Adding by 7" and "Adding by 12" sections are split. Do have fun and let me know what you think and how fast you are: MisterNumbers@RightBrainMath.com

0	Harder: Squares	to 60 Challenge: Squares to 90
1	31	61
2	32	62
3	33	63
4	34	64
5	35	65
6	36	66
7	37	67
8	38	68
9	39	69
10	40	70
11	41	71
12	42	72
13	43	73
14	44	74
15	45	75
16	46	76
17	47	77
18	48	78
19	49	79
20	50	80
21	51	81
22	52	82
23	53	83
24	54	84
25	55	85
26	56	86
27	57	87
28	58	88
29	59	89
30	60	90

http://goo.gl/h8l1XH

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http://www.patternplaymath.com/

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42			42			92		
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50			50			100		

Square Deal
Play on a
20x20
Times Table
&

Multiplication

### Using SQUARES to find most hard Multiplication Facts

The Squares take us down the biggest numbers in the times tables. Working from there helps us find (or confirm) hard multiplication facts **using addition.** 

The other helpful part is that you **only need to use the SN (smaller number)** when you know how far apart the pair of numbers are. The hardest part of the 12x12 times table for students is the 6-12 numbers and these are easily figured out.

If Numbers are equal. They are a Square. Use and learn the Squares <a href="http://youtu.be/J6AKMvLzYwo">http://youtu.be/J6AKMvLzYwo</a> Learning the Squares makes this all possible.

- 1) Numbers are one apart:  $SN^2+SN$  (example is 3x4=3x3+3=12
- 2) Numbers are two apart: Square the number between them and subtract 1.  $(SN+1)^2 1$  (example  $3x5 = 4^2 1$ ).
- 3) Numbers are three apart: Use formula for two apart +SN.  $(SN+1)^2 1 + SN$ . (example  $6x9 = 7^2 1 + 6$ ).
- 4) Numbers are four apart:  $(SN+2)^2$  -4. (example 4x8= 6<sup>2</sup>-4).
- 5) Numbers are five apart: Use formula for four apart +SN.  $(SN+2)^2 4 + SN$ . (example  $4x9 = 6^2 4 + 4$ ).
- 6) Numbers are six apart:  $(SN+3)^2$ -9. (example  $6x12=9^2$ -9). Thinking of -9 as minus 10+1 may be easier.
- 7) Numbers are seven apart: Use formula for six apart +SN.  $(SN+3)^2 9 + SN$ . (example  $3x10 = 6^2 9 + 3 = 30$ .
- 8) Numbers are eight apart:  $(SN+4)^2$ -16. (example=  $4x12=8^2$ -16 Thinking of -16 as minus 20+4 may be easier.
- 9) Numbers that are nine apart: Use formula for eight apart +SN. (example=  $4x13 = 8^2 16 + 4$ ).
- 10) Numbers are ten apart:  $(SN+5)^2$  -25. (example =  $5x15 = 10^2$  -25).

You can continue this as far as your mental capacity allows. Eleven apart would be same formula as 10 apart +SN, Twelve apart would be SN+6-36. Etc.

This is based on:

$$(x+1)(x-1) = x^2-1$$
 (example 5x7:  $(x=6) = 6^2-1$ ) = 36-1 =35   
  $(x+2)(x-2) = x^2-4$  (example 5x9:  $(x=7) = 7^2-4$ ) = 48-4 =45   
  $(x+3)(x-3) = x^2-9$  (example 5x11:  $(x=8) = 8^2-9$ ) = 64-9 =55   
  $(x+4)(x-4) = x^2-16$  (example 6x14:  $(x=10) = 10^2-16$ ) = 100-16 =84

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### **Creating the 20x20 Times Tables with Directions**

17	Playfully Creating the 20x20 Times Tables with Directions
18	Full 20x20 Times Table with Diagonal Colors
19	An Earlier Version on the Times Table
20	How to Fill out the 20x20 Times Table with Diagonals
21	The Blank Times Table (with Ones and Twos filled in)
22	Empty Table with dotted lines on Squares for Ones and Tens
23	Ones of Squares filled in on right of dotted lines: 0-1-4-9-6-5
24	Ones and Tens of Squares filled in
25	Squares in Yellow Diagonal in Place
26	Squares Mirror Image on two sides of the Times Table
27	Multiplying Numbers One Apart with Stars
28	Multiplying Numbers One Apart in Place
29	Multiplying Numbers Two Apart with Arrows from Squares
30	Multiplying Numbers Two Apart Alone
31	Multiplying Numbers One and Two Apart
32	Multiplying Numbers Three Apart
33	Multiplying Numbers Four Apart with Arrows
34	Multiplying Numbers Four Apart
35	Multiplying Numbers Five Apart
36	Multiplying Numbers Six Apart
37	Multiplying Numbers Seven Apart
38	Multiplying Numbers Eight Apart
39	Multiplying Numbers Nine Apart
40	Multiplying Numbers Ten Apart
41	20x20 Times Table with Diagonals All numbers in place

### Playfully Creating the 20x20 Times Table Using Squares

Patterns are powerful. To see and use patterns in numbers make a student powerful and helps them enjoy math. Looking for patterns is a game, a puzzle, and it has long term benefits in math and elsewhere because all deep learning is learning to look at underlying patterns.

Let the student discover as many of the patterns as possible. They may well find some that you have never seen, even if working with this table. Refrain from showing them the patterns, and let them find them on their own

There are a couple ways to look at each set of numbers. Where are they on the Table? How far apart are they? What color is the box? What are the values of the diagonals in both directions?

This structure is based on the Squares of the numbers 1-20, which are designated by the yellow boxes from the top left (1x1=1) to the bottom right 20x20=400. The cool aspect of starting with the squares is that they go right at the biggest (hardest) numbers for kids: 6x6, 7x7, 8x8, 9x9, 10x10, 11x11, 12x12, etc

Diagonals are cool patterns. It becomes like a game. The clues are in the different ways to identify any set of numbers.

Half of the boxes are colored by diagonals.

What are the diagonal patterns in each direction?

What are the up and down patterns?

What are the right and left patterns?

Find any array (rectangle of boxes) starting from top left and what do you find?

### Calculating in your head, using squares and adding or subtracting (not multiplying).

Numbers that are even numbers apart are based on squaring the middle number.

Have them fill in as many as they know of the Squares, and look for patterns in the Ones and Tens of the Squares.

Have them fill in as many as they know about the white boxes next to, and below the Squares.

What are these numbers?

How many apart are they?

Is there any pattern they can find to move from the square to that white box?

What is the difference between diagonal white boxes right to left.

There is a series of Times Tables with the Squares filled in, then the one apart numbers filled in, then two apart, three apart, four apart, etc.

Students get a sense of accomplishment as they create the Times Tables. The are CREATING MATH. From patterns.

If you don't have a colored printer, this still works. The diagonals are clear, and it is easy to identify the squares and the two apart, four apart, six apart diagonals.

CREATING THE TIMES TABLE USING SQUARES: All Facts in Place

Create on the Diagonals from Squares and watch for Patterns

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20	20	40	09	80	100	120	140	160	180	200	220	240	260	280	300	320	340	360	380	400
19	19	38	57	92	95	119	119	119	171	190	209	228	247	799	285	304	323	342	361	380
18	<del>2</del>	36	24	72	06	119	119	144	162	180	198	216	234	252	270	288	306	324	342	360
17	17	34	21	89	82	119	119	136	153	170	187	204	221	238	255	272	289	306	323	340
16	<b>1</b> 0	32	48	64	80	96	112	128	144	160	176	192	208	224	240	256	272	288	304	320
15	15	30	45	99	75	96	105	120	135	150	165	180	195	210	225	240	255	270	285	300
14	14	28	42	26	<b>20</b>	84	86	112	126	140	154	168	182	196	210	224	238	252	266	280
13	13	<b>26</b>	39	25	<b>6</b> 2	<b>78</b>	91	104	117	130	143	156	169	182	195	208	221	234	247	260
12	12	24	36	48	09	72	84	66	108	120	132	144	156	168	180	192	204	216	228	240
11	1	22	33	44	22	99	77	<b>&amp;</b>	66	110	121	132	143	154	165	176	187	198	209	220
10	10	20	30	40	20	09	<b>20</b>	80	90	100	110	120	130	140	150	160	170	180	190	200
6	6	<del>1</del> 8	27	<b>30</b>	45	54	<b>63</b>	72	81	90	66	108	117	126	135	144	153	162	171	180
<b>∞</b>	∞	16	24	32	40	48	26	<b>64</b>	72	80	<b>&amp;</b>	66	104	112	120	128	136	144	152	160
7	^	<del>1</del>	21	<b>78</b>	35	42	49	26	<b>63</b>	20	77	<b>8</b>	91	<b>86</b>	105	112	119	126	133	140
9	9	12	<del>2</del>	24	30	36	42	48	<b>54</b>	9	99	72	<b>78</b>	84	90	96	102	108	114	120
<b>S</b>	ſΩ	2	15	20	25	30	35	40	45	20	22	9	<b>65</b>	70	75	8	82	9	92	100
4	4	∞	12	16	20	24	<b>58</b>	32	36	40	<b>4</b>	48	25	26	9	49	89	72	92	80
3	က	9	6	12	15	<del>2</del>	21	<b>24</b>	27	30	33	33	39	42	45	48	51	54	27	09
2	7	4	ၜ	<b>∞</b>	9	12	14	16	18	20	22	<b>24</b>	<b>5</b> 6	<b>78</b>	30	32	34	36	38	40
1	_	7	က	4	ΓÛ	စ	<b>^</b>	∞	6	9	7	7	13	14	15	16	17	<del>2</del>	19	<b>50</b>
òs	1	7	8	4	S	9	7	<b>∞</b>	6	10	=	12	13	14	15	16	17	18	19	20

Look for patterns in eight directions from each box  $\odot$  2015MisterNumbers Pattern Play Math

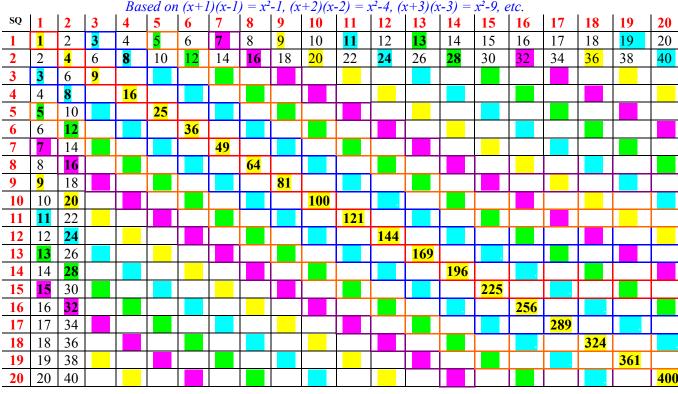
### CREATING THE TIMES TABLE USING SQUARES and plus and minus

© MisterNumbers Pattern Play Math 2015

20 x 20 Times Table Practice worksheet: fill it out or find any multiplication fact

It is fun. No multiplication needed. First: Easily learn the squares of 1-20 at https://goo.gl/wUIDs0 Subtract any two numbers you want to multiply and follow the rules below. You only use the SN (smaller number) and +&-. The formula is based on the fact that if numbers are 1-4-9-16-25 less than the middle square if they are 2-4-6-8-10 apart. Odd number apart? Use SN, find lower even number, and add SN. If you learn the squares you can you can figure out or confirm any multiplication fact. Half of boxes in the chart below are even numbers apart and colored. Find these and add SN for next clear box (odd apart).

- 1) Create the Squares to 20x20 (see MisterNumbers video <a href="https://goo.gl/wUIDs0">https://goo.gl/wUIDs0</a> YELLOW middle diagonal
- 2) Create **2X row and column** by adding each number to itself (**double 1**<sup>st</sup> **number**).
- 3) Create numbers 1 apart by adding SN (Smaller Number) to square of SN.
- 4) Create numbers 2 apart (blue) by add 1 to SN, square that, (square middle number) minus 1 (BLUE)
- 5) Create numbers 3 apart by adding 1 to SN, square that, minus 1 plus SN
- 6) Create numbers 4 apart (green) by adding 2 to SN, squaring that, minus 4 (GREEN)
- 7) Create numbers 5 apart by adding 2 to SN, squaring that, minus 4, plus SN
- 8) Create numbers 6 apart (pink) by adding 3 to SN, squaring that, minus 9 (PINK)
- 9) Create numbers 7 apart by adding 3 to SN, squaring that, minus 9, plus SN
- 10) Create numbers 8 apart (yellow) by adding 4 to SN, squaring that, minus 16 (NEXT YELLOW)
- 11) Create numbers 9 apart by adding 4 to SN, squaring that, minus 16, plus SN
- 12) Create numbers 10 apart (blue) by adding 5 to SN, squaring that, minus 25 (NEXT BLUE)



Middle Yellow diagonal = squares

Touching Blue diagonals = Squares -1

Touching Green diagonals = Squares -4

Touching Pink diagonals = Squares -9 (may be helpful to subtract 10 and add 1)

Touching Yellow diagonals = Squares -16 (may be helpful to subtract 20 and add 4)

Touching Blue diagonals = Squares - 25 etc. Add SN to get the white squares (odd numbers apart)

Multiplying 20 x 20 tables mentally: This system fills in all the big facts. Use multiplication for smaller facts.

Remember: you only need to know the SN and how far apart they are. Can be expanded to 50 x 50! Enjoy! -MisterNumbers

### 20 x 20 Times Table Practice worksheet: fill it out or find any multiplication2fact

It is fun. No multiplication needed. First: Easily learn the squares of 1-20 at <a href="https://goo.gl/wUIDs0">https://goo.gl/wUIDs0</a>
Playsheets for creating the squares to 50 are available. Notice the arrays that are numbered by boxes.

Create the squares down the middle yellow in the 20 x 20 Times Table Chart. The Ones and Twos are fairly easy and done in both directions. See that the Squares take you right down the middle, away from the safe shore. Yet creating the squares or finding one square is easy using the videos.

Notice the Purple diagonal boxes on both sides touching the squares. See the purple boxes that are filled in and add 3x5 is 15 and 6x4 is 24 on both sides. What do you notice about the touching purple boxes and yellow squares? Do you see any pattern?

Next check out the Green boxes that touch the purple boxes. Add 3x7=21 and 8x4=32 on both sides. What pattern do you notice between the green and the yellow squares? Between the Purple and Green boxes?

Hopefully you are seeing some cool patterns show up. Try the red boxes. What patterns do you see between the red boxes and the yellow squares? The Purple and the Red boxes? The Green and the Red?

Add some values to the white boxes. Notice about half of the squares are colored and half are white. What is the relationship between the colored and the White below or to the right?

If you need help or get stuck: Check below, but figure out as much as you can. It is really cool.

Middle Yellow diagonal = squares
Touching Blue/Purple diagonals = Squares -1
Touching Green diagonals = Squares -4
Touching Pink/red diagonals = Squares -9 (may be helpful to subtract 10 and add 1)
Touching Yellow diagonals = Squares -16 (may be helpful to subtract 20 and add 4)
Touching Blue/Purple diagonals = Squares -25 etc.

### White Squares?: Add the SN (smaller number of the two) to the colored squares above or to the left (completes the table).

Multiply Any Two numbers: Subtract any two numbers you want to multiply and follow the rules below. You only use the SN (smaller number) and +&-. The formula is based on the fact that if numbers are 1-4-9-16-25 less than the middle square if they are 2-4-6-8-10 apart. Odd number apart? Use SN, find lower even number, and add SN.

If you learn the squares you can you can figure out or confirm any multiplication fact. Half of boxes in the chart below are even numbers apart and colored. Find these and add SN for next clear box (odd apart).

- 1) Create the Squares to 20x20 (see MisterNumbers video https://goo.gl/wUIDs0 YELLOW middle diagonal
- 2) Create **2X row and column** by adding each number to itself (**double 1**<sup>st</sup> **number**).
- 3) Create numbers 1 apart by adding SN (Smaller Number) to square of SN.
- 4) Create numbers 2 apart (blue) by add 1 to SN, square that, (square middle number) minus 1 (BLUE)
- 5) Create numbers 3 apart by adding 1 to SN, square that, minus 1 plus SN
- 6) Create numbers 4 apart (green) by adding 2 to SN, squaring that, minus 4 (GREEN)
- 7) Create numbers 5 apart by adding 2 to SN, squaring that, minus 4, plus SN
- 8) Create numbers 6 apart (pink) by adding 3 to SN, squaring that, minus 9 (PINK)
- 9) Create numbers 7 apart by adding 3 to SN, squaring that, minus 9, plus SN
- 10) Create numbers 8 apart (yellow) by adding 4 to SN, squaring that, minus 16 (NEXT YELLOW)
- 11) Create numbers 9 apart by adding 4 to SN, squaring that, minus 16, plus SN
- 12) Create numbers 10 apart (blue) by adding 5 to SN, squaring that, minus 25 (NEXT BLUE)

Multiplying 20 x 20 tables mentally: This system fills in all the big facts. Use multiplication for smaller facts. Remember: you only need to know the SN and how far apart they are. Can be expanded to 50 x 50! Enjoy! - MisterNumbers

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Create Squares in Yellow Boxes using https://goo.gl/wUIDs0 Ones are 1-4-9-6 from 0 and Tens are 1-2-3-4 and 6-8-10-12-14-16 and 19-22-25-28 CREATING THE TIMES TABLE USING SQUARES: Colored Diagonals -1, 14, -9, -16, -25 ,Dx Square Souare Yellow Boxes from top left are Squares. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math salare Salate A Souare Solare solvare **>** Solare solution 16 3 6 Soliale of 10 11 5 10 11 × SOUTH solvare 8  $\infty$ **∞** Sollare 4 **%** , Cx sayare Solate sayare Saute **>** Ŋ Solate S  $\infty$ m 10 20 11 22 12 24 14 28 16 32  $\infty$ <del>2</del> IJ  $\infty$ S S  $\infty$ 

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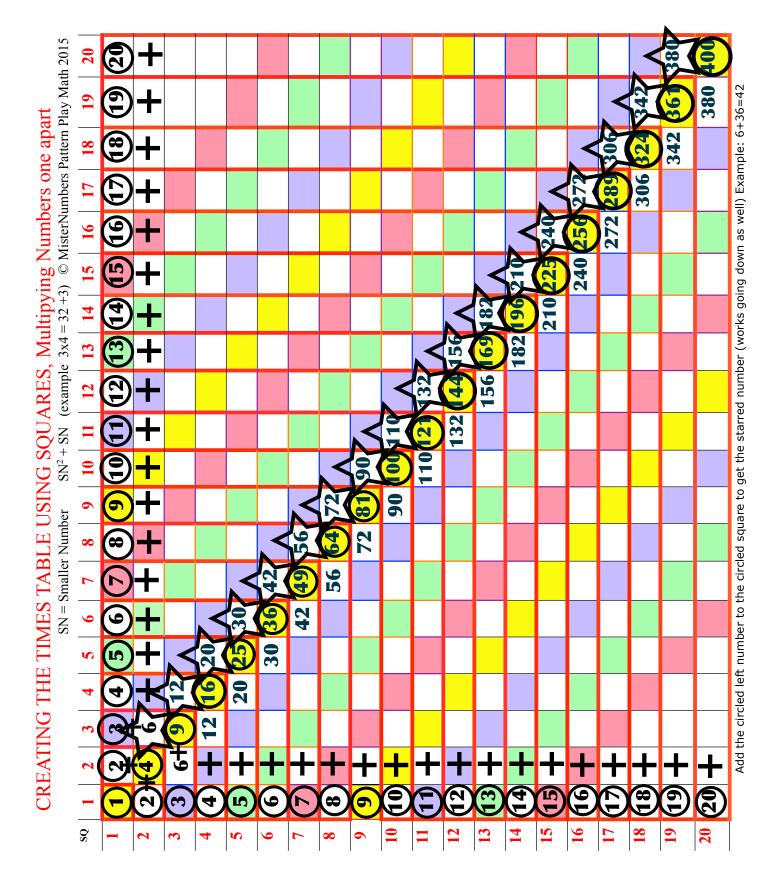
Create Squares in Yellow Boxes using https://goo.gl/wUIDs0 Ones are 1-4-9-6 from 0 and Tens are 1-2-3-4 and 6-8-10-12-14-16 and 19-22-25-28 CREATING THE TIMES TABLE USING SQUARES: Adding Ones of Squares 1-4-9-6-5 Yellow Boxes from top left are Squares. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math  $\overline{\phantom{a}}$ **1**Ŋ 4 <del>1</del>3 6  $\overline{\phantom{a}}$ \_  $\infty$  $\infty$ **^** Ŋ Ŋ S  $\infty$ 11 22 10 20 16 32  $\infty$  $\infty$ 4 Ŋ S **∞** 

Yellow Boxes from top left are Squares. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math

Create Squares in Yellow Boxes using https://goo.gl/wUIDs0 Ones are 1-4-9-6 from 0 and Tens are 1-2-3-4 and 6-8-10-12-14-16 and 19-22-25-2 CREATING THE TIMES TABLE USING SQUARES: Adding Yellow Squares (ex: 8x8) © 2015MisterNumbers Pattern Play Math 6 Yellow Boxes from top left are Squares. How would you find the numbers in the next white boxes? <del>1</del>3 6 5  $\infty$  $\infty$ Ŋ  $\infty$ 4 8  $\infty$ D  $\infty$  $\delta$  $\infty$ 

CREATING THE TIMES TABLE USING SOUARES: Mirror Image around Squares

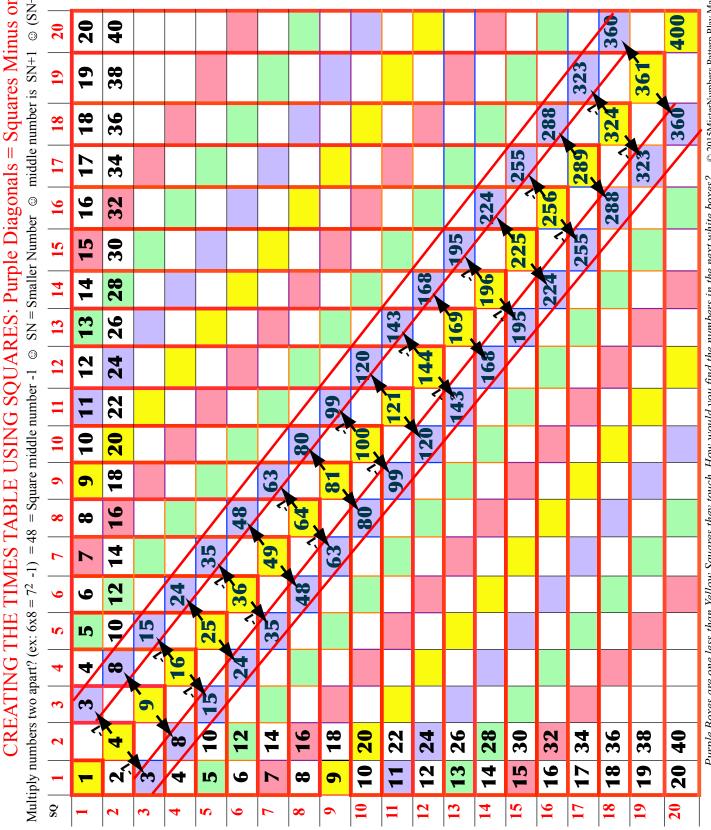
Numbers 8 apart: Yellow Box = Diagonal Square (middle number) - 16. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math



CREATING THE TIMES TABLE USING SQUARES and plus and minus © MisterNumbers Pattern Play Math 2015

20	20	40																	380	400
19	19	38																342	361	380
18	18	36															306	324	342	
17	17	34														272	289	306		
16	16	32													240	256	272			
15	15	30												210	222	240				
14	14	<b>78</b>											182	182 <mark>196</mark>	210					
13	13	<b>26</b>										156	169	182						
12	12	24									132	144	156							
11	7	22								110	121	132								
10	10	20							90	100	110									
9	6	18						72	81	90										
8	∞	16					<b>2</b> 6	<b>64</b>	72											
7	^	14				42	49	<b>2</b> 6												
9	9	12			30	36	42													
3	ΓÜ	10		20	25	30														
4	4	<b>∞</b>	12	16	20															
3	က	ဖ	6	12																
7	7	4	9	æ	10	12	14	16	18	20	22	24	<b>26</b>	<b>28</b>	30	32	34	<b>3</b> €	38	40
	<del>-</del>	7	8	4	r	9	7	∞	6	10	11	12	13	14	15	16	17	18	19	<b>20</b>
Š	1	7	8	4	w	9	7	<b>∞</b>	6	10	11	12	13	14	15	16	17	18	19	20

Multiply numbers two apart? (ex:  $6x8 = 7^2$  -1) = 48 = Square middle number -1 © SN = Smaller Number © middle number is SN+1 © (SN+1)<sup>2</sup> -1 CREATING THE TIMES TABLE USING SQUARES: Purple Diagonals = Squares Minus one



Purple Boxes are one less than Yellow Squares they touch. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math

CREATING THE TIMES TABLE USING SQUARES: Adding numbers two apart (ex: 6x8)

Purple boxes are one less than touching squares (ex:  $6x8 = 7^2$  -1) = 48 © SN = Smaller Number © middle number is SN+1 © (SN+1)<sup>2</sup>-1

20	<b>50</b>	40																360		400
19	19	38															323		361	
18	<del>1</del> 8	36														288		324		360
17	17	34													255		289		323	
16	16	32												224		256		288		
15	15	30											195		225		255			
14	14	28										168		196		224				
13	13	<b>5</b> 6									143		169		195					L
12	12	<b>24</b>								120		144		168						
111	7	22							66		121		143							
10	10	20						80		100		120								
6	6	<del>2</del>					<b>63</b>		84		66									
<b>%</b>	∞	16				48		64		8										
7	^	14			35		49		63											
9	9	17		24		36		48												
<b>S</b>	īυ	2	15	_	25		35													
4	4	<b>&amp;</b>		16	10	24														_
3	က		6		15				20					-					25	
2		4		<b>&amp;</b>	2	12	14	16	<del>2</del>	20	22	24	3 26	1 28	30	32	34	36	38	40
	7	7	8	4	ΙÜ	9	<b>^</b>	<b>∞</b>	9	2	7	12	13	14	15	19	17	<del>1</del> 8	19	20
SO	-	7	8	4	S.	9	7	<b>∞</b>	6	10	11	12	13	14	15	16	17	18	19	20

Purple Boxes are one less than Yellow Squares they touch. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math

Purple boxes are one less than touching squares (ex:  $6x8 = 7^2$  -1) = 48 © SN = Smaller Number © middle number is SN+1 ©  $(SN+1)^2$ -1 CREATING THE TIMES TABLE USING SQUARES: Adding numbers two apart (ex: 6x8)

20	20	40																360	380	400
19	19	38															323	342	361	380
18	18	36														288	306	324	342	360
17	17	34													255	272	289	306	323	
16	16	32												224	240	256	272	288		
15	15	30											195	210	225	240	255			
14	14	<b>28</b>										168	182	196	210	224				
13	13	26									143	156	169	182	195					
12	12	24								120	132	144	156	168						
11	7	22							66	110	121	132	143							
10	10	20						80	90	100	110	120								
6	6	<b>1</b> 8					<b>63</b>	72	81	90	66									
œ	∞	16				48	<b>2</b> 6	<b>64</b>	72	80										
7	7	14			35	42	49	<b>2</b> 6	63											
9	9	12		24	30	36	42	48												
S	Ŋ	10	15	20	25	30	35													
4	4	<b>∞</b>	12	16	20	24														
3	က	9	6	12	15															
7	7	4	9	<b>&amp;</b>	10	12	14	16	18	20	22	24	26	28	30	32	34	36	38	40
1	7	7	ಣ	4	ιυ	9	7	œ	6	10	11	12	13	14	15	16	17	<b>4</b>	19	20
òs	1	7	က	4	w	9	7	∞	6	10	11	12	13	14	15	16	17	18	19	20

© 2015MisterNumbers Pattern Play Math Purple Boxes are one less than Yellow Squares they touch. How would you find the numbers in the next white boxes?

CREATING THE TIMES TABLE USING SQUARES: Adding numbers three apart (ex: 3x6) (SN+1)2+SN -1

Numbers 3 apart: Find Purple Box (Square -1) and add SN How would you find the numbers in the next green boxes? © 2015MisterNumbers Pattern Play Math

		•	•		•				٠										
` '	7	3	4	2	9	7	<b>«</b>	6	10	11	12	13	14	15	16	17	18	19	20
, -	7	က	4	īύ	9	_	∞	6	10	7	12	13	14	15	16	17	<b>4</b>	19	20
	4	9		10	12	4	16	<del>1</del> 8	20	22	24	<b>26</b>	28	30	32	34	36	38	40
	9	6	12		18	77,													
		12	16	20		28	35												
•	10		20	25	30		40	45											
	12	18		30	36	42		<b>54</b>	9										
• •	4	21	28		42	49	<b>2</b> 6		20	1									
	16		32	40		26	64	72		88	96								
	8			45	54		72	81	90		108	117							
	20				99	70		90	90 100 110	110		130	140						
	22					11	88		110	110 121	132		154	165					
	24						96	108		132	132 144 156	156		180	180 192				
	<b>26</b>							117	117 130		156	156 169 182	182		208	221			
	28								140	140 154	1	182	196	196 210		238	252		
	30									165	180		210	210 225	240		270	285	
	32										192	208		240	256	272		304	320
	34											221	221 238		272	272 <mark>289</mark> 306	306		340
	36												252	270		306	324	342	
	38													285	304		342	361	380
	40														320	340		380	400

MisterNumbers Pattern Play Math Worksheets.indd 33

CREATING THE TIMES TABLE USING SQUARES: Adding numbers four apart (ex: 2x6)

		<b>2</b> 0		Smaller Number	Numbe	#: -	(SN+2)~ -4	4. 4.	ex: 7	ex: $2x6 = 4^{2}$	4	=1.7			© Misi	terNum	bers Pa	ttern Pla	© Misternumbers Pattern Play Math 2015	C107
SQ	П	2	ဗ	4	S	9	7	<b>∞</b>	6	10	11	12	13	14	15	16	17	18	19	20
1	1	7	က	4	Ŋ	9	7	∞	6	10	7	12	13	14	15	<b>1</b> 0	17	<b>18</b>	19	<b>70</b>
7	7	4	9	<b>∞</b>	10	12	14	16	<b>18</b>	20	22	24	26	28	30	32	34	36	38	40
8	3	9	6	12	15	<del>2</del>	21													
4	4	<b>∞</b>	12	16	20	24	<b>28</b>	32												
ν.	Ŋ	2	15	20	25	30	35	40	45											
9	9	12	<del>2</del>	24	30	36	42	48	24	09										
7	7	14	21	<b>28</b>	35	42	49	26	<b>63</b>	20	11									
∞	<b>∞</b>	16		32	40	48	26	<b>64</b>	72	80	88	96								
6	6	18			45	<b>54</b>	63	72	81	90	66	108	117							
10	10	20				09	92	80	06	100	110	120	130	140						
#	7	22					1,	<b>&amp;</b>	66	110	121	132	143	154	165					
12	12	24						96	108	120	132	144	156	168	180	192				
13	13	26							117	130	143	156	169	182	195	208	221			
14	14	28								140	154	168	182	196	210	224	238	252		
15	15	30									165	180	195	210	225	240	255	270	285	
16	16	32										192	208	224	240	256	272	288	304	320
17	17	34											221	238	255	272	289	306	323	340
18	<b>18</b>	36												252	270	288	306	324	342	360
19	19	38													285	304	323	342	361	380
20	20	40														320	340	360	380	400
1	M L	,	1. 17:22	7	c	1:	5/ 1	Í	٤	:	į				]	٥				

Numbers 4 apart: Find Green Box on diagonal (Square -4) How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattem Play Math

1   2   3   4   5   6   7   8   9   10   11   12   13   14   15   16   17   18   19   20     2   2   4   6   8   10   12   14   16   18   20   22   24   26   28   30   32   34   36   38   40     3   3   6   9   12   15   18   21   24   24   25   24   26   28   30   32   34   36   38   40     4   8   12   16   20   24   28   32   36   24   25   24   25   24   25   24   25   24   25   25			SN =	EAI Small	CREATING TH SN = Smaller Number	THI	VIII. S	IMES TAB (SN+2) <sup>2</sup> -4 +SN	IABJ 4 +SN	CE C	$\frac{1511N}{2x7} = 4$	42 -4	Ex: $2x7 = 4^2 - 4 + 2 = 14$	KES:	Add	ing r	numb AisterN	ers fr umbers	ve ap	1E TIMES TABLE USING SQUARES: Adding numbers five apart (ex: $2x/$ ) (SN+2) <sup>2</sup> -4 +SN ex: $2x7 = 4^2$ -4 +2 =14 © MisterNumbers Pattern Play Math 2015	2X, th 201:
1         2         3         4         5         6         7         8         9         10         11         12         14         16         18         10         12         14         16         18         10         12         14         16         18         20         22         24         26         28         30         32         34         36         38         36         40         45         60         60         7         60         7         60         7         60         7         8         9         10         110         110         110         110         110         110         110         110         110         110         110         110         110         110         110         110         110         110	òs	1	7	3	4	2	9	7	<b>%</b>				12	13	14			17	18	19	20
2         4         6         8         10         12         14         16         18         20         22         24         26         28         30         32         34         36         38         38         34         36	_	_	7	က	4	rv	9	7	∞			7		13	14	15	16	17	18	19	<b>20</b>
3         6         9         12         18         21         24         28         32         36         48         56         66         370         77         84         48         56         66         77         84         56         48         56         64         72         80         88         96         104         56         77         84         96         104         77         84         96         106         107 <th>7</th> <th>7</th> <th>4</th> <th>9</th> <th>∞</th> <th>2</th> <th>12</th> <th>14</th> <th></th> <th></th> <th></th> <th>22</th> <th></th> <th>26</th> <th>28</th> <th>30</th> <th>32</th> <th>34</th> <th>36</th> <th>38</th> <th>40</th>	7	7	4	9	∞	2	12	14				22		26	28	30	32	34	36	38	40
4         8         12         16         24         28         36         4         50         45         50         46         66         66         66         67 <th>က</th> <th>က</th> <th>9</th> <th>6</th> <th>12</th> <th>15</th> <th>18</th> <th>21</th> <th>24</th> <th></th>	က	က	9	6	12	15	18	21	24												
5         10         15         20         25         30         45         50         66         70         77         84         70         77         84         70         77         84         70         77         84         70         77         84         70         77         84         70         77         84         70         77         84         70         77         84         80         100         100         100         100         100         100         11	4	4	∞	12	16	20	24	28	32	36											
6         12         18         24         30         48         56         63         70         77         84         6         6         6         6         6         7         84         6         6         7         84         7         84         7         84         7         84         7         84         7         84         8         96         104         17         126         176	w	D	2	15	20	25		35			20										
7         14         21         28         35         42         49         56         64         72         80         88         96         104         6         7         80         88         96         104         7         8         96         104         7         8         96         100         110         120         130         140         150         7         8         96         100         110         120         130         140         150         140         110         120         130         140         150         140         140         150         140         140         150         140         140         150         140         140         150         140         150         140         150         140         150         140         150         140         150         140         150         140         150         1	9	9	12	<del>2</del>	24	30	36	42				99									
8         16         24         32         40         86         104         10         104         10         10         10         10         10         10         10         117         126         0         0         10         110         120         10         117         126         0         0         100         110         120         130         140         150         10         110         120         130         140         150         100         110         120         130         140         150         160         170	7	^	4	21	<b>28</b>	35	42	49				77	84								
9         18         36         45         54         63         72         81         90         99         108         117         126         7         80         90         100         110         120         130         140         150         7         8           11         22         50         66         77         88         99         110         121         132         143         154         165         176	∞	<b>∞</b>	16	24	32	40	48					<b>88</b>		104							
10         20         50         60         70         80         90         110         120         130         140         150	6	6	<del>2</del>		36	45	54	63	_						126						
12       24       66       77       88       99       110       121       144       156       168       180       192       204       8         12       24       84       96       108       120       182       195       208       221       234         14       28       104       117       130       144       156       169       182       195       208       221       234       256         15       30       126       140       154       168       182       195       210       224       238       252       266         16       32       32       32       32       32       32       32       364       368         17       34       36       32	10	10	20			20	9	29	_		001	110	120	130	140	150					
12       24       84       96       108       120       132       144       156       168       180       192       204       84       96       104       117       130       180       182       195       208       221       234       234       252       266       221       238       252       266       252       240       255       270       285       270       285       270       285       270       285       270       285       270       286       272       288       304       323       342       340       323       342       340       380 <th>11</th> <td>11</td> <td>22</td> <td></td> <td></td> <td></td> <td>99</td> <td>77</td> <td>_</td> <td></td> <td>110</td> <td></td> <td>132</td> <td></td> <td>154</td> <td></td> <td>176</td> <td></td> <td></td> <td></td> <td></td>	11	11	22				99	77	_		110		132		154		176				
13         26         104         117         130         143         156         169         182         195         208         221         234         236         252         266           14         28         30         126         140         154         168         182         196         210         224         238         252         266           15         30         30         30         30         30         30         30         30         30           16         32         30         30         30         30         30         30         30         30           17         34         36         30         30         30         30         30         30         30           18         36         30<	12	12	24					84		108	120		144	156	168			204			
14         28         126         140         154         168         182         196         210         224         238         252         266           15         30         150         165         180         195         210         225         240         255         270         285           16         32         32         30         30         30         30         30         30           17         34         36         36         37         30         30         30         30         30           18         36         36         36         30         30         30         30         30         30         30           20         40         30	13	13	26						104	117	130	143	156	169	182			221	234		
15         30         150 165 180 195 210         225 240 255 270 285         270 285 270 288 304           16         32         22         208 224 240 256 272 288 304         272 289 306 323           17         34         204 221 238 255 272 289 306 323         304 323           18         36         32         32         32           19         38         30         324 252 270 288 306 324 342 342         36         36           20         40         30         30         320 340 360 380         360 380	14	14	28							126	140	154	168	182	196			238		266	
16         32         82         176         192         208         224         240         256         272         288         304           17         34         8         8         8         8         8         10         8         8         306         323         323         323         323         323         323         323         323         323         323         324         324         324         325         324	15		30							-	20	165	180		210		240	255		285	300
17         34         8         204         221         238         255         272         289         306         323           18         36         36         324         325         270         288         306         324         342           19         38         38         36         324         323         342         361           20         40         30         320         320         340         360         380	16	16	32								,_	176	192	208	224	240	256	272	288	304	320
18         36         23         23         25         270         288         306         324         342           19         38         26         285         304         323         342         361           20         40         30         320         340         360         380         380	17	17	34									•	204	221	238		272	289	306	323	340
19         38         266         285         304         323         342         361           20         40         30         320         340         360         380         380	18	18	<b>3</b> 6										• •	234	252	270	288	306	324	342	360
20         40         300         320         340         360         380	19	19	38											· ·	<b>5</b> 90			323	342	361	380
	20	20	40													300	320	340	360		400

CREATING THE TIMES TABLE USING SQUARES: Adding numbers six apart (ex: 2x8)

Numbers 6 apart: Red Box = Diagonal Square (middle number) - 9. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math

CREATING THE TIMES TABLE USING SQUARES: Adding numbers seven apart (ex: 2x9)

20	<b>50</b>	40											260	280	300	320	340	360	380	400
19	19	38										228	247	<b>266</b>	285	304	323	342	361	380
18	18	<b>3</b> €									198	216	234	252	270	288	306	324	342	360
17	17	34								170	187	204	221	238	255	272	289	306	323	340
16	16	32							144	160	176	192	208	224	240	256	272	288	304	320
15	15	30						120	135	150	165	180	195	210	225	240	255	270	285	300
14	14	28					<b>86</b>	112	126	140	154	168	182	182 <mark>196</mark>	210	224	238	252	266	280
13	13	26				78	91	104	117	130	143	156	169		195	208	221	234	247	960
12	12	24			9	72	84	66	108	120	132	144	156	168	180	192	204	216	228	
11	7	22		44	22	99	7	<b>&amp;</b>	66	110	121	132	143	154	50 165	176	187	198		
10	2	20	30	40	20	3	2	8	90	100	110	120	130	140	7	160	170			
6	6	<b>4</b>	27	36	45	54	<b>63</b>	72	8	90	66	108	1117	2 126	20 135	144				
<b>∞</b>	∞	16	24	32	40	48	26	64	72	8	88	66	104	7	12(					
7	_	14	27	<b>7</b>	35	42	49	26	<b>63</b>	70	77	84	91	86						
9	9	12	18	24	30	) 36	42	48	54	9	99	72	78							
S	īΟ	2	15	6 20	0 25	1 30	8 35	2 40	6 45	0 20	1 55	9								
4	4	<b>&amp;</b>	12	2 16	5 20	8 24	1 28	3	2 36	0 40	44									
3	<u>ლ</u>	9	6	7	7	7	4 21	6 24	8 27	0 30	2	4	9	<b>&amp;</b>	0	2	4	و	<b>&amp;</b>	ے
1 2	7	2	9	8	10	6 12	7 1,	8	9	10 20	11 22	2 24	3 26	4 28	5 30	6 32	7 34	18 36	9 38	20 40
so 1		2	63	4	ις) Π')	9	7	∞ ∞	6	10	11	12 1	13	14	15	16 1	17 1	18	19	20

 $\ensuremath{\text{@}}\xspace 2015\ensuremath{\text{MisterNumbers}}\xspace$  Pattern Play Math Numbers 7 apart: Red Box = Diagonal Square (middle number) - 9 + 5N. How would you find the numbers in the next yellow boxes?

# CREATING THE TIMES TABLE USING SQUARES: Adding numbers eight apart (ex: 2x10)

© 2015MisterNumbers Pattern Play Math How would you find the numbers in the next white boxes? Numbers 8 apart: Tellow Box = Diagonal Square (middle number) - 16.

CREATING THE TIMES TABLE USING SQUARES: Adding numbers Nine apart (ex: 2x11)

© MisterNumbers Pattern Play Math 2015  $(SN+4)^2 - 16 + SN$  ex:  $2x111 = 6^2 - 16 + 2 = 22$ SN = Smaller Number

																			I		
20	<b>20</b>	40									220	240	260	280	300	320	340	360	380	400	
19	19	38								190	209	228	247	266	285	304	323	342	361	380	
18	<del>2</del>	36							162	180	198	216	234	252	270	288	306	324	342	360	١
17	17	34						136	153	170	187	204	221	238	255	272	289	306	323	340	
16	16	32					112	128	144	160	176	192	208	224	240	256	272	288	304	320	
15	15	30				96	105	120	135	150	165	180	195	210	225	240	255	270	285	300	
14	14	28			20	84	<b>86</b>	112	126	140	154	168	182	196	210	224	238	252	266	280	
13	13	<b>26</b>		25	<b>6</b> 2	<b>28</b>	91	104	117	130	143	156	169	182	195	208	221	234	247	260	
12	12	24	36	48	09	72	84	66	108	120	132	144	156	168	180	192	204	216	228	240	
11	7	22	33	44	52	99	77	<b>&amp;</b>	66	110	121	132	143	154	165	176	187	198	209	220	
10	10	20	30	40	20	09	<b>20</b>	80	90	100	110	120	130	140	150	160	170	180	190		
6	6	18	27	<b>3</b> €	45	<b>54</b>	<b>63</b>	72	81	90	99	108	117	126	135	144	153	162			
<b>∞</b>	∞	16	24	32	40	48	<b>2</b> 6	<b>64</b>	72	80	88	66	104	112	120	128	136				
7	7	14	21	<b>78</b>	35	42	49	<b>2</b> 6	<b>63</b>	<b>20</b>	77	84	91	<b>86</b>	105	112					
9	9	12	<del>2</del>	24	30	36	42	48	<b>54</b>	09	99	72	<b>78</b>	84	90						
S	rU	2	15	<b>20</b>	25	30	35	40	45	20	22	99	<b>65</b>	<b>20</b>							_
4	4	∞	12	16	20	24	<b>78</b>	32	<b>3</b> 6	40	44	48	25								
<u>e</u>	က	9	6	12	15	18	21	24	27	30	33	33									
2	7	4	9	<b>∞</b>	10	12	14	16	18	20	22	<b>54</b>	<b>26</b>	<b>78</b>	30	32	34	36	38	40	
	-	7	ಣ	4	ΙÜ	9	^	∞	6	19	11	12	13	14	15	16	17	18	19	<b>50</b>	
òs		7	က	4	S	9	7	<b>∞</b>	6	10	11	12	13	14	15	16	17	18	19	20	Ī

Numbers 8 apart: Yellow Box = Diagonal Square (middle number) - 16. How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math

## CREATING THE TIMES TABLE USING SQUARES: Adding numbers Ten apart (ex: 2x12)

Numbers 10 apart: Purple Box = Diagonal Square - 25 How would you find the numbers in the next white boxes? © 2015MisterNumbers Pattern Play Math

CREATING THE TIMES TABLE USING SQUARES: All Facts in Place

Create on the Diagonals from Squares and watch for Patterns © MisterNu

© MisterNumbers Pattern Play Math 2015

20	<b>70</b>	40	09	80	100	120	140	160	180	200	220	240	260	280	300	320	340	360	380	400
19	19	38	27	9/	92	119	119	119	171	190	209	228	247	<b>266</b>	285	304	323	342	361	380
18	<del>2</del>	36	54	72	90	119	119	144	162	180	198	216	234	252	270	288	306	324	342	360
17	17	34	21	89	82	119	119	136	153	170	187	204	221	238	255	272	289	306	323	340
16	16	32	48	64	80	96	112	128	144	160	176	192	208	224	240	256	272	288	304	320
15	15	30	45	09	75	90	105	120	135	150	165	180	195	210	225	240	255	270	285	300
14	14	28	42	<b>2</b> 6	20	84	<b>86</b>	112	126	140	154	168	182	196	210	224	238	252	266	280
13	13	26	39	52	<b>6</b> 2	78	91	104	117	130	143	156	169	182	195	208	221	234	247	260
12	12	24	36	48	09	72	84	66	108	120	132	144	156	168	180	192	204	216	228	240
11	7	22	33	44	22	99	77	<b>&amp;</b>	66	110	121	132	143	154	165	176	187	198	209	220
10	10	20	30	40	20	09	70	80	90	100	110	120	130	140	150	160	170	180	190	200
6	6	18	27	36	45	<b>5</b> 4	<b>63</b>	72	81	90	66	108	117	126	135	144	153	162	171	180
<b>∞</b>	<b>∞</b>	16	24	32	40	48	<b>2</b> 6	<b>64</b>	72	80	<b>&amp;</b>	66	104	112	120	128	136	144	152	160
7	^	14	21	<b>28</b>	35	42	49	<b>2</b> 6	63	70	77	84	91	86	105	112	119	126	133	140
9	9	12	<del>2</del>	24	30	36	42	48	54	09	99	72	78	84	90	96	102	108	114	120
3	гU	2	7	20	25	30	35	40	45	20	22	99	<b>65</b>	20	75	<b>8</b>	82	96	92	100
4	4	<b>∞</b>	12	16	20	24	<b>58</b>	32	36	40	4	48	52	<b>2</b> 6	99	<b>6</b> 4	89	72	9/	08
3	က	9	6	12	7	18	21	24	27	30	33	33	39	42	45	48	21	54	57	09
2	7	4	9	<b>∞</b>	2	12	4	16	<b>18</b>	20	22	24	<b>26</b>	28	30	32	34	36	38	40
1	1	7	ಣ	4	ιυ	9	<b>^</b>	<b>∞</b>	6	10	7	12	13	14	15	16	17	<del>2</del>	19	20
OS		7	က	4	v	9	7	∞	6	10	11	12	13	14	15	16	17	18	19	20
•2				1			1			-			1		-	-	1	-		14

Look for patterns in eight directions from each box © 2015MisterNumbers Pattern Play Math

### Number Wheels

Ten Adds and Multiplication

### Ten-Adds (Pairs of numbers that add up to 10)

ALL ADDITION FALLS WITH PLUS OR MINUS 2 OF THE FIVE-ADDS OR TEN-ADDS Start with the 5 at the bottom of the Ten-Add Number Wheel. It is alone, so double it and it add up to ten. Think of your two hands. You have five fingers on each hand, and ten finger in all. A great way to look at numbers adding up to ten. Have a student look at his hands and hold a ruler between the hands. Still ten fingers, but separated by the ruler into 5 + 5. Move the ruler to divide the fingers into 4+6. Still 10 fingers. 3+7, 2+8, 1+9. 0+10. Then slowly step down to 9+1, 8+2, etc down to 0+10. Keep asking how many fingers they have.

The other way to do this is to use five coins in each hand (pennies or quarters?). This is 5+5=10. Place one coin from the left hand into the right and you have 4+6=10. Still ten coins. Add another coin makes it 3+7=10. Go down to 0+10=10 and then back to 10+0=10. Always ten coins and remembering which numbers go together.

Now look at the Ten-Add Number Wheel and have kids see that the numbers across from each other (making parallel lines) add up to 10. If they can visualize the wheel, they can SEE the Ten-Adds. Give them one number and see if they can SEE the Ten-Add pair. Spend time daily to anchor these Ten-Add pairs.

Give kids numbers that add up to ten, and let them respond with "10". Give them 7+4 and see if they can identify that it is one more than a ten-add, or 11. Give them orally or worksheets that are within one of Ten-adds (pairs of numbers that add up to 9, 10, or 11.)

Stretch this to numbers that add up to 8, 9, 10, 11, or 12 (within 2 of a Ten-Add).

This also includes numbers that add up to 20, 30, 40 etc.

### Five-Adds (Pairs of numbers that add up to 5)

Do the same thing with a Five-Add Number Circle. Numbers that add up to 5 or 15 (end in 5) create vertical lines on the number wheel. Use the ruler with one hand and separate the fingers into 1+4=5, 2=3=5, 3+2=5, 4+1=5 and 5+0=5. This is the middle and the right vertical lines on the Number Wheel. Ask students about the number pairs on the left. They all add up to 15. 6+9=15, 7+8=15, 8+7=15, and 9+6=15.

These numbers can also be thought of as "more than 5" add up to 5 that way (6+9 becomes 1+4=5) Work with students to anchor the numbers that add up to 5 orally or with worksheets. Expand this to plus or minus 2 (3 to 7).

### Nine-Adds (Pairs of numbers that add up to 9)

Nine adds are parallel, and down one from Ten-Adds. Cool. If you say the numbers going around clockwise, they also give you the Nines times tables: 09-18-27-36-45-54-63-72-81-90.

### **Cube Numbers and Ten Adds**

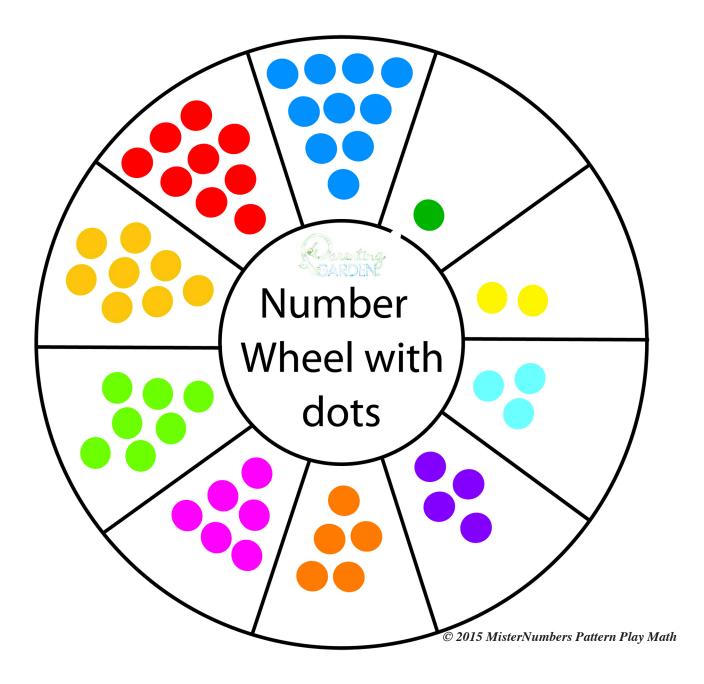
Another place that Ten Adds show happens when any number is cubed.

Numbers ending in:	Cube ends in:
0	0
1	1
2	8
3	7
4	4
5	5
6	6
7	3
8	2
9	9

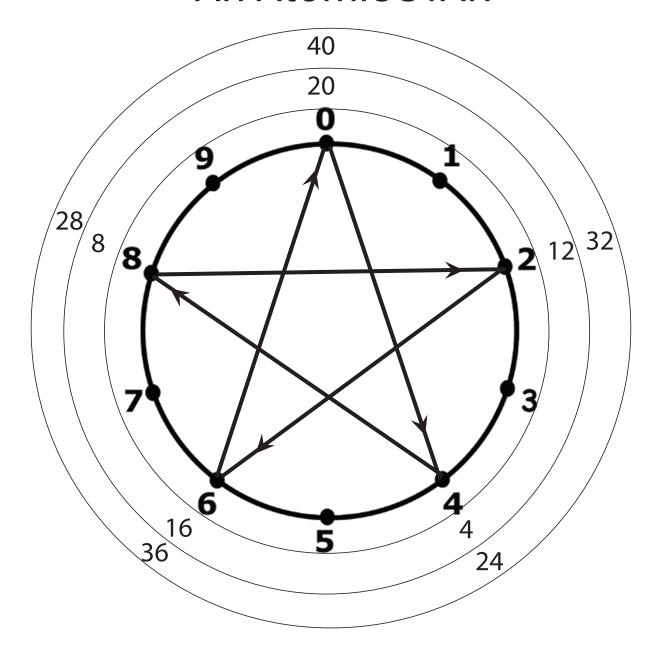
Most cubes end in the same number as the Ones of the root number.

The four exceptions are 2, 3, 7, and 8. All of them end in their Ten-Add pair: 2-8, 3-7, 7-3, and 8-2.

### Visualize Number Wheels



### Fours on a Number Circle: An Atomic STAR



Go around the numbers 4, 8, 2, 6, and 0 in the circle and make a STAR. Each time you reach 0, jump out one ring and go around again clockwise. The rings keep getting bigger and bigger and contain all the Fours.

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### Create 2s, 4s, 6s, 8s on these tables

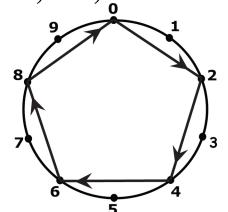
### NUMBER WHEEL TABLES ARE IN ROWS OF 5: 5, 10, 15, 20, ETC ©MisterNumbers Pattern Play Math

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
	<u> </u>			
			@ 2015 15: 4 N	ımhors Pattorn Play Mat

Create the 2s, 4s, 6s, 8s, and 12s, 14s, 16s, 18s

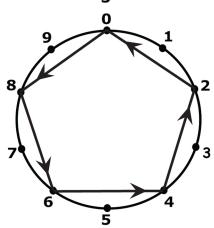
Create your	Own Two	and Twelves
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_				~	
x5	<b>_0</b>	8	6	4	2
x10	_0	8	6	4	2
x15	0	8	<b>6</b>	4	2
x20	0	8	6	4	2



**Create your Own Eights and Eighteens** 

· ·					
8	6	4	2	0	x5
8	<u>6</u>	4	2	0	x10
8	6	4	2	0	x15
8	<u>6</u>	4	2	0	x20



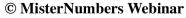
**Create your Own Fours and Fourteens** 

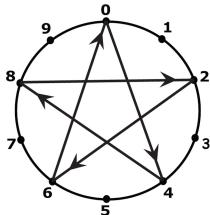
 4
 8
 2
 6
 0
 x5

 4
 8
 2
 6
 0
 x10

 4
 8
 2
 6
 0
 x15

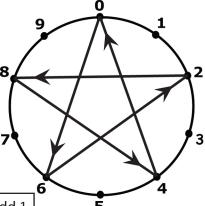
 4
 8
 2
 6
 0
 x20





**Create your Own Sixes and Sixteens** 

·					
6	2	8	_4	0	x5
6	2	8	4	0	x10
6	2	8	4	0	x15
<u>6</u>	2	8	4	<u></u> 0	x20



The ones-digits repeat for each factor set. Start the tens-digits with 0 and add 1 each time the column has a smaller number to its left, indicated by an 1 above

© 2015 MisterNumbers Pattern Play Math

### FREE NUMBER WHEEL Iphone APP BY MISTERNUMBERS

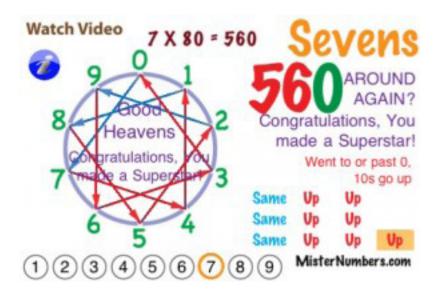
I have FIVE IPHONE APPS and I have temporarily made them all FREE (ENJOY) This one allows kids to create all numbers on the Number Wheel from 1-9. Link is

Wheel Math Wheel Fun Iphone App http://itunes.apple.com/us/app/wheel-math-wheel-fun/id387151566?mt=8

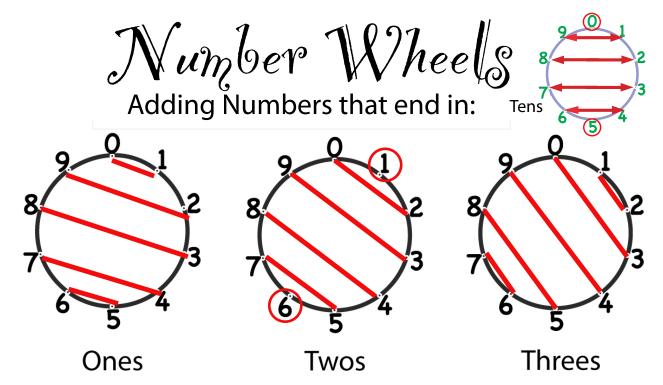
- 2) TTT †imes Table http://itunes.apple.com/us/app/tic-tac-toe-times-table/id395176671?mt=8
- 3) Wheel math 4 U http://itunes.apple.com/us/app/wheel-math-4-u/id395487961?mt=8
- 4) TTT Threes http://itunes.apple.com/us/app/tic-tac-toe-threes/id400623591?mt=8
- 5) TTT Sevens http://itunes.apple.com/us/app/tic-tac-toe-sevens/id400622245?mt=8

The Wheel Math apps work on iphone, but not on ipads, the other three work on both iphone and ipad.

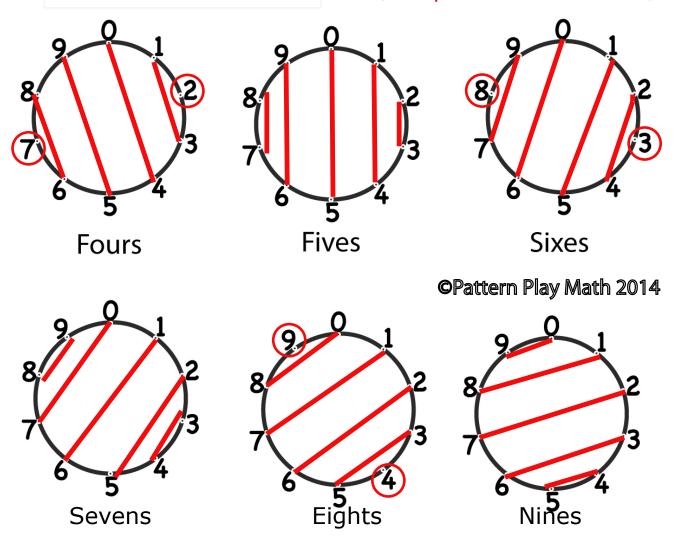
-MisterNumbers



### Addition on Number Wheels



Add circled numbers to themselves (examples 1+1=2 and 6+6=12)



### **Instructions for Learning Addition on the Number Wheel**

Look at any or all of the Addition Number Circles.

Let kids explore these ten number wheels. What do they see? What can they figure out? Let them own it!

Help for you or them if needed:

Let's start with 4: Pairs of Numbers whose sum ends in Four.

Look at the two ends of the arrow

Look at the circled numbers that are left alone

Add any of these two numbers and the sum will end in 4

To visualize this, start with seeing in your head the number wheel with 0 on top and 5 at the bottom.

It will help to make your own

Now see a line from 0 to any other number on the wheel.

Those two numbers will easily add up to the number other than 0, right? Example 0 and 9 = 9

See that all parallel lines add up to that number. Example 8 +1, 7 and 2, 6 and 3, 5 and 4, and their opposites.

With another even number (example 8) 0 and 8 add up to 8.

Also 1 and 7, 2 and 6, 3 and 5.

Even numbers leave two numbers alone on the outside, here the 4 and 9 are on the edge without a paired number.

DOUBLE these numbers: 4 plus 4 = 6 and 9 plus 9 = 18. These numbers also end in 8.

Imagine a parallel line touching the circle starting at the 4 and see in your mind another 4 at the end of that line, Or a nine at the end of the line from the 9.

This will be true for all even numbers.

Draw 0 to 6 and parallel lines to 1 and 5, 2 and 4, 9 and 7. The sum of these all numbers end in 6. 3 and 8 are alone on the edge. Double 3 and 8 to get numbers ending in 6

Draw 0 to 4 and parallel lines to 1 and 3, 9 and 4, 8 and 6. The sum of these numbers all end in 4. 2 and 7 are alone on the edge. Double 2 and 7 to get numbers ending in 4.

Draw 0 to 2 and parallel lines to 9 and 5, 8 and 4, 7 and 5. The sum of these all numbers end in 2. 1 and 6 are alone on the edge. Double 1 and 6 to get numbers ending in 2

Numbers that add up to ten ending in 0, another even number

You can't draw a (example 0) 0 and 8 add up to 8.

Look at the numbers that add up to ten Start with 5 and 5. Circle the 5.

Imagine 5 pennies in each hand. You have ten pennies, right?

Take one from your right hand and put it in your left hand. You still have 10 pennies! 6 and 4

Put another penny from your right hand and put it in your left hand. You still have 10 pennies! 7 and 3 = 10

Put another penny from your right hand and put it in your left hand. You still have 10 pennies! 8 and 2 = 10

Put another penny from your right hand and put it in your left hand. You still have 10 pennies! 9 and 1 = 10

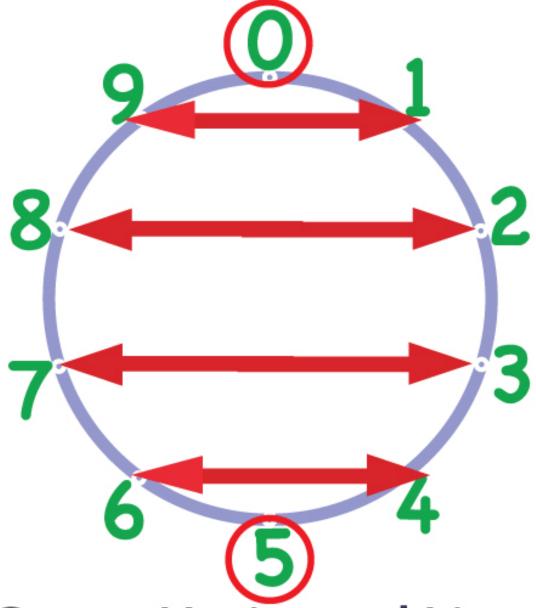
All these pairs of numbers have created horizontal lines. With 5 on the bottom and 0 on the top alone.

Put another penny from your right hand and put it in your left hand. You still have 10 pennies! 10 and 0 = 10

Notice that the arrows from 0 and to the right add up to the number: example is 5: 0 and 5, 1 and 4, 2 and 3 = 5 Lines on the left = 15: 6 plus 9 and 7 plus 8.

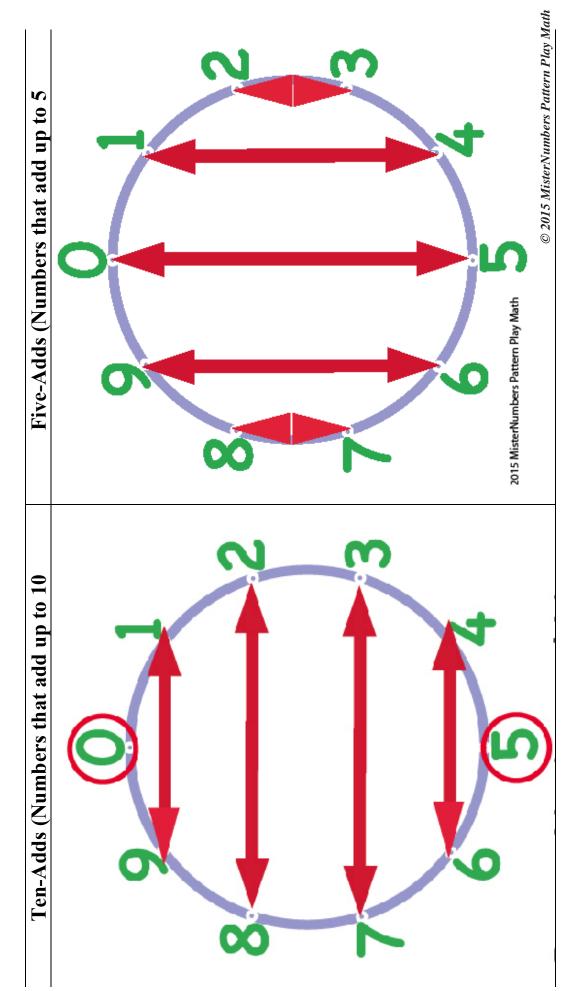
Plus or Minus 5 is VERY helpful Number Wheel for kids. © 2015 MisterNumbers Pattern Play Math

### Number Wheel Ten-Adds: Numbers that add up to TEN



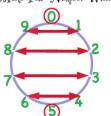
Create Horizontal Lines
Circled numbers too: 0 + 10 and 5 + 5

All Addition (Ones) is within 2 of the 5 and 10 Add Number Circles



### Ten Adds and Nine Adds

Make Ten" Number Wheel



### **Importance of students learning Ten Adds**

Our number system is ten base so Ten, and the numbers that add up to 10, are very important for kids when learning addition, subtraction and multiplication, They show up on the number wheel in cool ways that can help kids with basic addition. Start with the five at the bottom.

### **Cube Numbers and Ten Adds**

Another place that Ten Adds show happens when any number is cubed.

Numbers ending in:	Cube ends in:
0	0
1	1
2	8
3	7
4	4
5	5
6	6
7	3
8	2
9	9

Most cubes end in the same number as the Ones of the root number.

The four exceptions are 2, 3, 7, and 8. All of them end in the Ten Add of the original Ones digit.

### Learning Ten Adds on a Number Wheel

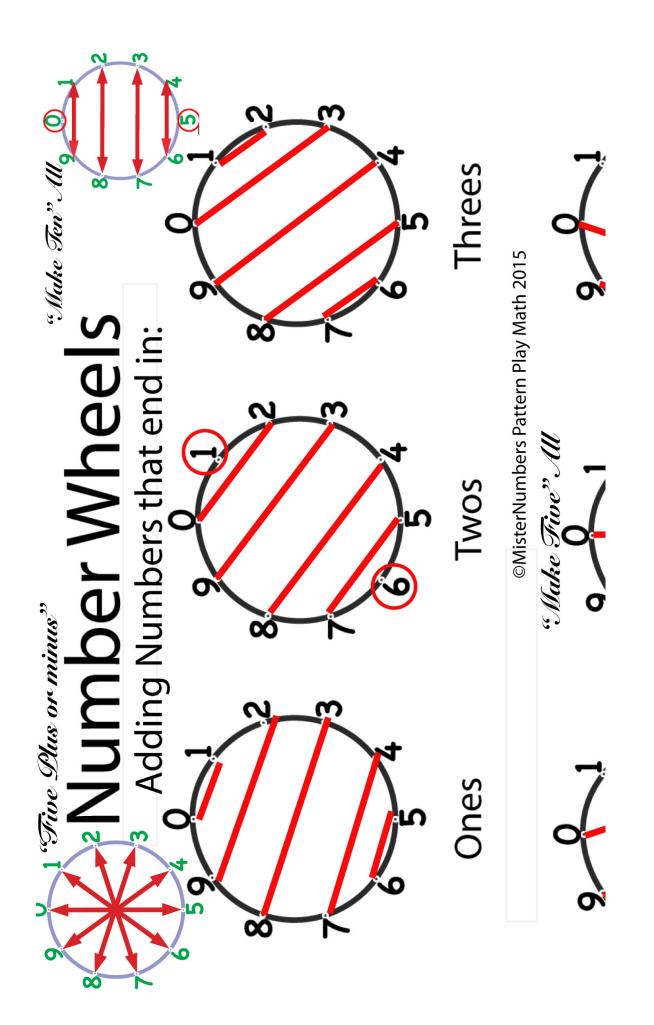
Start at the 5 at the bottom of the number wheel. It is all alone there. You can circle (and double an alone number. 5+5=10. We have 10 digits (fingers) and 10 digits (numbers) and our number system is ten based BECAUSE humans have 10 fingers.

To be more flexible, have five pennies in each hand. Again 5+5=10.

Now put one penny from the right hand into the left hand. We still have 10 pennies, but now 6+4=10. Now put another penny from the right hand into the left hand. We still have 10 pennies, but now 7+3=10. Now put another penny from the right hand into the left hand. We still have 10 pennies, but now 8+2=10. Now put another penny from the right hand into the left hand. We still have 10 pennies, but now 9+1=10. Now put the last penny from the right hand into the left hand. We still have 10 pennies, but now 10+0=10. On the number wheel horizontal parallel lines show us the Ten Adds.

### Nine Adds

Look at the Ten Adds on a number Wheel. Raise all the right side up one number to create Nine Adds. Again we have parallel lines and the numbers linked not only show all the numbers adding up to 9: 0-9, 1-8, 2-7, 3-6, 4-5, 5-4, 6-3, 7-2, 8-1, 9-0 as we go around, but they also are revealing the Nines times table: 9-18-27-36-45-54-63-72-81-90. See the Nines Add Wheel

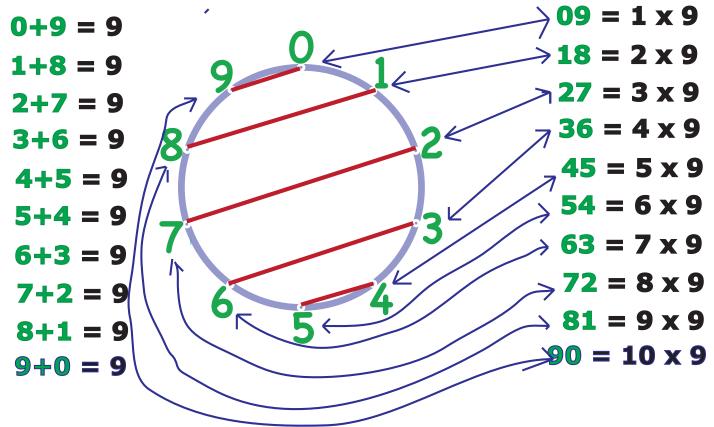


Make Nines Number Wheel

### Nine-Adds on a Number Wheel

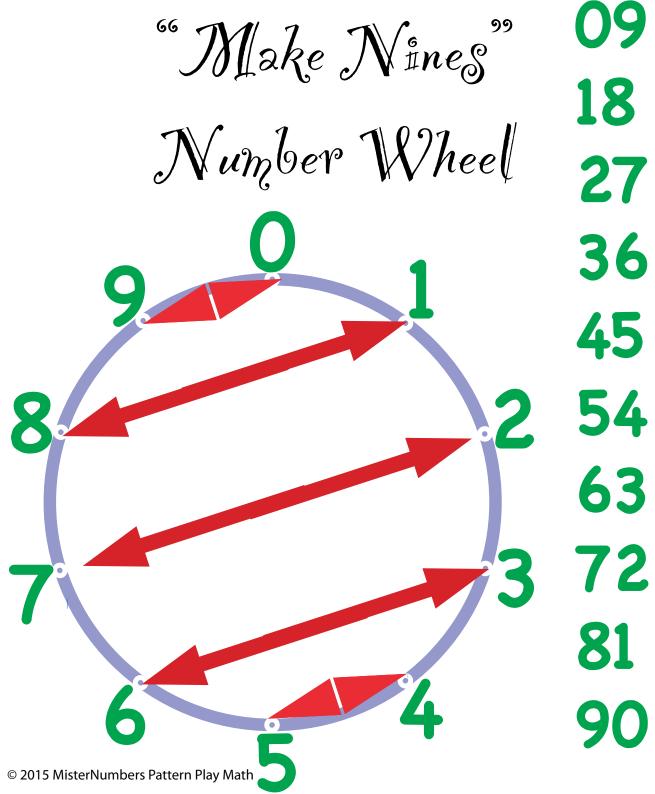
Playing with numbers that add up to Nine Close to Ten-Adds (down to left) create the Nines

©MisterNumbers 2014 PatternPlayMath.com

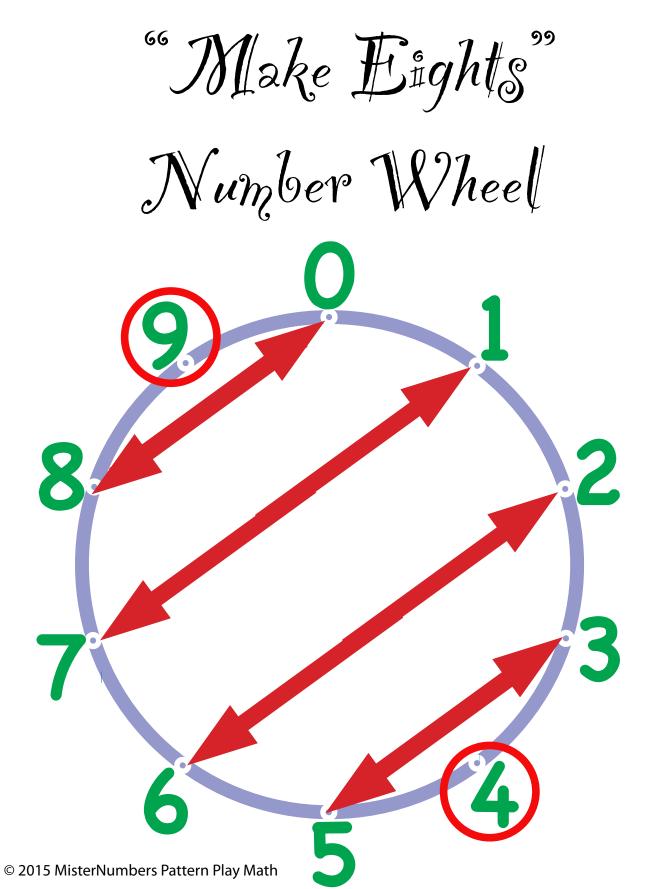


Go Around Clockwise from 0 to create the Nines Times Table Start at 0 and follow the line. Then at 1 and follow the line. Continue around the circle to create the NINES.

### Fill in the missing Nines below



Find Nines Times Table by going around from 0 on this Wheel

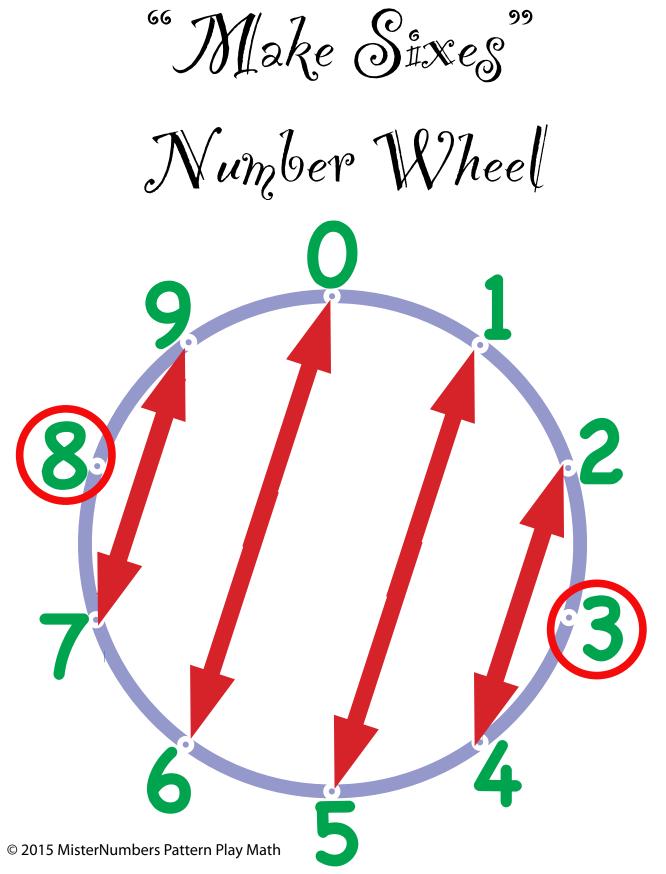


Add any of these two numbers and the sum will end in 8

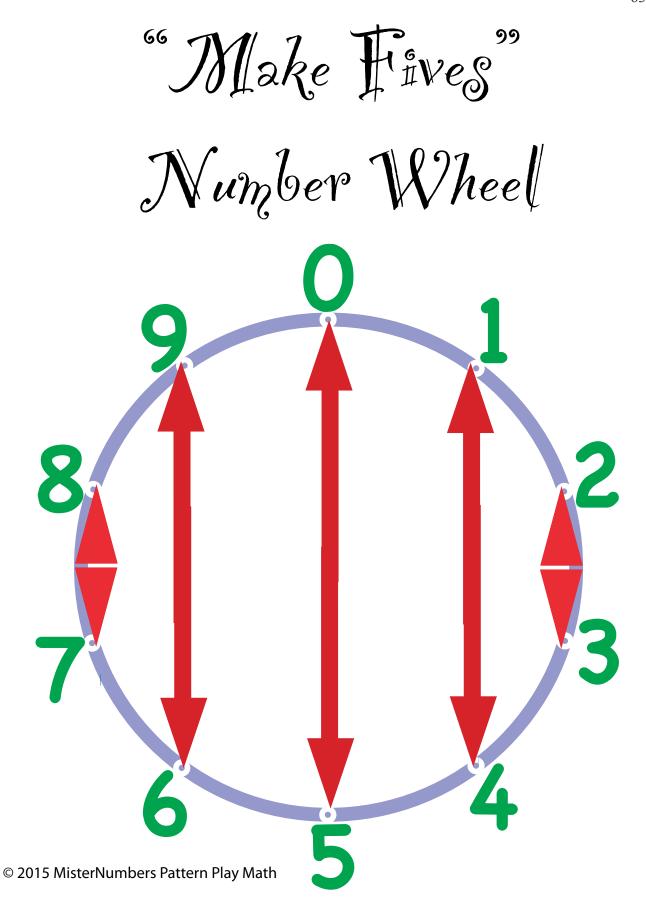
"Make Sevens" Number Wheel

Add any of these two numbers and the sum will end in 7

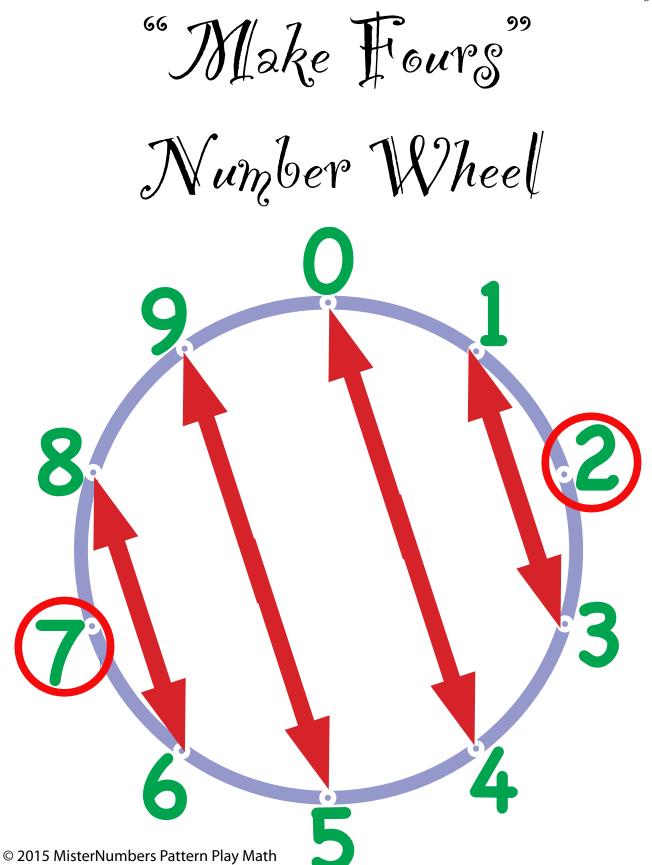
© 2015 MisterNumbers Pattern Play Math



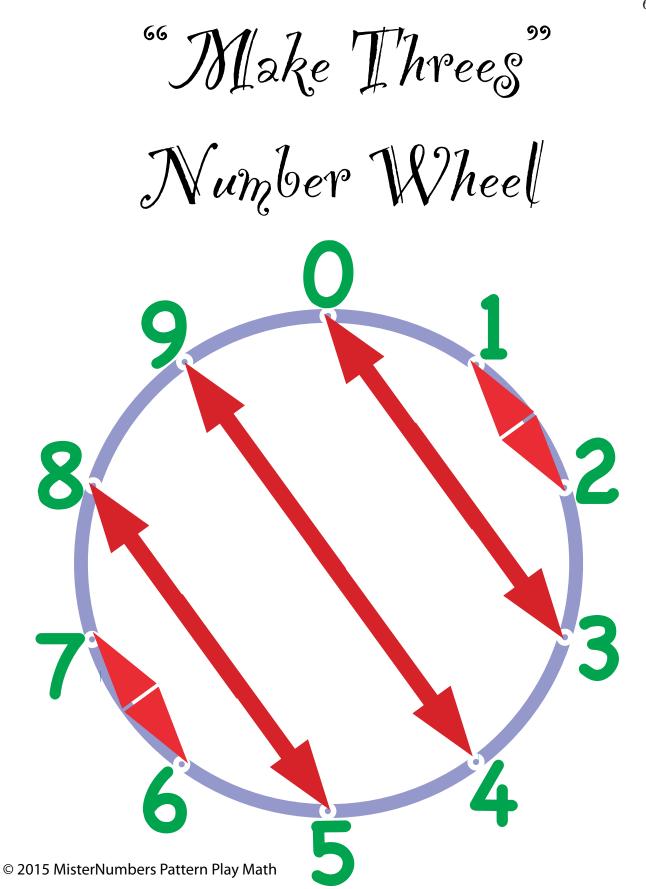
Add any of these two numbers and the sum will end in 4



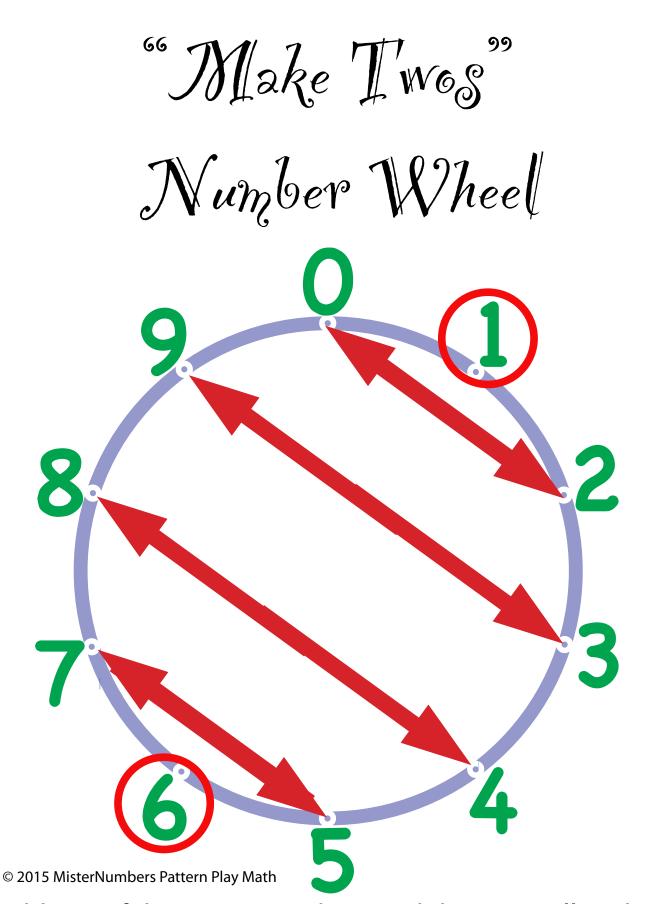
Add any of these two numbers and the sum will end in 5



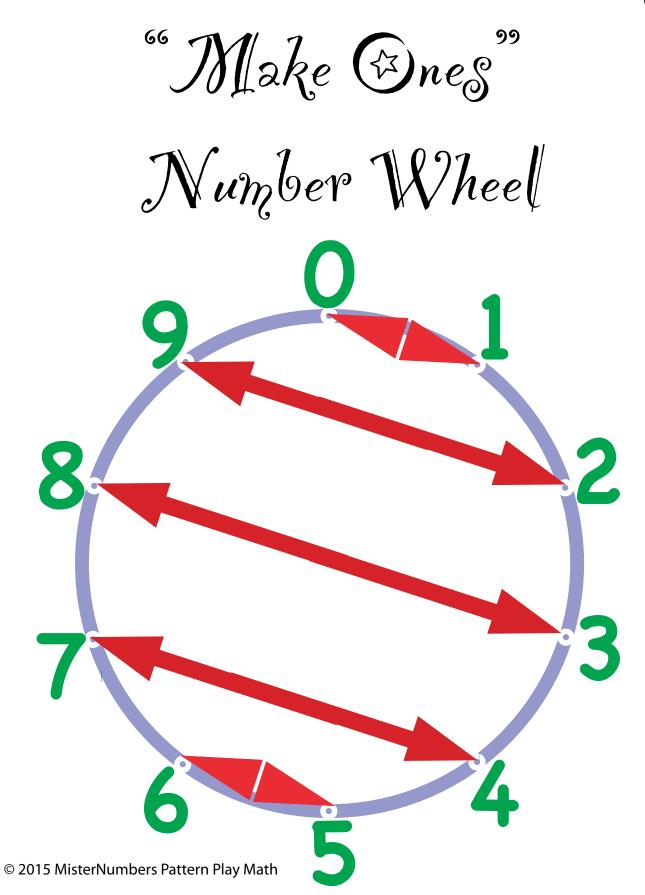
Add any of these two numbers and the sum will end in 4



Add any of these two numbers and the sum will end in 3

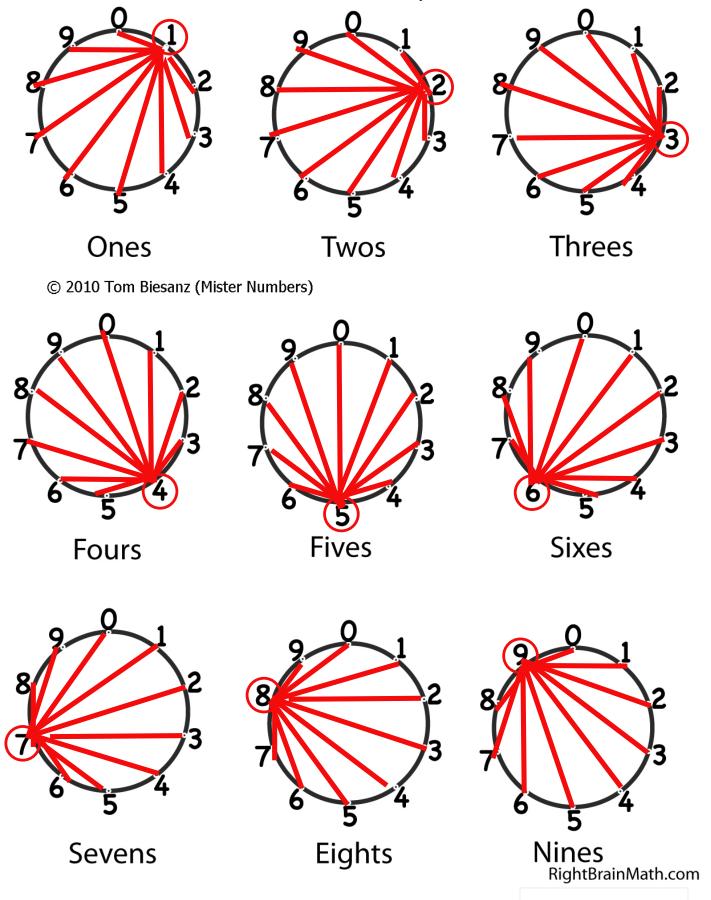


Add any of these two numbers and the sum will end in 2



Add any of these two numbers and the sum will end in 1

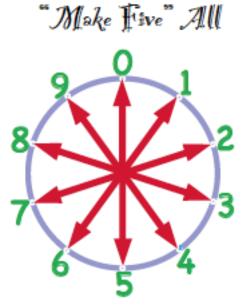
### Number Wheels for any Numbers



## "Plus or Minus 5" Number Wheels

### Plus or Minus 5 Number Wheel

See the Plus or Minus 5 Number Wheel.



Add Five to any number and it will take you across the wheel to the left to the answer, or to the right with a 1 in front.

Start at 0 and add 5. You go half way around the wheel to 5. Add another 5 and go half way around back to 10 (0). The number wheel only plays with the Ones and so 10 shows up as 0.

Again add 5 and go half way around (down to 5) to 15. Then back up to 20 (up to zero). This is like a yo-yo going up and down 5-10-15-20-25-30-35-40-45-50, and so forth.

We can also start at any number and subtract 5 by going half way around.

We can also add 5 from any other number. Start at 1 and add 5 (go half way around to 6). Add five again and go back to 1 (or 11). Add 5 again to go to 16. This is great fun because kids see it is just going back and forth from 1 to 6 to 1 to 6, whether you are adding or subtracting.

The same thing applies for 2 and 7, 3 and 8, and 4 and 9, and of course the reverse numbers.

Really fun.

© Pattern Play Math 2015

### Plus or Minus 5 is VERY helpful Number Wheel for kids.

Many kids end up counting on their fingers. When they play with these Number Wheels, they find it much quicker and easier..Look at any or all of the Plus or MinusAddition Number Circles. Let kids explore these number wheels. What do they see? What can they figure out? Let them own it!

Help for you or them if needed:

Start with 0 and add by fives: 5, 10, 15, 20, 25, 30, 35, 40, 45, 50. Almost all kids can do this easily and maybe even sing it with a "Here I come, Ready or Not"

But it works from any number.

P.s. they can go one more or one less than 5, to add 4 or 6 to any number. Just add or subtract 1. Or to add 3 or 7. Just add or subtract 2. Still easy.

A great tool is to go back to their fingers, but use them to jump 5 or subtract 5. Hold out both hands with fingers up. Turn one hand so both thumbs are on the left. Count from 1 to 10 starting from the left. Great.

Now notice that 1 and 6 are both thumbs

Wiggle each thumb as you count from 1 (left thumb) to 6 (right thumb) to 11 (left thumb) to 16 (right thumb).

Continue to 21 (left thumb) to 26 (right thumb) to 31 (left thumb) to 36 (right thumb). How high can you go?

Wiggle each thumb as you count from down from 36 (right thumb to 31 (left thumb) to 26 (right thumb)

Coninue to 21 (left thumb) to 16 (right thumb), to 11 (left thumb) to 6 (right thumb) to 1 (left thumb).

Now do it from 2, your pointer finger on your left hand, to 7, wiggle your pointer finger on your right hand.

Continue to 12 (wiggle left pointer) to 17 (wiggle right pointer) to 22 (wiggle left pointer) to 27 (wiggle left pointer).

Go as high as you like and then subtract Fives. To up or down five from any 2 or 7.

Now do it from 3, your long finger on your left hand, to 8, wiggle your long finger on your right hand. Continue to 13 (wiggle left long finger) to 18 (wiggle right long) to 22 (wiggle left long) to 27 (wiggle left long).

Go as high as you like and then subtract Fives. To up or down five from any 3 or 8.

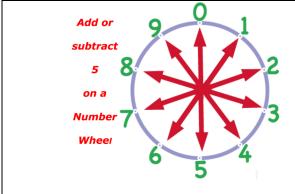
Now do it from 4, your ring on your left hand, to 9, wiggle your ring finger on your right hand. Continue to 14 (wiggle left ring finger) to 19 (wiggle right ring) to 24 (wiggle left ring) to 29 (wiggle left ring).

Go as high as you like and then subtract Fives. To up or down five from any 4 or 9.

Play with starting at 5 (your little finger). Easy, right? 5, 10, 15, 20, 25, 30, 35, 40, 45, 50

Play often with counting by fives on your fingers and see how easy it is. © 2015 MisterNumbers Pattern Play Math

### Handy Trick for Adding or Subtracting Five from any Number



See the Number Wheel for adding or subtracting five from any number. It is easy to add or subtract 5 from 0 and 5: 5-10-15-20-25-30-35-40-45-50. Going up and down is easy, but it can be easy to do it from any number using the Number Wheel and a Handy Trick.

Hold both hands in front of you with the thumbs left (see picture: looking at the palm of your left hand and the back of your right hand). If you start with your left thumb as 1 (wiggle it), then see your right thumb as 6 (wiggle your sixth finger). You have just added 5 to 1 and got 6. Now add another 5 and see that it takes you back to your left thumb at 11 and wiggle it (we are focusing on the Ones and the Tens are easy). Add another 5 to 11 and you are at your right thumb as 16. Add another 5, and of course you are back to your left thumb at 21. Go to 26, to 31, to 36, to 41, and see that 6 and 1 are across the number wheel and you can go half way around each time.



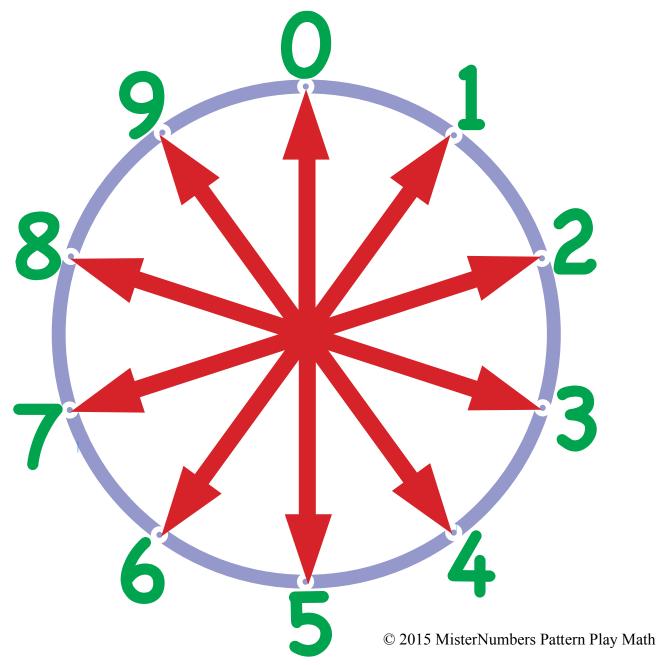
What is cool is that you can also subtract 5 using your hands and/or the wheel, because subtracting 5 also takes you exactly half way around the wheel. Let's start at 26 with our right thumb and subtract 5 and wiggle your left thumb at 21 (or go half way around the number wheel to 1).

Subtract 5 again from 21 and you are back to your right thumb at 16, then to 11 (left thumb) and 6 (right thumb) and subtract 5 to get to 1 on your left thumb. Look at your thumbs and see the jumps from 1 to 6 and to 1. Do this daily for two weeks and 1 and 6 are connected in your mind, and it will always be easy to add or subtract 5 from 1 or 6.

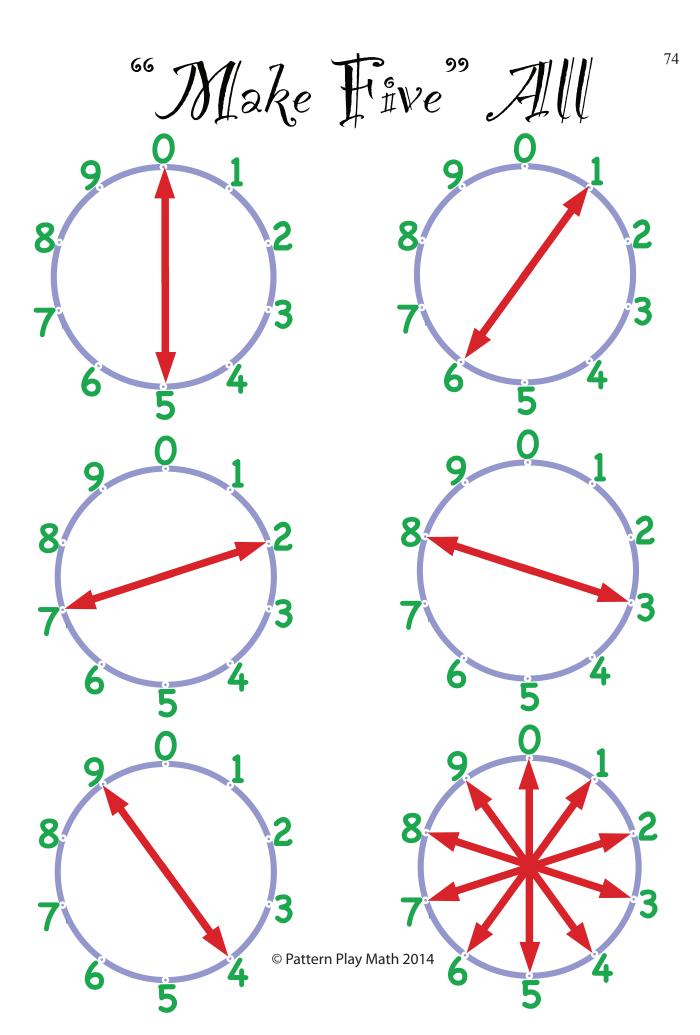
Repeat adding and subtracting 5 using your pointer fingers. Can you see that these are twos and sevens? Can you see that 2 and 7 are exactly half way around the Number Wheel? Look at your hands and count up and down from 2-7-12-17-22-27-32-37-42-47 and higher. Do this also daily for two weeks and 2 and 7 are connected in your mind, and it will always be easy to add or subtract 5 from 2 or 7.

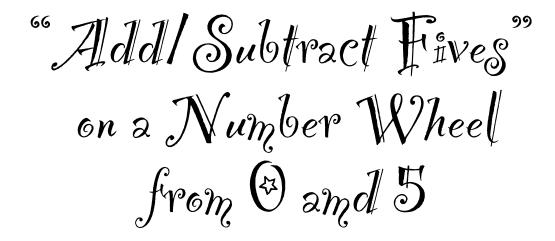
Repeat using the middle fingers for 3 and 8, and the ring fingers for 4 and 9.

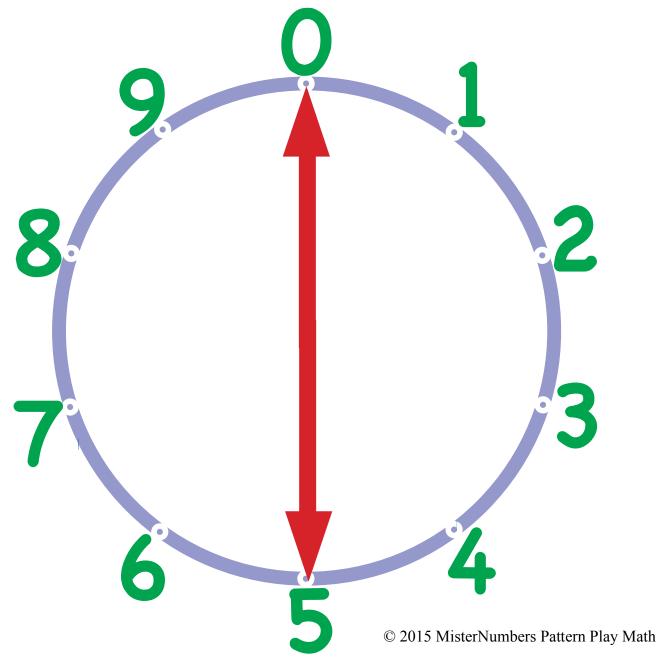
"Add/Subtract Fives" on a Number Wheel from any Number



Add or subtract 5 from any number: Follow the arrow

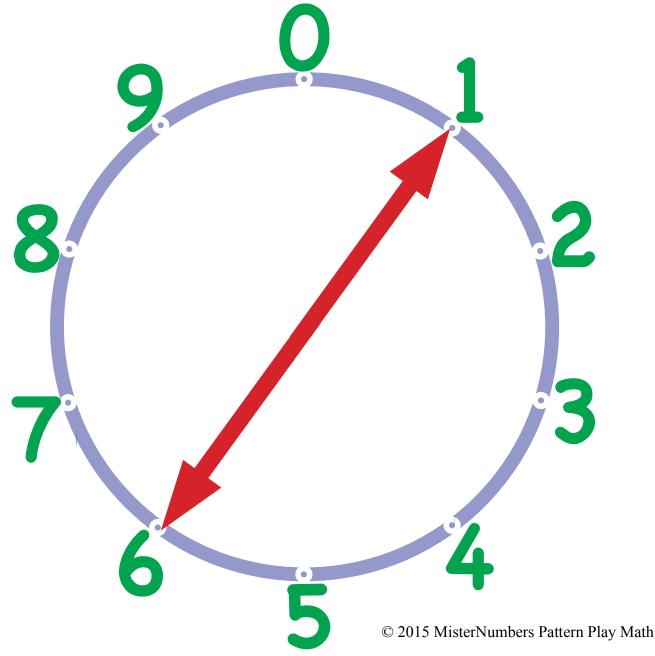






Add or subtract 5 from 0 and 5: Follow the arrow

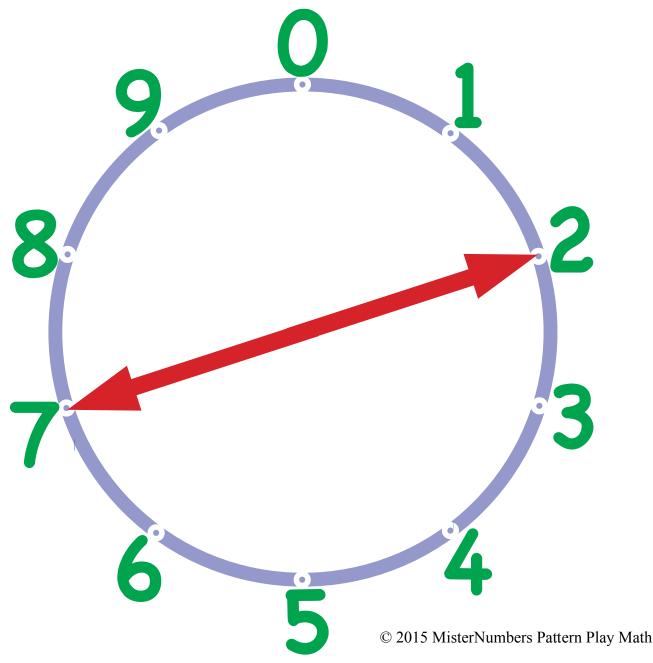
"Add/Subtract Fives" on a Number Wheel from I and G:



Add or subtract 1 and 6: Follow the arrow for last digit

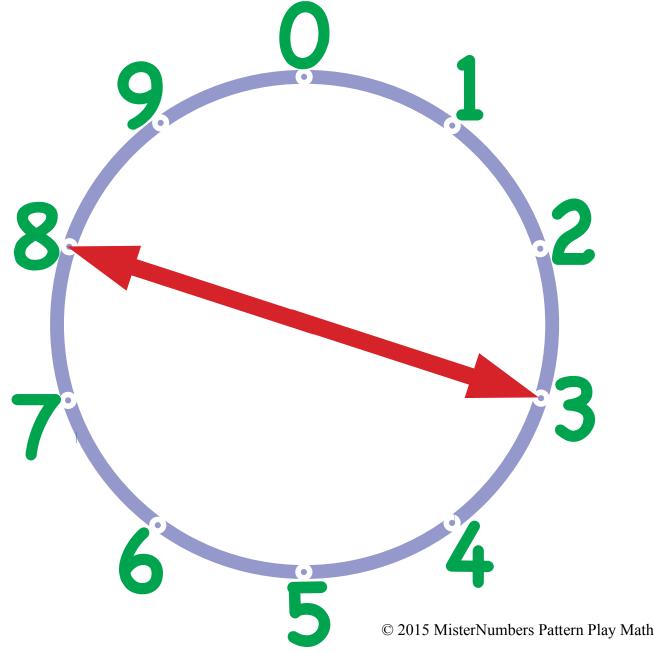
and Mumber Wheel

from 2 and 7



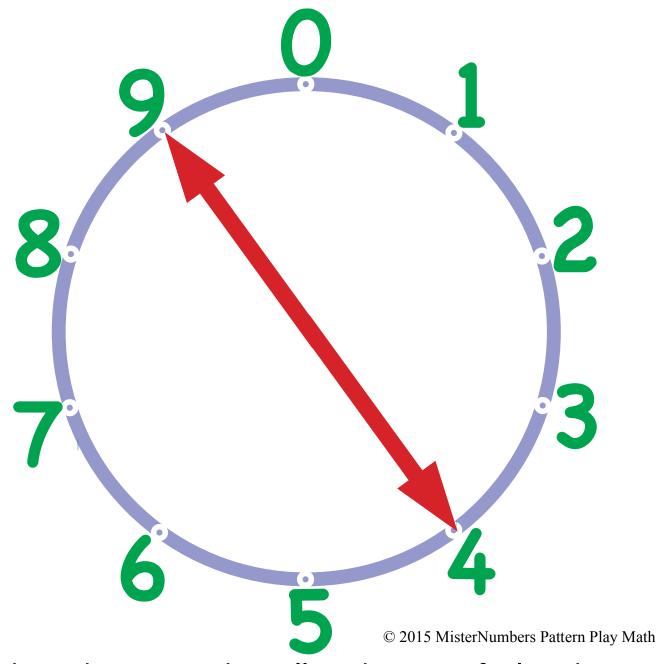
Add or subtract 2 and 7: Follow the arrow for last digit

"Add/Subtract Fives" on a Number Wheel from 3 and 8



Add or subtract 3 and 8: Follow the arrow for last digit

and Subtract Fives"
on a Number Wheel
from 4 and 9:



Add or subtract 4 and 9: Follow the arrow for last digit

Tic
Tac
Toe
Math

## **THREES**

Start with Tic-Tac-Toe lines.



Add the 123456789 pattern starting from lower left going up. These are ones-digits.

3	6	9
2	5	8
1	4	7

In the second row, add 1's in the Tensdigit place and 2's in the third row. You are creating the Threes (3x1 - 3x9).

<u>0</u> 3	<u>0</u> 6	<u>0</u> 9
<u>1</u> 2	<u>1</u> 5	<u>1</u> 8
<u>2</u> 1	<u>2</u> 4	<u>2</u> 7

3x10 = 30 Notice that this is the first box (3) with a 0 after it. The second will end in 60 (6) with a 0 after it. The 3rd set will end in 90, the 3<sup>rd</sup> number (9) with a 0 after it. The 4<sup>th</sup> will end in 120.

Repeat Tic-Tac-Toe lines and 123456789 pattern. Add 3's, 4's, and 5's in the next three rows, creating 3x11 - 3x19.

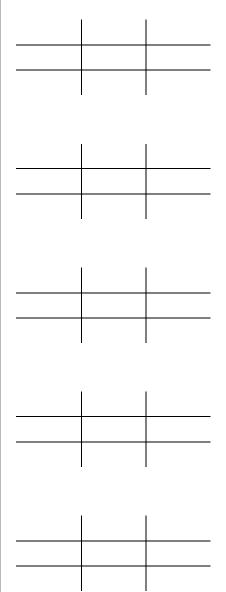
<u>3</u> 3	<u>3</u> 6	<u>3</u> 9
<u>4</u> 2	<u>4</u> 5	<u>4</u> 8
<u>5</u> 1	<u>5</u> 4	<u>5</u> 7
3x20 =	= 60	

Do lines and and123456789 pattern.

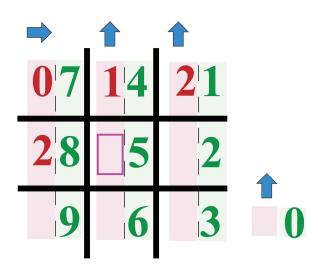
3	6	9
2	5	8
1	4	7

Copyright2008 Tom Biesanz

Continue creating the Threes as long as you like in this fun way. The next rows <sup>81</sup> will add 6,7, and 8 in front of the 1-9 and the next table will add 9, 10, and 11 in front.

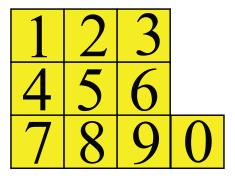


Buy EZ Times Table book on my website <a href="http://eztimestable.com">http://eztimestable.com</a> for \$9.95. It includes ways to do the Twos, Threes, Fours, Sixes, Eights, and Nines as well as a 1-page creation of the whole times table.



## 12 DIAL PADS TO PLAY ON FOR ALL NUMBERS

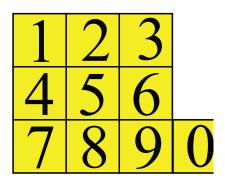
PatternPlayMath.com



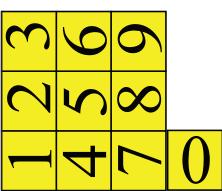
1	2	3	
4	5	6	
7	8	9	0

1		2	3	
4	-	5	6	
7	7	8	9	0

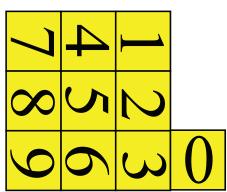
©MisterNumbers2014



**THREES** 

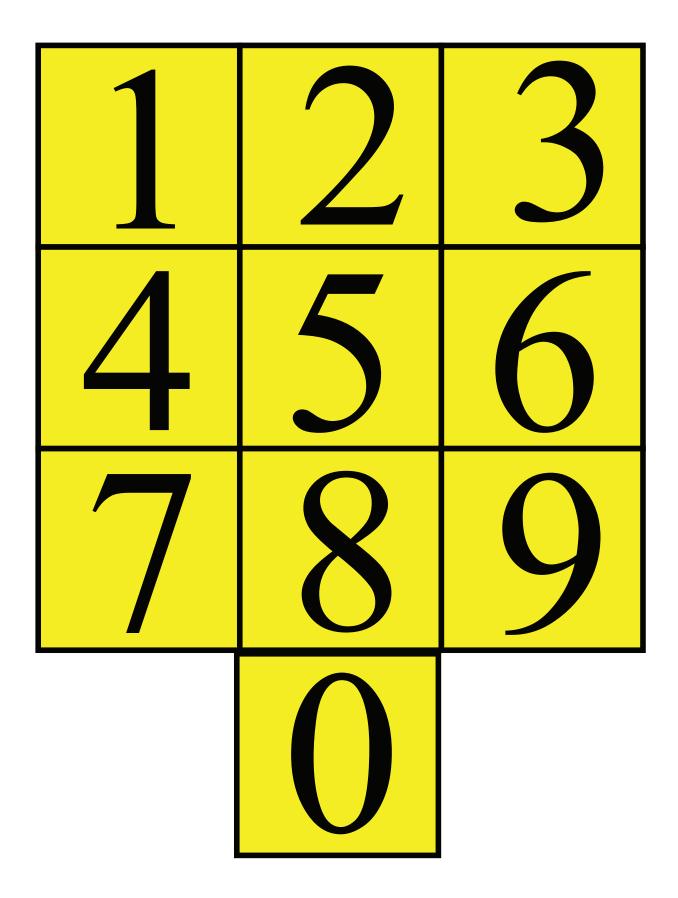


**SEVENS** 

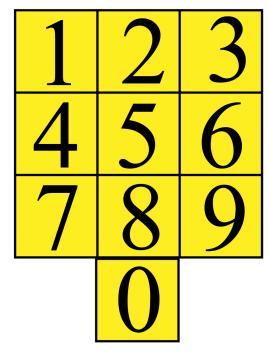


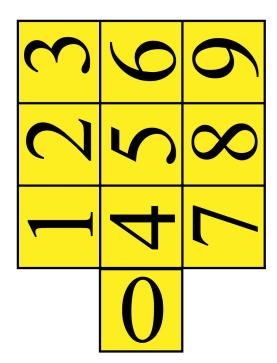
**NINES** 

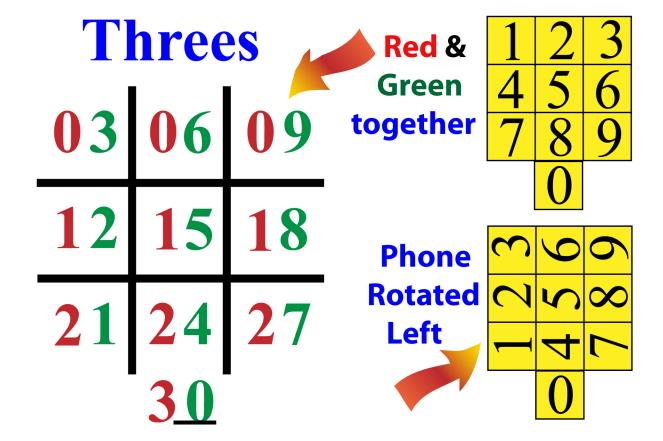
6	8	$\Gamma$	
9	5	7	
3	7	I	0



## Threes: Rotate Phone left







07       14       21         28       35       42         49       56       63	Here the Tensies are added to see how to complete the 7s times tables
4 6	9
3	nsies are a lete the 7s
07       14         28       35         49       56	Here the Te
	_
2 8	the numbers are flipped up for reading but all in the same place.
5	Here the numbers are flipped up for sier reading but all in the same plac
88	Here the nun Hasier reading
	ě
1 2 3	ight shows ble
4 5 6	Cell phone turned to right shows the 7s times table
7 8 9	Cell phone the

# EZ Times Table Worksheets

Grades K-4; Remedial 4-12

September 08 Issue (published by Federal News

Services, a division of PaperClip Communications, Inc.)

## Math Made Easy

SBN# 978-0-9799636-1-2). This new book is a revmake math fun! EZ Times Table by Thomas Biesanz available September 2008, Growth-ink Publishing The words "math" and "fun" don't often make the same sentence. But, in this case, a new book does math—a welcome resource in a time when U.S. nath scores are falling behind other countries. olutionary visual and auditory introduction to

While traditional math instruction relies mainly on

rote memory

work, EZ Times All they need to know is how to count to 10 and multiplication. that 2, 4, 6, 8, children with and 0 are the Table helps http://youtube.com/user/ MisterNumbers.

brain.

enjoy making the kindergarten age from there. Kids EZ Times Table as young as

Students generate Iwos, that makes sense to a child's on the Ones and numbers, based a structure for

on "Subscriber Spot" and

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Patterns: Wow!" handout from Curriculum Review website at: Just go to the website, click www.curriculumreview.com Threes and Seven from EZ Times Table on the blank copy of the Sub To find out more about the book, check out the "Creating the

MisterNumbers

on Youtube).

This right-brain approach presents instructions, addiwith playful graphics on the side. Employing the EZ each addition, subtraction, multiplication, division. Times Table, the book then shows how to use it to factors, squares, place value, prime numbers, and 8.5" x 11" table for each step, detailing the result tional information for parents/teachers, and a full

multiplication. The Tic-Tac-Toe square helps students create multiplication tables all the Find Out More About EZ Times Table way up to 20x20. Free instructional videos EZ Times Table uses pattern play to teach are available on Youtube by MisterNumbers at:

http://eztimestable.com/. You'll quickly see how passionate author Thomas Biesanz (aka MisterNumbers) is about math! A DVD is also available at

create a whole

times table

and they can

even numbers,

# Curriculum Review Magazine (established 1960)

## **Right Brain Math**

## A fun, visual approach to learning multiplication and division where kids play with patterns and make friends with numbers

by
Thomas Biesanz
a.k.a. MisterNumbers



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Art work by Jakob Marsh
http://EZTimesTable.com

EZ Times Table is patent pending.

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## All Instructions on one page

- 1. Put a big 1 above the left gray column. Going down the right side of the column, write the numbers 1, 2, 3, 4, 5, 6, 7 8, 9, 0, and repeat until you reach the bottom of the column.
- 2. Put a 1 in front of the first 0, a two in front of the second 0... Put 1's between the 1 and 2 on the left side, 2's between the 2 and 3, and 3 in front of the last 1 and 2. You have created the numbers 1-32. write the numbers 2, 4, 6, 8, 0, and repeat until you reach the bottom of the column.
- 3. Put a 1 in front of the first 0, a two in front of the second 0... Put 1's between the 1 and 2 on the left side, 2's between the 2 and 3..., and 6 in front of the last 2 and 4. You have created the numbers 2-64.
- 4. Put a big 3 above the column to the left of the Ones. Put a 3 in the same row as the 3 in the Ones column. Above the 3 you just put in the Threes column, there are two empty boxes. Place a dot in these boxes. Look at the pattern you have just created. (dot, dot, 3). Continue all the way down this column with this pattern of ● 3, ● 3...
- 5. Put a big 4 in the column to the right of the Twos. Put a 4 in the same row as the 4 in the Twos column. Above the 4 you just put in the Fours column, there is one empty box. Put a dot in that box. Notice that you have a pattern of a dot and then a 4. Continue this pattern all the way down the column: 4, 4, 4, 4, 4.
- 6. Put a big 6 above the column to the right of the Fours. In this column, put a 6 in the same row as the 6 in the Twos column. Above the 6 you just put in the Sixes column, there are two empty boxes. Put a dot in those boxes. Now in the Sixes column, you have two dots and a 6. This is your pattern. Continue it all the way down the column: 6, 6, 6, 6, 6...
- 7. Put a big 8 above the column to the right of the Sixes. Put an 8 in the same row as the 8 in the Twos column. Above the 8 you just put in the Eights column, there are three empty boxes. Put a dot in those boxes. Now in this Eights column, you have three dots and then an 8. Look at this new pattern. Continue it down to the bottom of the column: ● 8, ● 8, ● 8, ● 8...
- 8. Put a big 10 in the column to the right of the Eights. Here we will use a shortcut. On the left side, put the numbers 1-10. On the right side, put a 0 in each of the ten boxes. You have created the numbers 10-100.
- 9. Put a big 5 above the column to the left of the Threes. In the column to the left of the Threes, count down by 5's to 50 (5, 10, 15, 20, 25, 30, 35, 40, 45, 50).
- 10. Put a big 9 above the far left column. The Nines column has 10 rows divided by a dotted line. Write down the left side of the dotted line the numbers 0-9. In the same row as the 9 at the bottom, write a 0 on the right side of the dotted line. Write 0-9 going UP.
- 11. Put a big 7 above the column to the left of the Fives. In the seventh box down, write the number 49.
- 12. In the box in the bottom left corner of the EZ TIMES TABLE write "O X any number = O" or "Zero times any number equals zero."
- 13. To eliminate counting the numbers using dot patterns, place a little x1 in the corner of the first 3, a little x2 in the corner of the second 3, a little x3 in the corner of the third 3.... Repeat for the Fours, Sixes and Eights.

## EZ TIMES TABLE Odd Numbers Even Numbers Use the Ones column to multiply the Fixes, Sevens, Nines, and Tess. : EZ. Table copyright Thomas Biesarz www.ezimestable.com

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The Nines-A Table copyright©Thomas Biesarz www.ezimeslable.com

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The Sevens-49 Table copyright@Thomas Biesanz www.eztimeslable.com

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27	21	15	3 n	3	6	•	6 x1	•	30
36	28	20	•	4	8	4 2	•	8 n	40
45	35	25	•	5	10	•	•	•	50
54	42	30	3 2	6	12	4 23	6 ∞	•	60
63	49	35	•	7	14	•	•	•	70
72	56	40	•	8	16	4 24	•	8 12	80
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	6	P	•	19	3.8	•	•	•	
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			•	29	5.8	-	•	•	
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Complete EZ Table OThomas Biesanz 2007 www.extimestable.com

Zero X any mumber = 2ero

## **EASY TIMES**

## by Janet Jacobsen

If numbers make you feel numb and dumb, here is a way to make them fun.

Just take a look at the open chart and see the big "T", that's your start.

Now number down both sides of the "T".

On the left side write down 1, 2, 3,

4, 5, 6, 7, 8, 9, oh,
repeating again on down the row.

On the right side 2, 4, 6, 8, oh,

And repeat again on down you go.

Add one's and two's making teens and twenties.

It's as easy as counting copper pennies.

Odd numbers go across the left top "T" line. Write 1, 3, 5, 7, and then 9. Even numbers go across the right side again, 2, 4, 6, 8 and then 10.

Now you have a big numbered "T".

Once you add dots you'll have the key
to finding patterns that are fun and easy to see
and will help you learn the times table effortlessly.

# EZ TIMES TABLE Odd Numbers Even Numbers Use the Orne column to multiply Blank EZ Table copyright Thomas Biesanz http://ezimeslable.com

reality (half of a box). **Division** 

If a number (the dividend) is **divided by a number in a short column, the answer is in the Ones column** in the same row as the dividend. Let's divide 63 by 9. we would look in the Nines column for the "answer" since we are dividing by 9. We find 63 or the nearest lower number. It is in the seventh box in the nines column, so the answer is  $63 \div 9 = 7$ . It is also in the same row as the 7 in the Ones column. Students now understand that multiplication and division are opposites and that they can work either way with the Chart.

#### **SQUARES**

**Finding the first One, the second Two, the third Three**, the fourth Four, the fifth Five... adds a dimension to squares that creates interest and promotes understanding of what a square number is. Ones, Twos, Threes, etc. are capitalized because they are families where the individual numbers in each set are at home. The Fives include 5, 10, 15, 20, and **25, which is the fifth and square number of the Five family.** 

#### **FRACTIONS**

**Fractions are another way of seeing division with some multiplication thrown in.** Start with ¼ of 12. Since 12 is an even number, find 12 in the
Twos column. One fourth means that you are dividing by 4. Looking in the
Fours column next to the 12 in the Ones column, you see that the third 4 is
there. You can also divide the Ones column down to twelve in four equal parts
(three numbers each). **This adds another visual, right-brain dimension**.
¼ x 12 = 3. I like using ¼ because it is also called a quarter. For 2/4 (two
quarters) of 12, I hold up a real quarter and ask, "If one quarter (¼) is worth 3,
then two quarters are worth \_\_\_\_\_?" I hold up two quarters and the students see
that two quarters (each worth 3) are worth 6. "And three quarters are worth
\_\_\_\_\_?" They see that three quarters (each worth 3) are worth 9. Once the
principle is established, fractions are easy work.

#### **FACTORS**

Factors can easily be found for any number by finding the number on the EZTT. Looking to see what column they are in tells the student one factor of the number. Another can be found by looking in the Ones and Twos column in the same row. 24, next to 6x4 shows that 6 and 4 are factors of that number.

#### PLACE VALUE

Students have used Ones-digits and Tens-digits in patterns when they created the Ones, Twos, Nines and Tens. See **Ones-units on page 54**. Kids are just learning names for what they already are using.

#### PRIME NUMBERS

The *Times Line Table* (page 65) is a great overview to explore **prime numbers**. These are numbers that can only be divided by 1 and themselves. Accepting that 2, 3, 5, and 7 fit this definition, they are circled (they show up as factors of themselves). Go down the Ones column and see that 11 has only dots (no factor numbers) in that row. 13, 17, 19, 23, 29, 31, 37, 41, 43, & 47 also have only dots in their row. These numbers are also circled. Because they have no factors, they are prime numbers. The Table could be continued to 100 or more as a project to learn about factors and prime numbers using this right-brain overview. Could we find all prime numbers by continuing this chart?

### USING THE EZ TIMES TABLE WITH OTHER LEARNING METHODS

The EZ TIMES TABLE appeals to several learning strategies. It can stand alone as a method of teaching math, but it also is reinforced by combining it with other methods.

**Using it with flash cards can become a game** to find the answers in two different ways for each card. This increases confidence and locks in the actual multiplication facts as students learn their way around the Table.

The **EZTT works well with manipulatives** too. As you move each pair of blocks (or other manipulatives), go down one box in the Twos column with a finger or pencil. The Twos column will keep count of the total number of blocks and Ones column will keep track of the number of pairs.

Now double up the pairs and move the groups of four blocks down as groups. In the Fours column, point to the first 4 with this group, and then the second 4 with the second group of 4 blocks. Moving over to the Twos column shows that you have 8 blocks and the Ones column shows that this is your second group of 4 blocks. Moving the tenth group of four is done as you point to the tenth 4. This shows the student that he has moved 40 blocks (in the Twos column) and that this is his tenth group of four blocks (by counting the 4's or looking at the small x10 after that 4).

The same method works for the Threes, Sixes, and Eights. For the Fives, Sevens, Nines, and Tens, go down one box with each corresponding set of blocks moved.

The EZ Times Table also works well with counting rectangles on graph paper. On graph paper you can give added meanings to each of the families of Ones, Twos, Threes, Fours, etc. with rectangles one wide, two wide, three wide, etc. and then going to the **EZTT** to get totals for each row of squares.

#### WORKSHEET

The next two pages are a two sided worksheet that can be used to focus on using the Table while, or after creating the Table. It can also be used in a class for fast students who are waiting for their peers to finish a column.

ONES	TWOS	NAME		_ DATE_
8 x 1 =	6 x 2 =			
6 x 1 =	3 x 2 =	THREES	FOURS	SIXES
3 x 1 =	9 x 2 =	3 x 5 =	8 x 4 =	9 x 6
9 x 1 =	8 x 2 =	3 x B =	4 x 4 =	8 x 6 =
1 x 4 =	2 x 4 =	3 x 2 =	4 x 4 =	6 x 4 =
1 x 2 =	2 x 2 =	2 x 3 =	4 x 7 =	= 9 x 9
1 x 7 =	2 x 7 =	3 x 7 =	<b>4</b> x 1 =	6 x 7 =
1 x 1 =	2 x 1 =	3 x 9 =	4 x 2 =	6 x 1 =
6 + 2 =	2 x 18 =	3 x 1 =	6 x 4 =	6 x 8 =
7 + 4 =	2 x 23 =	1 x 3 =	3 x 4 =	6 x 3 =
14 + 3 =	14 / 2 =	4 x 3 =	9 x 4 =	3 x 6 =
15 + 6 =	18 / 2 =	3 x 6 =	7 x 4 =	<b>6 x</b> 2 =
12 + 3 + 4 =	26 / 2 =	8 x 3 =	5 x 4 =	7 x 6 =
22 + 5 + 2 =	30 / 2 =	9 x 3 =	2 x 4 =	5 x 6 =

EIGHTS	TENS	FIVES	NINES	SEVENS
8 x 5 =	10 x 5 =	8 x 5 =	$= 6 \times 6$	9 x 7 =
= 8 × 8	10 x 8 =	5 x 5 =	8 x 9 =	8 x 7 =
8 x 2 =	10 x 2 =	5 x 8 =	9 x 4 =	7 x 4 =
2 x 8 =	2 x 10 =	5 x 7 =	= 6 x 6	7 x 7 =
8 x 7 =	10 x 7 =	5 x 1 =	9 x 7 =	7 x 7 =
= 6 x 8	$10 \times 9 =$	<b>5 x</b> 2 =	$9 \times 1 =$	7 x 1 =
8 x 1 =	10 x 1 =	= <b>2</b> X 9	= 8 x 6	7 x 2 =
1 x 8 =	1 x 10 =	3 x 5 =	9 x 3 =	7 x 3 =
4 x 8 =	4 x 10 =	9 x 5 =	3 x 9 =	3 x 7 =
5 x 8 =	10 x 3 =	2 x 6 =	5 x 9 =	<b>6 x 7</b> =
8 x 3 =	10 x 6 =	5 x 3 =	7 x 9 =	7 x 5 =
<b>6 x 8</b> =	10 x 4 =	7 X 5 =	4 x 9 =	7 x 8 =
8 x 4 =	8 x 10 =	<b>4 x</b> 5 =	= 6 x 9	7 x 6 =
3 x 8 =	6 x 10 =	9 x 5 =	2 x 9 =	5 x 7 =

# PLAYING WITH THE EZ TIMES TABLE

**Any multiplication** workbook or page of **problems can be used with the Chart**. The following page starts with one digit multiplication. Copy this for your class or use your own. The students have created the times table and they are amazed that all the answers to one-digit multiplication are in this simple Table. It is very important to use the **EZTT** with many problems until they understand that all multiplication facts are here and they start thinking in the families of the Threes, Sixes, Eights, etc.

There is even a pattern way to learn a 20 X 20 times table in the back of the book. Students will have to learn a traditional or lattice technique to multiply 2 digit or larger numbers. They are learning to use it quickly and to double-check their answers by reversing the problems (6 X 8 gives the same result as 8 X 6). Finding the same answer in two different ways on a chart that they made is very satisfying for many students.

There is a huge amount of information on this Table and it is useful for students to look at similarities, patterns, and go back and forth between addition and multiplication with the Table. They can visually see where the same numbers have more than one factor (24 has half of the numbers 1-10 as factors: 1, 3, 4, 6, and 8).

For 6 X 5=30, the student can count down 6 Fives, or go down the Ones column to 6 and then over to the Fives column. They have found the answer 30 in two ways. This also **reinforces that multiplication is just adding the same number over and over again.** 

**Numbers start making more sense to the student.** Four 4's and two 8's both add up to 16. They can **SEE** number relationships. They trust the **TREES of the Ones and Twos column** to know that their answers are correct. They can visually see the answers. These TREES of the Ones and Twos can help them learn the multiplication tables by heart because it is not blind memory. The numbers make sense and relate to each other. Studying the numbers with the Table that they created **helps them own the numbers**.

The following **worksheet** gives students an opportunity to expand the use of the EZ Times Table.

2 X 3 =	34	Half of 26 is
6 x 2 =	<u>x 2</u>	Half of 50 is
3 x 4 =		Half of \$88 is
4 x 5 =		Double 4 is
5 x 6 =	23 <u>x 3</u>	Double 7 is
6 x 7 =		Double 8 is
7 x 8 =	35	Double 16 is
8 x 9 =	<u>x 4</u>	Double 25 cents
9 x 9 =		
9 x 7 =	68	½ of 26 is
8 x 6 =	<u>x 5</u>	½ of \$38 is
7 x 5 =		½ of \$55 is
6 x 4 =		1/4 of 20 is
5 x 3 =	44 <u>x 62</u>	<sup>3</sup> / <sub>4</sub> of 20 is
8 x 4 =		1/9 of 36 is
7 x 3 =		2/9 of 36 is
	73 <u>X 96</u>	3/9 of 36 is
6 X 9 =	<u> </u>	1/3 of 27 is
26 / 2 =		3 3's are
24 / 6 =		4 4's are
32 / 8 =	853 <u>x 421</u>	5 x 5 is
35 / 5 =		6 squared is
63 / 9 =		7 squared is
18 / 4 =		-
21 / 3 =		8 <sup>2</sup> is
49 / 7 =		9 <sup>2</sup> is

## Using EZ Times Table in a Home or in the Classroom

**The EZTT can be used many ways with a single student or a class-room.** To introduce it to a group of students, I recommend use of an overhead projector. **Make a transparency of the blank EZTT** and talk the class through it as you create your own Table on the transparency. Some students often quickly get excited by seeing and creating the patterns. This becomes an incentive for other students to join in the fun. I recommend grouping students who start going ahead ("All students who have finished the Threes already should come over here and do these problems").

Another approach is eliminating the small  $x_1$ ,  $x_2$ ,  $x_3$ ,  $x_4$ , etc. for the whole class and then giving it to the faster students to fill in. Leaving it out makes the Table easier and clearer for some students, and it is still fully functional. The students just need to count down the numbers in the pattern to multiply and divide (for example, look at 24, find the 6 in the same row, and count down to find that it is the 4th 6 in the Sixes column).

A third addition for fast students is to have them convert their **EZTT** to an **EZ Facts Table** by changing the patterns to the multiplication facts (found in the Ones and Twos columns). The second 6 is erased and replaced with a 12 (which is in the same row in the Twos column). The third 6 is replaced by 18 (in the same row in the Twos column), etc. Have these students replace all patterns with numbers from the same row in the Twos column for the Threes, Fours, Sixes, and Eights columns or give them the **EZ Fill-in Facts** Table.

Students can use their own **EZTT** to work on their math problems for addition, subtraction, multiplication and division for their daily work. Students have chosen to laminate their **EZTT** because it was so valuable to them. They have made their own calculator!

The students could re-create the EZTT once a week. If they use graph paper, they start seeing that they are creating the whole times table "from scratch", which they can do for standarized tests. Even just re-creating the Nines or Sevens in a few seconds on the side of a paper can eliminate errors and build trust.

I highly recommend **Teach Your Child the Multiplication Tables: Fast, Fun & Easy with Dazzling Patterns, Grids & Tricks!** by Eugenia Francis who has created great worksheets that focus on patterns. Please send me ideas and suggestions that I can pass on to other teachers.

#### Lesson Plan for EZ Times Table

#### **Lesson Plan: EZ Times Table**

Combine Goals, Objectives, and Activities that are appropriate for your students. Some of the 3rd, 4th, and 5th grade activities are found in the advanced Part 3.

Time varies: usually .5 hour for each table (20 tables)

**Subject: Math** 

#### **Goals:** (Use these California Standards or from your own state)

#### **1**<sup>st</sup> Grade California Standards

- 1.0 Students understand and use numbers up to 100.
- 2.0 Students demonstrate the meaning of addition and subtraction and use these operations to solve problems.

#### **2<sup>ND</sup> Grade California Standards**

- 1.0 Students model, represent, and interpret number relationships to create and solve problems involving addition and subtraction.
- 3.0 Students model and solve simple problems involving multiplication and division:

#### 3rd Grade California Standards

- 2.0 Students calculate and solve problems involving addition, subtraction, multiplication, and division:
- 2.3 Use the inverse relationship of multiplication and division to compute and check results.
- 2.6 Understand the special properties of 0 and 1 in multiplication and division.

#### 4th Grade California Standards

- 2.0 Students use two-dimensional coordinate grids to represent points and graph lines and simple figures.
- 3.0 Students solve problems involving addition, subtraction, multiplication, and division of whole numbers and understand the relationships among the operations.
- 4.0 Students know how to factor small whole numbers.

#### **5th Grade California Standards**

- 2.0 Students perform calculations and solve problems involving addition, subtraction, and simple multiplication and division of fractions and decimals.
- 2.0 Students use strategies, skills and concepts in finding solutions.
- 3.0 Students move beyond a particular problem by generalizing to other situations.

#### **Objectives** 1st GRADE: Student will be able to

- 1.1 ...count, read, and write whole numbers to 100. ... create the Twos from patterns to 64 and beyond.
- 1.3 ...represent equivalent forms of the same number through the use of physical models, diagrams, and number expressions (to 20) (e.g., 8 may be represented as 4 + 4, 5 + 3, 2 + 2 + 2 + 2, 10 2, 11 3).
- ... half or double any number to 32 and beyond.
- ... add any three numbers from 1-10 in any order resulting in the same answer.
- ... subtract a smaller number from any number up to 32.

#### **2<sup>ND</sup> GRADE:** Student will be able to:

- ...use repeated addition, arrays, counting by multiples to do multiplying
- ...Use the commutative and associative rules to simplify mental calculations and to check results.
- ...Recognize and describe patterns & determine a next term in linear patterns.

Solve problems involving simple number patterns.

#### 3rd GRADE: Student will be able to:

- ... Recognize and use the commutative and associative properties of multiplication (e.g., if  $5 \times 7 = 35$ , then what is  $7 \times 5$ ?, if  $5 \times 7 \times 3 = 105$ , then what is  $7 \times 3 \times 5$ ?).
- ...Use the inverse relationship of multiplication and division to compute and check results.
- ... Understand the special properties of 0 and 1 in multiplication and division.
- ... Select appropriate operational and relational symbols to make an expression true (e.g., 4 \_\_\_ 3 = 12, what operation symbol goes in the blank?).
- Use a variety of methods, such as words, numbers, symbols, charts, graphs, tables, diagrams, and models, to explain mathematical reasoning.

#### 4<sup>th</sup> GRADE: Student will be able to:

- ... Understand that many whole numbers break down in different ways (e.g.,  $12 = 4 \times 3 = 2 \times 6 = 2 \times 2 \times 3$ ).
- ...Know that numbers such as 2, 3, 5, 7, and 11 do not have any factors except 1 and themselves and that such numbers are called prime numbers.
- ...Draw the points corresponding to linear relationships on graph paper.
- ...Use a variety of methods, such as words, numbers, symbols, charts, graphs, tables, diagrams, and models, to explain mathematical reasoning.

#### 5<sup>th</sup> GRADE: Student will be able to:

- 1.4... Determine the prime factors of all numbers through 50.
- 1.1... Use information taken from a graph or equation to answer questions about a problem situation.
- 2.3... Use a variety of methods, such as words, numbers, symbols, charts, graphs, tables, and models, to explain mathematical reasoning.

#### **Activities**

You may go in sequence or choose whatever the student or class is ready to learn.

#### Kindergarden

p.8: Create the Ones Number line.

#### First Grade, EZ Times Table

- p.11: Do addition problems, adding two or more numbers.
- p. 11: Do subtraction problems with EZTT.
- p.12: Create the 2's. Count by 2's, Double a number, Multiply by 2.
- p. 14 Learn to Divide by 2, to find half of a number.

#### Second Grade, Ez Times Table

- p. 4-40 Create the EZ Times Table.
- p. 68: Create the Color EZTT.
- p. 37: Add multiples of 1-10 (preparation for multiplication).

#### Third Grade, EZ Times Table

- p. 43: Multiplication with EZTT.
- p. 60: Create EZ Facts Table. Use EZ Facts to memorize multiplication table.
  - p. 45: Find and understand factors on the EZTT.
- p. 55: Threes and Sevens patterns. Fun! See MisterNumbers on Youtube.
  - P. 58: Twos, Fours, Sixes, Eights patterns.
  - p. 44: Division on the EZTT.
  - p. 45: Learn Square Numbers on the EZTT.
  - p. 74: Create a Ruler EZTT
  - p. 4-40: Create the EZTT on graph paper.

#### Fourth Grade, EZTT

- p. 56: Learn Rule of Tens.
- p. 70: Create 10 X 10 and 10 X 20 Multiplication Table
- p. 64: Create Time Line Table.
- P. 64: Find factors on Time Line Table.

#### Fourth & Fifth Grade, EZTT

- p. 72: Create a 20 X 20 Multiplication Table.
- p. 66: Create the Slope Line Table.
- p. 66: Anchor slope lines in Graphing with slope line table.
- p. 64: Find Prime Numbers on Times Line Table.
- P. 72 : Create a 30 x 30 Table on graph paper.

#### Fun Patterns with the Ones-digits and Tens-digits Feel free to skip this page. Come back if you want to understand ones-digits.

What are **Ones-digits?** We have already worked with the Ones-digits when we created the Ones, Twos, Nines and Tens columns in the EZTT. They are the numbers to the right of the dotted line, in the Ones place. The **Tens-digits** are the digits in the tens place, the number to the left of the dotted line in these four columns. See below. We will use the Ones-digits and Tens-digits for **more pattern play starting on the next page.** 

Note that on the last row of the Tens, the tens-digits reach 10 at 100, we could add another dotted line on the left and have 1 in the hundreds-digits.

The **ONES-DIGITS** are circled below. In the EZTT, we started the Ones and Twos with a pattern in the ones-digits.

The **TENS-DIGITS** are circled below. In the EZTT, we started the Nines and Tens with patterns in the tens-digits.

6 4 0 :6 8:1 10 0 

:6

The Ones-digits are on the right side of the dotted line in these four columns from the EZTT. We ended making the Nines with a 0-9 pattern going up and the Tens with zeros. See pages 8, 12, 26, and 32 for making the ones-digits in these columns.

:8 1:16 1:8 1:0 2:0 2.4 3.0 3:2 3.4 3:6 4:0 4:2 4:6

4:8

5:0

3 0

The Tens-digits are on the left side of the dotted line in these four columns from the EZTT. See pages 12, 14, 26 and 30 for making the tens-digits in these columns.

#### **Creating the Threes and Sevens from Patterns: WOW!**

#### The Threes

Make a Tic-Tac-Toe Square.

Add the 1-2-3-4-5-6-7-8-9-0 pattern starting from lower left going up. These are ones-digits.

	3 2 1	6		9
	2	5	П	8
$\neg$	1	4	П	7
		0		

Add 1's in the Tensdigit place in the second row, and 2's in the third row. You are creating the Threes (3x1-3x9).

03	06	<u>0</u> 9	
12	15	18	
21	24	27	
3x10 = 30			

Repeat Tic-Tac-Toe square & 123456789 pattern. Add 3's, 4's, and 5's in each of the next three rows, creating  $3x11 - 3 \times 19$ .

<u>3</u> 3	<u>3</u> 6	<u>3</u> 9
<u>4</u> 2	<u>4</u> 5	<u>4</u> 8
<u>5</u> 1	<u>5</u> 4	<u>5</u> 7
3x20 = 60		

Repeat Tic-Tac-Toe square & 123456789 pattern. Add 6's, 7's, and 8's in each of the next three rows, creating 3x21 - 3 x 29.

<u>6</u> 3	<u>6</u> 6	<u>6</u> 9	
<u>7</u> 2	<u>7</u> 5	<u>7</u> 8	
<u>8</u> 1	<u>8</u> 4	<u>8</u> 7	
3x30 = 90			

Notice that each Ticac-Toe square ends with 30, 60, 90, 120, 150...These are threes (3, 6, 9, 12, 15...) with a 0 after it.

Continue creating the
Threes as long as you
like in this fim way.

See MisterNumbers on Youtube for a video.

3	6	9		
2	5	8		
1	4	7		
3x40 = 120				

3	6	9		
2	5	8		
1	4	7		
3x50 = 150				

#### The Sevens

Make a Tic-Tac-Toe Square.

Add the 1-2-3-4-5-6-7-8-9-0 pattern starting from upper right and going down. This is the same, but opposite pattern as 3's.

As you go across, add 1 to the tens-digit in 2<sup>nd</sup> & 3<sup>nd</sup> columns (X's). You are creating the Sevens (7x1 – 7x9).

Add 70 as the 10<sup>th</sup> 7. Repeat Tic-Tac-Toe square & 123456789 pattern. Continue to add 1 to the tens-digit in 2<sup>th</sup> & 3<sup>th</sup> columns (X's) as you go across

Repeat Tic-Tac-Toe lines and 123456789 pattern.

Notice that each Ticac-Toe square ends with 70, 140, 210, 280, 350...These are sevens (7, 14, 21, 28, 35...) with a 0 after it

Continue creating the Sevens as long as you like or start over in the last three Squares.

Notice on both Threes and Severe squares that all opposite digits add up to 10: 7+3, 4+6, 1+9, & 2+8.

7 4 1 1 8 5 2 9 6 3 V

	. Х	X	
<u>0</u> 7	<u>1</u> 4	<u>2</u> 1	
28	35	42	
49	56	63	
7x10 = 70			

	X	X	
77	84	91	
98	105	112	
119	126	133	
7x20 = 140			

	X	X		
7	4	1		
8	5	2		
9	6	3		
7x30 = 210				

	X	X	
7	4	1	
8	5	2	
9	6	3	
$7\pi A \Omega = 72\Omega$			

	X	X		
7	4	1		
8	5	2		
9	6	3		
7x50 = 350				

#### "RULE OF TENS" PATTERNS

My Rule of Tens states that all columns adding up to ten have reversed patterns in the ones-digits. Looking just at the ones-digits give us a great place to explore patterns in numbers. You just learned used two of them in the Threes and Sevens page. If you understand ones-digits, feel free to TURN THE PAGE NOW AND CONTINUE TO HAVE FUN with the Twos, Fours, Sixes, Eights, and creating a 20 X 20 EZ Table from patterns. When you want to know more about HOW it works, read this page.

We know that the ones-digit (Could Ones-ie be a simpler name?) holds the ones place, the last digit in a whole number. In the Ones, Twos, Nines and Tens columns, we saw that it is the number to the right of the dotted line, and the **tens-digit** (Tens-ie?) is the digit in the tens place, the number to the left of the dotted line.

All multiplication table ones-digits fall into just 6 patterns (some are reversed). This gets more interesting when one of the patterns is made up only of Zeros in the Zero and Tens columns. The Fives end with alternating 5's and 0's, and suddenly we are down to only four patterns in the ones-digits. All patterns start and end with 0. We can leave the starting or ending Zero off to see the reverse pattern clearer.

In the EZ Table, we created the ones-digits for both the **Ones and Nines** and they (1 and 9) add up to ten, so let us look at the Rule of Tens. We made the ones-digits for the Ones column with a repeating **0-1-2-3-4-5-6-7-8-9-0**. We created the second half of the Nines with the same pattern. We reversed them by starting at the bottom. So reading **down** the right side of the Nines column is the reverse **0-9-8-7-6-5-4-3-2-1-0**. Look at the 10 x 20 EZ Table on page **74** (where we separate all the ones-digits with a dotted line for 20 rows) for confirmation that the pattern repeats. This is the **third pattern**.

We created the ones-digits for the **Twos** with a repeating **0-2-4-6-8-0** on the right side of the dotted line. By my Rule of Ten, the **Eights** should have the opposite pattern. If we look at the 10 x 20 EZ Table again, we see that, indeed, the Eights pattern is **0-8-6-4-2-0**. This is the **fourth pattern**, which is really a 5-digit pattern when we leave off one of the zeros.

By the Rule of Tens, The Fours and Sixes columns should have reversed patterns. We can look at the EZ Facts Table (page 57) to confirm that the

ones-digit repeating pattern for the Fours is **4-8-2-6-0** and the Sixes pattern is the opposite, **6-2-8-4-0** (leaving the starting zeros off gives us the 5 repeating numbers). This is the **fifth pattern**.

Our **sixth and last pattern** is in the **Threes** and, by the rule of Tens, the **Sevens** columns (3 + 7 = 10). Looking at the EZ facts Table or the 10 x 20 EZ Table we can see that the patterns for the Threes is 3-6-9-2-5-8-1-4-7-0 and the Sevens have the reverse pattern of 7-4-1-8-5-2-6-3-1-0. We have seen in the Threes and Sevens page this easy way to visualize these patterns in sets of Three on a **Tic-tac-Toe square**, with the zero below. Threes add 3 to 3, 2, 1 while the Sevens subtract 3 from 7, 8, 9.

Threes: 3-6-9, 2-5-8, 1-4-7, 0

	/ -	
3	6	9
2	5	8
1	4	7

0

Sevens: 7-4-1, 8-5-2, 9-6-3, 0

7	4	1		
8	5	2		
9	6	3		
Ö				

The Six patterns and their opposites in the Ones-digits All patterns start and end in Zero, the starting zero has been left off.

Cosumn	Repeating Pattern & Reverse	Also shows up in larger Table
For Zeros	0-0	Tens, Twenties,
For Fives	5-0	Fifteens, Twentyfives,
For Ones	1-2-3-4-5 <del>-6-</del> 7-8-9-0	Elevens, Twenty-ones,
For Nines	9-8-7-6-5-4-3-2-1-0 (neverse)	Nineteens, Twenty-nines,
For Twos	2-4-6-8-0	Twelves, Twenty-twos,
For Eights	8-6-4-2-0 (reverse of Twas)	Eighteens, Twenty-eights,
For Fours	4-8-2-6-0	Fourteens, Twenty-fours,
For Sixes	6-2-8-4-0 (reverse of Fours)	Sixteens, Twenty-sixes,
For Threes	3- <del>6-9</del> -2-5 <del>-8</del> -1-4-7-0	Thirteens, Twenty-Threes,
For Sevens	7-4-1-8-5-2-9-6-3-0 (reverse)	Seventeens, Twenty-sevens,

If we look at the 20 x 20 EZ Table on page 72, we see that the patterns in the ones-digits are the same for 1 and 11, 2 and 12, 3 and 13, 4 and 14, 5 and 15... If we make the Table even wider, we will see that all numbers ending in 1 will repeat the 1-2-3-4-5-6-7-8-9-0 pattern, all numbers ending in 2 will repeat the 2-4-6-8-0 pattern, all numbers ending in 4 will repeat the 4-8-2-6-0 pattern, numbers ending in 5 will repeat the 5-0 pattern, and so forth.

You will now use these patterns to create the Twos, Fours, Sixes, and Eights, and you can use these patterns in Part 3 to create several multiplication tables.

#### Patterns for the Twos, Fours, Sixes and Eights

We will create these times tables from patterns in groups of 5 repeating numbers in 5 columns. The Twos and Eights, as well as the Fours and Sixes, have the same but opposite sequence in the first four numbers of the Ones-digits and end in 0. If a ones-digit in a box below is less than the one to its left, it has an X above it. Since it is less, we increase the Tens-digit by one (We are "carrying" a ten when we pass 0). Once we establish where the X's are, we can fill in the tens-digits. The left tables show the pattern, then adds the tens-digits. The right column is for you.

The Twos repeating pattern in the ones-digits is 24680. Only 0 is less than the number to its left (8) and has an X above it. So at 0, the tens-digit always increases by 1. On the left table we add a 1 in front of the first 0. Continue with 1's in the second row until the 0 gets a 2. We are creating the Twos with this pattern. Continue to create the Twos on the right table.

Create the Two pattern X					
2	4	6	8	0	
2	_4	_6	_ 8	٦	
2	4	6	8	0	
Ad	d the	tens d	ligits	X	
2	_4	_6		10	
12	14	16	18	20	
22	24	<u>26</u>	<u>28</u>	<u>3</u> 0	

Create your own Twos X				
_2	4	6	8	_0
2	4	6	8	0
2	4	6	8	0
_2	4	_6	_8	-
2	4	6	8	0
2	4	6	8	0
_2	_4	6	8	_0

The Eights repeating pattern is the apposite (putting the zero last): **86420**. The 6, 4, 2, and 0 are decreasing and get an X above their columns. This means that their tens-digits increase by one. So in each row, we add 1 under each X to make multiplication by 8. The 0 column makes 8 x5, x10, x15... Multiplying by 8 the EZ way!

	I	X	I	X
8	6	4	2	0
8	6	4	2	0
8	6	4	2	0
	<b>144</b> ()	le tens	digit	5
	x	x	x	X
8	<u>1</u> 6	<u> 2</u> 4	<u>32</u>	40
48	<u>5</u> 6	<u>6</u> 4	72	80
88	96	<u>10</u> 4	112	<u>12</u> 0

Create the Eights Pattern

Create your own Eights					
	X	X	X	X	
8	6	4	2	0	•
8	6	4	2	0	•
8	6	4	2	0	•
8	6	4	2	0	•
	_6	_4	_2	_0	•
8	6	4	2	0	•
8	6	4	2	0	•
	_6	_4	_2	0	•

The Fours repeating pattern is 48260. The 2 and 0 are getting smaller and get an X above their columns. This means that their tens-digits increase by one. In the first row, we add 1 & 2 under the X's to create 4,8,12,16,& 20. Say aloud the rhythm of the tens-digits:22334, 44556, \_

4	- 6		•	v		
4	8	2	6	0		
4	8	2	6	0		
	Add the tens-digits					
		X		X		
4	8	12	16	20		
24	28	<u>3</u> 2	<u>3</u> 6	40		

Create the Sixes Pattern

Create the Fours Pattern.

·	(6) If	your (	<b>JWE 4</b>	3
		X		X
4	8	2	6	•
_4	8	_2	_6	_0
4	8	2	6	•
4	8	2	6	0
_4	8	_2	_6	0
4	8	2	6	0
4	8	2	6	0
4	8	2	6	0
_				_

The Sixes repeating pattern is 62840, opposite of the Fours. The 2, 4, and 0 are getting smaller and get an X above their columns. This means that their tens-digits increase by one. In the first row, we add 1's under the X's to create 6 x 5 = 30. The next rows end in 60 & 90. Isn't this fun and amazing? See MisterNumbers on Youtube.

	X	X	X	
6	2	8	4	0
_6	_2	8	_4	_0
6	2	8	4	0
Į	<b>144</b> (1	ie ten:	s-digit: X	5
	X		x	X
6	12	18	24	<u>_3</u> 0
<u>36</u>	<u>4</u> 2	<u>48</u>	<u>5</u> 4	60
66	72	78	84	90

					_				
Create your own 6's X X									
6	2	8	4		D-				
6	2	8	4		Ð				
6	2	8	4		Ð				
6	2	8	4		D.				
6	2	8	4	$\Box$	D.				
6 	_2	<b>8</b>	4		D				
6	2	8	4	_	D.				
6	2	8	4		D				
	6 6 6 6 6	6 2 6 2 6 2 6 2 6 2 6 2 6 2 6 2	X       6     2     8       6     2     8       6     2     8       6     2     8       6     2     8       6     2     8       6     2     8       6     2     8       6     2     8	X     X       6     2     8     4       6     2     8     4       6     2     8     4       6     2     8     4       6     2     8     4       6     2     8     4       6     2     8     4       6     2     8     4	X X X 5 5 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 2 8 4 6 6 6 2 8 4 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6				

#### **PART 3:**

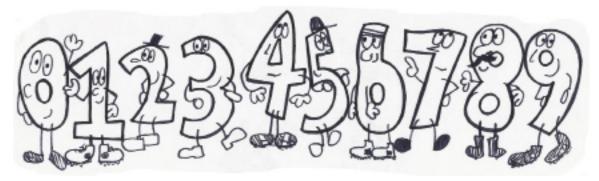
#### ADVANCED EZ TABLES

The first advanced table is the *EZ Facts Table*, which is helpful to almost all students.

We have created most of the times table in two ways. First we created the EZ Times Table and then we created the Threes, Sevens, Twos, Fours, Sixes and Eights from patterns. Now we can create a  $20 \times 20$  times table purely from patterns. Those who play here often feel that numbers are fun and friendly.

$\mathbf{E}$	Z	ΤI	[ <b>M</b>	Έ	S	T	<b>1</b> B	L	E
		Odd	Numbers	4	_	Even Nur	mbers		
9	7	5	3	1	2	4	6	8	10
0.9	7	5	•	1	2	•	•	•	10
18	14	10	•	2	4	4 21	•	•	20
27	21	15	3 n	3	6	•	6 x1	•	30
36	28	20	•	4	8	8 2	•	8 x1	4 0
4.5	35	25	•	5	1.0	•	•	•	50
5.4	42	30	6 z	6	12	12 🗷	12 x2	•	60
63	49	35	•	7	14	•	•	•	70
72	56	40	•	8	16	16 24	•	16 ∞	8 0
8:1	63	45	9 23	9	1.8	•	18 **	•	90
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	ure the nun		•	1:3	2.6	•	•	•	
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	re ine i multiply to		•	1:9	3.8	•	•	•	
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	oo a factor		•	28	56		•	56 ₽	
			•	2 9	58	•	•	•	
			30 x10	3.0	6.0		60 x11	•	
			•	3 1	62	•	•	•	
			•	3 2	6:4		•	64 ∞	
Zero X a	ny munber	= 2810	EZ Facts	Table copyr	igH2009 <b>©</b>	Forn Biesan	z Numbers	REZ <b>Ø</b> eol.o	DMI

#### **EZ FILL-IN FACTS Table**



Students who have created an EZ Times Table can form the **Facts Table** on the previous page. One way is to erase the 3's in the Threes column, replacing them with numbers from the Ones column. They can create the Fours, Sixes, and Eights in the same manner by erasing and filling in the numbers from the Twos column.

**The table on the right** is an exercise for students who understand the EZ Times Table to quickly **create the FACTS Table** on the previous page. Creating the Fill-In Facts chart allows them to keep their original **EZTT** that they value and create the Facts Table too. The need for erasing on the EZTT is eliminated. Fun and neat.

They now have the sets of the Ones, Twos, Threes, Fours, Fives, Sixes, Seven, Eights, Nines, and Tens. Each is still in the structure of the EZ Times Table and the relationship to the Ones and Twos are still evident. Now they can easily memorize the facts from a chart that they made. Creating this chart makes it easier to move up or down one or two boxes to figure out any facts they are unsure of. **They have the structure of each set of numbers.** 

They have accepted the Ones and Twos as accurate and the dot patterns are already in place in the Threes, Fours, Sixes, and Eights columns. Even the little " $x_1, x_2,...$ " are in place in the openings in the dot pattern on the table on the right.

The student creates the Threes by going down to each open box in the pattern, seeing the number in the same row of the Ones, and putting in that number in the Ones column. So the first open box (cell) in the Threes column (. . \_) is a 3. At the next open box, the student puts a 6 since it is in the same row of the Ones. The third box is a 9, and down they go to 30. They have now created the set of the Threes.

They also create the Fours (4, 8, 12, 16,...), Sixes (6, 12, 18, 24, ...) and Eights (8, 16, 24, 32...) in a similar manner by pulling numbers from the Twos column. They have created the sets of the Fours, Sixes and Eights. This allows them to see each of these sets separate, but connected to the Ones and Twos.

They again re-create the Tens, Fives, Nines, and Tens similar to the EZ Times Table. Notice that one **factor** for each number found on the Table is the column that contains it. The other factor is the little number next to the x, or it is the number in the Ones column. For example, we find 18 in the Sixes Column and it has a x3 behind it which means that 6 and 3 are factors. 15 is in the Fives column in the same row as 3 in the Ones column and so 5 and 3 are factors.

$\mathbf{E}$	Z	ΤI	M	$\mathbf{E}$	S	$\mathbf{T}$	A E	3 L	$\mathbf{E}$
		Odd	Numbers	4	_	Even Nur	nbers		1
9	7	5	3	1	2	4	6	8	10
			•	1	2	•	•	•	
			•	2	4	21	•	•	
			<b>z</b> 1	3	6	•	xi	•	
			•	4	8	12	•	πi	
			•	5	10	•	•	•	
			2	6	12	13	22	•	
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<u> </u>			23	9	18	•	23	•	
			•	1.0	2.0	25	•	•	
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			•	1.7	3 4	•	•	•	
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			17	2 1	42	•	<b>x</b> 7	•	
			•	2 2	44		•	•	
			•	2 3	4.6	•	•	•	
			28	24	4.8		五	16	
			•	2:5	5:0	•	•	•	
			•	2:6	52		•	•	
			19	2.7	54	•	19	•	
			•	2.8	56		•	17	
			•	29	5.8	•	•	•	
			<b>71</b> 0	3:0	6.0		Til	•	
			•	3 1	62	•	•	•	
			•	3 2	64		•	161	

Zero X any mumber = zero Fill in EZ Table copyright XID8©Tom Biesanz Numbers REZ Quot com

# VARIATIONS OF THE EZ TIMES TABLES

**The EZ Times Table (EZTT)** that the student has already created contains the whole multiplication table. They are hooked. There is nothing weird or scary about it. They count by Ones and Twos, count up to three, and do their Fives. Everything else falls into place in a way that they totally understand. Viewing the Table in different forms can facilitate fun understanding and learning math the easy way. A **Color EZ Times Table** can be created using different colors for each number.

#### THE TIMES LINE TABLE

The *Times Line Table* on the right uses the dots pattern from the **EZTT**. The Ones and Twos columns increase to 50 rows and are still the anchors of the table. The main difference is that 5, 7, 9, and 10 are also done as dot patterns. A student sees that Fives can also be dot, dot, dot, dot, 5, and similar patterns can be created for the Sevens, Nines and Tens. **The numbers arrange themselves in angle line patterns.** The lines of these patterns are drawn on this table and we can see that the first lines are all multiplication-times-one problems for the even and the odd numbers.

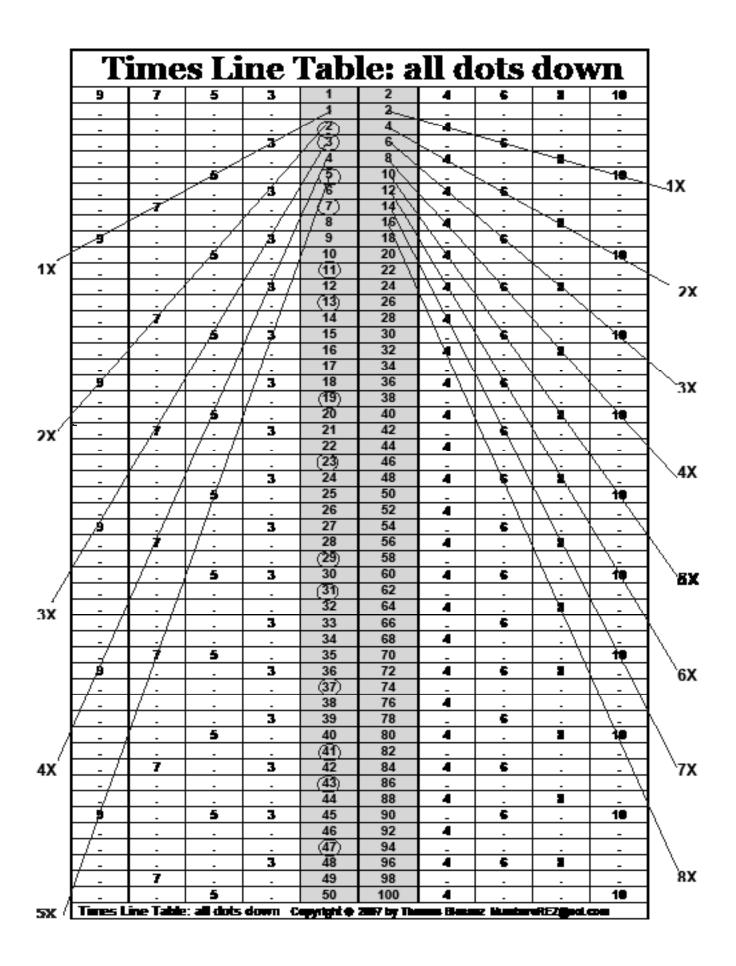
The first 9 is in the same row in the Nines column as it is in the Ones column, and the 3, 5, and 7 that are in the same line are also repeated in the Ones column. In the 2X line on the even side, the second 10 is in the same row as the 20 in the Twos column (10 X 2= 20). Look at the 4X (multiplication-by-4) line on the left and find the 7. Looking in the same row in the Ones column, we find the answer, 28. **Similar results are found for every number on a line.** Students can accurately guess that **all whole numbers are on lines if the chart is long enough.** 

**Prime numbers show up on this chart** (see page 44). Numbers outside the Ones and Twos column indicate **factors** in the same row. The numbers without factors (only dots) in their rows are circled and are **prime numbers**. We could continue the chart and have students **find more prime numbers**.

This table can be created by students on graph paper for a "Wow" learning experience. Use large square graph paper and use ten squares width, or for more rows, use small square graph paper and use two square width for each column.

#### VARIATIONS ON THE FOLLOWING PAGES

This is followed in the next pages by the **Slope Lines Table** which is very similar with an amazing twist for graph charts, **Patterns create an EZ 20 x 20 Table** and an **EZ Ruler Table** making the times table on a blank sheet.



#### MORE VARIATIONS ON THE NEXT PAGES

The **Times Line Table** is followed in the next pages by the **Slope Lines Table** which is very similar with an amazing twist for graph charts, Patterns creating an **EZ 20 x 20 Table**, and **an EZ Ruler Table** that creates the times table on a blank sheet.

#### THE SLOPE LINE TABLE

The **Slope Line Table** on the right is fascinating to many students when they see the patterns that the numbers create. It is identical to the *Times Line Table* except the numbers start at the bottom and the boxes are square. The first line at the bottom is the One times line. (One times the number is the same number). The second line is the 2X line  $(2 \times 4 = 8, 2 \times 6 = 12...)$ . The third and fourth lines are the 3x and 4x lines (3 or 4 times the number is found in the Twos column). This is similar to the *Times Line* table.

What is amazing is that the **One-times-line (1x)**, looking at the table as a graph, is also **the slope line y=1x**. The Two times line (2x) is the slope line y=2X. This gives students similar results for y=3x, y= 4x... Students now have a memory anchor for the angle of different slope lines.

Now students can look at a y=1x slope line and see a practical form that it takes that is real to them, that they created. They can remember that as the value of X gets larger, the slope line gets sharper, just as you multiply by a larger number, the number increases.

#### THE COLOR EZ TIMES TABLE

A fun color Table can be created with different colors for each number. This gives a nice graphic picture of how the different numbers relate. Making the **EZTT** in color is a **right-brain way** for students to help the number families come alive and make the Table visually appealing. This can be expanded to the EZ Facts table, adding colors for factors of the number.

#### THE IMPORTANCE OF PATTERN RECOGNITION

**Kids notice patterns with all the Tables,** like the Threes and Sixes are in the same rows, and that every other 4 is an 8, and that the Eights end with a repeated 8, 6, 4, 2, 0 pattern. Students love the dot patterns and these patterns include numbers, and soon the numbers are easier. An older friend told me he was recruited to do early computer programming based, not on math ability, but on pattern recognition. The variations of the EZ Times Table all teach pattern recognition. Right-brain creative insights and learnings in life and in school are based on noticing patterns and seeing relationships.

5	Slo	p	e l	_īr	ıe:	<b>s</b> 7	Га	ble	е	All-Dots, going up
			-	3	9				-	***************************************
	7		-	*	<b>4</b>	4	-	•	-	Y = 4 X
•	•	•	3	77	54		6		-	
			-	3	22	4			-	] /
,		5	-	25	9				10	] /
•	•	•	3	24	4	4	6	٠	-	] /
	•	•	-	23	4	٠		٠	-	/ Y = 8 X
	•	٠	-	72	#	4		•	-	Y /
	7	٠	3	<b>Z</b> 1	æ		6	٠	-/	] /
	•	5	-	20	4	4		٠	79	] /
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9	7	5	3	1	2	4	6	8	10	

Slope Line Table copyright 2007 Thomas Biesanz

#### NUMBER PATTERNS 10 x 10

From this page to the end of the book **is extra** for those students who enjoy seeing and playing with the patterns. In the top table on the next page, all ten columns are divided by dotted lines like the Ones, Twos, Nines and Tens were in the EZTT. These four columns are copied here and the numbers for the Threes, Fours, Sixes, and Eights are found in the **EZTT** or in the **EZFT** (EZ Facts Table). They are placed here with the dotted lines separating the the **ones-digits** (the single number to the right) and the **tens-digits**.

A learning progression is to have students create the **EZTT** with verbal instructions and use of an overhead projector, then create the **EZTT** on their own, then create the **EZ Facts Table**, and then this **EZ 10 x 10 Table**. Each step helps the student see the fun patterns while learning the multiplication facts. **This results in a form of the EZTT that is similar in some ways to a standard times table**, but we have established patterns that we can continue to play with to see how full of fun patterns numbers can be.

#### NUMBER PATTERNS 10 x 20

The lower table is identical to the upper table, but is extended down to 20 rows. The Ones and Twos are already done past 20 rows in the **EZTT** and can be transferred to the empty table. The Ones can be put in the left column of the Tens and finished by putting zeros in the ones-digit column.

**The ones-digits**: Look at the EZTT and see that the ones-digit patterns repeat for every number (except that 3, 7 and 9 have ended in 0 and are ready to repeat). The dotted lines again divide each column into ones and tens columns. Repeat ones-digit patterns in all right columns for 2-9 all the way down the chart. Since 3, 7, and 9 ended in 0, they start over with 3, 7, and 9 in the 11<sup>th</sup> row and repeat their respective patterns from the **EZTT**.

The Tens digits: We already have the first ten rows for 3-9 in this chart from EZTT. To do the next tens-digit in 3-9, look at the number above on the ones-digit side. If the new ones digit number is larger, repeat the previous number on the left. If it is smaller, increase the number by one. For example, after 30 (tenth row of the Threes), the pattern indicates a shift from 0 to 3 in the ones-digit. Since the 3 is larger than the 0, the tens-digit remains the same: 33 (11<sup>th</sup> row). After 39 the ones digit pattern indicates a shift from 9 to 3. Since the 3 is smaller, the tens increase to 4, resulting in 42). Using this pattern works for all columns.

Look at how it works on the EZ Pattern 10 x 20 Table and re-create it using these rules on the empty EZ 20 x 20 Table when you turn the page.

Check MisterNumbers on Youtube.com for help creating this table.

#### Seeing the Patterns in the Ones-digits and Tens-digits

	EZ Patterns 10 x 10 e2007 Tom Stevers								
9	7	5	3	1	2	4	6	8	10
09	07	5	3	1	2	4	6	8	10
18	14	10	6	2	4	8	12	16	20
27	2 1	15	9	3	6	1 2	18	24	30
36	28	20	12	4	8	16	24	3 2	40
4 5	3 5	25	15	5	10	20	3 0	4 0	50
5 4	42	30	18	6	12	24	36	48	60
63	49	3 5	2 1	7	1 4	28	42	56	70
72	56	40	24	8	16	3 2	48	6 4	80
8 1	63	45	27	9	18	36	5 4	72	90
90	70	50	3 0	10	20	40	60	80	100

#### Using the Patterns in the Ones-digits and Tens-digits

		EZ	Patter	ns 10 x	20 620	07 Tom Ble	eenz		
9	7	5	3	1	2	4	6	8	10
0 9	7	5	3	1	2	4	6	8	10
18	1 4	10	6	2	4	8	12	16	20
2 7	2 1	15	9	3	6	1 2	1 8	24	3 0
3 6	28	20	1 2	4	8	16	2 4	3 2	4 0
4 5	3 5	25	15	5	10	20	3 0	40	50
5 4	42	3 0	18	6	1 2	2 4	3 6	48	60
63	49	3 5	2 1	7	1 4	28	4 2	56	70
7.2	56	4 0	2 4	8	16	3 2	4 8	64	8.0
8 1	63	45	2 7	9	1 8	3 6	54	72	90
90	70	50	30	10	20	4 0	60	80	10 0
99	77	5 5	3 3	1 1	22	4 4	66	88	11 0
10 8	84	60	3 6	12	24	4 8	72	96	12 0
11 7	9 1	6 5	39	1 3	26	5 2	7 8	10 4	13 0
12 6	98	70	4 2	1 4	28	5 6	8 4	11 2	14 0
13 5	10 5	7.5	4.5	15	3 Q	60	90	12 0	15 0
14 4	11 2	80	4 8	16	3 2	6 4	96	12 8	16 0
15 3	11 9	8 5	5 1	17	3 4	68	10 2	13 6	17 0
16 2	12 6	90	5 4	18	3 6	72	10 8	14 4	18 0
17 1	13 3	95	5 7	19	3 8	76	11 4	15 2	19 0
18 0	14 0	10 0	60	20	4 0	80	12 0	16 0	20 0

#### NUMBER PATTERNS TO 20 x 20

The top half of the **EZ 20 x 20 Table** is the **EZ 10 x 20** Table from the previous page. The bottom half is the EZ  $11 \times 20$  patterns. These are lined up so that the Nineteens are located directly below the Nines, The Seventeens are located directly below the Sevens, etc. In the top half, the Ones show you the row numbers. There are numbers on the right to show the row number in the lower half of the Table.

Notice that the ones-digit in the right column have created a pattern in the  $10 \times 20$  top portion of the Table and are exactly the same numbers in the same pattern in the Nines as in the Nineteens. This holds true for every column and **you can fill in all the ones-digits in the Eleven to Nineteen columns simply be repeating the patterns** established in the Ones to Tens columns above them!

See that this is true on the EZ 20 x 20 Table on the right and fill in those patterns on the blank EZ 20 x 20 Table when you turn the page. You may want to use your **EZTT** or the **EZMFT** to see the patterns. You have now created all the ones-digits for the 20 x 20 Table

Now we will use a similar pattern from the last page to create the **tens-digits** on the  $11 \times 20$  part of the table. In the first row of 12-19, put a 1 in the left column to create the numbers 12-19, since the ones-digits are already in place. To do the next row, look at the number above on the ones-digit side.

If the new ones-digit number is larger, increase the previous number on the left by one. If it is smaller, increase the number by two (e.g. after 12, the ones-digit pattern indicates a shift from 2 to 4 in the ones digit. Since the 4 is larger than 2, the tens increase by 1: resulting in 24. After 48 the pattern indicates a shift from 8 to 0. Since the 0 is smaller, the tens increase by two, resulting in 60). Use this pattern going down the tensdigit columns to fill in all the numbers.

**You are done.** I hope you made it through the maze of words because the patterns are fairly simple and creating the Table is satisfying.

You can actually start with a blank  $20 \times 20$  table, fill in the Ones-digits from the Rule of Tens, and use the two rules for Tens-digits to fill in the whole table. There is also a blank  $20 \times 20$  Table for you to fill in with these patterns. The Ones are filled in as well as the first row of 11-19 to get you started. Follow the instructions on the last pages and you will have created the times table to  $20 \times 20$  from patterns without doing any multipying!

Creating EZ Patterns 20 x 20 in two parts (10 x 20 and 11 x 20)

9 7 5 3 1 2 4 6 8 10  0 9 7 5 3 1 2 4 6 8 10  1 8 14 10 6 2 4 8 12 16 20  2 7 2 1 1 5 9 3 6 12 1 8 2 4 30  3 6 2 8 2 0 1 2 4 8 1 6 2 4 3 2 40  4 5 3 5 2 5 1 5 5 10 2 0 3 0 40 50  5 4 4 2 3 0 1 8 6 12 2 4 3 6 4 8 60  5 4 4 2 3 0 1 8 6 12 2 4 3 6 4 8 60  6 3 4 9 3 5 2 1 7 1 4 2 8 4 2 5 6 70  7 2 5 6 4 0 2 4 8 1 6 3 2 4 8 6 4 8 0  8 1 6 3 4 5 2 7 9 1 8 3 6 5 4 7 2 9 0  9 0 7 0 5 0 3 0 1 0 2 0 4 0 6 0 8 0 100  9 9 7 7 5 5 3 3 1 1 2 4 4 8 7 2 9 6 12 0  10 8 8 4 6 0 3 6 12 2 4 4 8 7 2 9 6 12 0  11 7 9 1 6 5 3 9 13 2 6 5 2 7 8 10 4 13 0  12 6 9 8 7 0 4 2 1 4 2 8 5 6 8 4 11 2 14 0  13 5 10 5 7 5 4 5 1 5 3 0 6 0 9 0 12 0 15 0  14 4 11 2 8 0 4 8 1 6 3 2 6 4 9 6 12 8 16 0  13 3 11 9 8 5 5 7 1 9 3 8 7 6 1 4 18 20  3 8 3 4 3 0 2 6 2 2 2 4 2 8 3 2 3 6 4 0  5 7 5 1 4 5 3 9 3 3 8 7 6 1 4 15 2 19 0  EZ Patterns 11 x 20 e2007 Torn Elemns  EZ Patterns 11 x 20 e2007 Torn Elemns  EZ Patterns 11 x 20 e2007 Torn Elemns  19 17 15 13 11 12 14 16 18 20  3 8 3 4 3 0 2 6 2 2 2 4 2 8 3 2 3 6 4 0  9 5 8 5 7 5 6 5 5 6 6 7 2 8 4 9 6 10 8 12 0  11 1 4 10 2 9 0 7 8 6 6 7 2 8 4 9 6 10 8 12 0		EZ Patterns 10 x 20 e2007 Tom Bleeonz											
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Create your own 20 x 20 Times Table here from Patterns 137

	EZ	Patter	ns in O	nes thr	ough T	ens e20	07 Tom Bh	MANZ	
9	7	5	3	1	2	4	6	8	10
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#### **EZ RULER TABLE**

This EZ Ruler Table is created on a blank sheet of paper with just a 1" wide ruler and a pencil. It is interesting to view new patterns and see how the Threes and Sixes, and Fours and Eights are connected. It is also possible to re-create part or all of it in a testing situation. I suggest doing an EZTT first because it will establish how to create the Ones and Twos accurately. Neatness helps and variations are included at the bottom of this page. The next few pages will demonstrate the steps in creating the EZ Ruler Table.

- 1. Put the ruler along the top of the page and draw a line on the lower side.
- 2. Put the pencil tip roughly in the center of that line and draw a line down the page perpendicular to the first line. Accuracy is not important here.
- 3. Put the top of the ruler on the horizontal line and draw a line on the lower side of the ruler making a parallel line. Repeat until you have 9 evenly spaced horizontal lines.
- 4. Put a big 1 above the left side of the T made by the first two lines. Placing four numbers per line, put the numbers 1-32 just to the left of the vertical line.
- 5. Put a big 2 above the right side of the T made by the first two lines. Using four numbers per line, put the even numbers 2-64 just to the right of the vertical line.
- 6. Put a small-circled 3 babove the big 1 and 2. Count every third set of numbers (3 and 6, 6 and 12, 9 and 18, etc.) and enclose with an oval.
- 7. Put a 48 in a rectangle above the big 1 and 2. Put a rectangle enclosing numbers that are just above the lines. Rectangles create the 4's and 8's. Starting at the vertical line, draw horizontal lines to the left under the 1, 2, 3, 5, 6, 7, 9, and 10 (lines are already under the 4 and 8).
- 8. Put a big 5 to the left of the big 1. Count by Fives down to 50 in the ten spaces.
- 9. Put a big 9 to the far left of the big 1. Put a vertical dotted line down the ten spaces. Put 0-9 going down the left side of the dotted line and 0-9 going up the right side of the dotted line. This creates the Nines.
- 10. Put a big 7 between the big 5 and the big 9. Put 49 in the seventh space.

**You are done.** Count the circles to multiply by 3 and 6 and count the lines to multiply by 4 and 8. The other numbers are similar to the **EZTT**.

**Variations:** Use these variations to make the Table neater and give more and faster answers.

- 1. Use dotted lines for the Ones and Twos column for accuracy.
- 2. Number the horizontal lines starting with 1 after the first four numbers. This gives the number for multiplication by 4 and 8. The sixth line:  $4 \times 4 = 16$  and  $4 \times 8 = 32$ . Also number the ovals for multiplying by 3 and 6.
- 3. Extending the Ones and Twos to 36 and 72 below the last horizontal line gives more answers.
- 4. Count down every 5th set of numbers and put an arrow in front of the numbers in the Ones and Twos columns. This creates your Fives and Tens.
- 5. Create these patterns on the **EZTT** after creating the Ones and Twos. The last Table shows the variations and tips on how to use this Table. Enjoy!

1	2
1	2
1 2 3	2 4 6
3	
4	8
5	1 0 1 2
6	1 2
7	1 4
8	1 6
9	1 8 2 0 2 2 2 4 2 6 2 8 3 0 3 2 3 4 3 6 3 8
1 0	2 0
1 1	2 2
1 2	2 4
1 3	2 6
1 4	2 8
1 5	3 0
1 6	3 2
1 7 1 8 1 9	3 4
1 8	3 6
	<i>3</i>
$\tilde{2}$ $\tilde{0}$	4 0
2 1	4 2
2 2	4 4
2 3	4 6
2 4	4 2 4 4 4 6 4 8
2 5	5 0
2 6	5 2
2 7	5 4
2 8	5 0 5 2 5 4 5 6
2 9	5 8 6 0 6 2 6 4
3 0	6 0
3 1	6 2
3 2	6 4

1	2
1	2 <b>4</b>
1 2 3	6
4	8
	10
5 6 7	1 2 1 4
8	16
	1.8
1 0	2 0
1 <u>1</u>	2 0 2 2 2 4
1 3	2.6
14	2 8 3 0
15	3 0 3 2
16	
18	3 4 3 6
1_9_	38
2 0	4 0
2 1 2 2	4 4
23	4.6
24	48
2 5	5 0
27	54
2 8	5 6
29	5 8
3.1	6.2
3 2	4 4 4 6 4 8 5 0 5 2 5 4 5 6 5 8 6 0 6 2 6 4

EZ I	RUL	.ER	TABLE	steps 8-	11 <	3
	9	•	7	5	1	4 8 <b>2</b>
	0	9		5	1	2
•	1	8		10	2	4
	2	7		15	<u>3</u>	6
	3	6		20	4	8
	4	5		25	5	1 0
•	5	4		30	<b>€</b>	12
	6	3	49	35	7_	14
	7	2		40	8	16
•	8	1		45	<b>_</b>	18
•	9	0		50	1 0	2 0
•					11	2 2
					12	24
					1 3	2 6
					14	2 8
					1 5	3 0
					1 7	3.4
					18	3.6
					1 9	3 8
					2.0	4.0
•					21	4 2
					2 2	4 4
					23	4 6
					24	48
•					25	5 0
					26	5 2
					27	<del>5 4</del>
					28	<del>30</del>
					$\frac{29}{20}$	5 8
					3 U	6.2
					3 2	4 2 4 4 4 6 4 8 5 0 5 2 5 4 5 6 5 8 6 0 6 2 6 4
•					- <u>-</u> -	

				3	(	6	EZ RULER TABLE variations 1-4	1
9	7	5	1	4	8	2		
0 9		5		1		2		
1 8		10		2		4		
2 7		15		3		6	$\rightarrow$ 1	
3 6		20		4		8		1
4 5		25	<b>→</b>	5	1	0		
5 4		30		6	1	2	→ 2	
6 3	49	35		7	1	4		
7:2		40		8	1	6		2
8 1		45		9	1	8	This	
9 0		50	<u>→</u> 1	0	2	0	4th oval on the	
•			1	1	2	2	left shows that the fourth 3 is 12 and the	_
			$\bigcirc 1$	2	2	4	4 fourth 6 is 24.	3
			1	3	2	6		
			1	4	2	8		
			1	5	3		<b>&gt;</b> 5	4
			1	b	3	2		7
			1	Z	3	4	This rectangle on  the left and the line	_
			$\bigcirc 1$	8 9	3		number show that	
			$\rightarrow \frac{1}{2}$	0	<u>3</u>	_8 ∩⊬	the fifth 4 is 20 and the fifth 8 is 40	4
			7	7	7	<del>-</del>	7	
			2	5	4	4		
			2	3	4			
			$\bigcirc$ 2	4	4		<b>&gt;</b> 8	6
			<b>→</b> 2	5	5	0		
			2	6	5	2		
			$\bigcirc 2$	7	5	4	<b>&gt;</b> 9	7
			2	8	5	6		7
I	ixth arr s that tl	_	2	9	5	8		
I	5 is 30		3	0	6	0	<b>&gt;</b> 10	
the siz	xth 10	is 60	3	1	6	4		8
				3	<b>6</b>		<b>&gt;</b> 11	
			3	4	6	8	> 11	_
			3	4 5 6	7 7	0 L 2		9
					•	I		

#### Fun Patterns in Numbers

1 x 1 = 1 11 x 11 = 121 111 x 111 = 12321 1111 x 1111 = 1234321 11111 x 11111 = 123454321 111111 x 111111 = 12345654321 1111111 x 1111111 = 1234567654321 11111111 x 11111111 = 123456787654321

1 x 9 + 2 = 11 12 x 9 + 3 = 111 123 x 9 + 4 = 1111 1234 x 9 + 5 = 11111 12345 x 9 + 6 = 111111 123456 x 9 + 7 = 1111111 1234567 x 9 + 8 = 11111111 1234568 x 9 + 9 = 1111111111 123456789 x 9+10 = 111111111

6<sup>2</sup> = 36 66<sup>2</sup> = 4356 666<sup>2</sup> = 443556 6666<sup>2</sup> = 44435556 66666<sup>2</sup> = 4444355556 666666<sup>2</sup> = 444443555556

1 x 8 + 1 = 9 12 x 8 + 2 = 98 123 x 8 + 3 = 987 1234 x 8 + 4 = 9876 12345 x 8 + 5 = 98765 123456 x 8 + 6 = 987654 1234567 x 8 + 7 = 9876543 12345678 x 8 + 8 = 98765432 123456789 x 8 + 9 = 987654321

9 x 9 + 7 = 88 98 x 9 + 6 = 888 987 x 9 + 5 = 8888 9876 x 9 + 4 = 88888 98765 x 9 + 3 = 888888 987654 x 9 + 2 = 8888888 9876543 x 9 + 1 = 88888888

# Creating the Ones and Nines from fun patterns

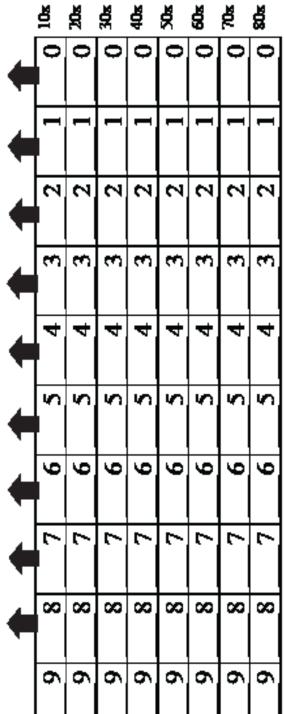
Ones

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http://RightBrainMath.com

뵬	ģ	8	<b>∯</b>	Š	ĝ	ę	ğ
0	0	0	0	0	0	0	0
6	6	6	6	6	6	6	6
<b>0</b> 0	90	90	<b>o</b> ¢	8	90	8	<b>0</b> 0
7	7	7	7	7	7	7	7
9	9	9	9	9	9	9	9
3	5	5	5	5	5	5	5
4	4	4	4	4	4	4	4
3	3	3	33	3	3	3	3
2	2	2	2	2	2	2	2
1	1	1	1	1	1	1	1

# Nines



# See EZ Times Table pp 54-58. It's Easyl RightBrainMath.com

# Directions for making the Ones and Nines w/patterns

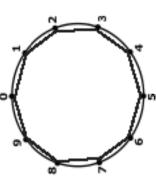
The numbers on this page are the pattern for the Ones and Nines. The Ones are easy, the numbers 1-0 repeated in the ones-digit place. When we get to 0, there is an above it because the tens-digit gets bigger

You are making 10 in each row so the last column ends in 10, 20, 30, 40, etc.

The Nines work the same way.

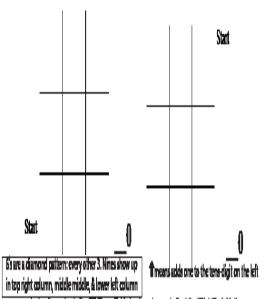
Each number after the first 9 is smaller, so the tens-digit has to get bigger, and has an pover it.

Starting with 0 in front of the first 9, put a 1, 2, 3, 4, 5, 6, 7, 8, and 9 in front of the other numbers. You have created the Nines. You can continue in the next row, repeating the 9 in front of the second 9, and then 10, 11, 12, 13, 14, 15, 16, 17, and 18. You are now at 9 x 20.



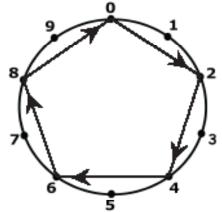
See MasterNumbers instructional videos Magic Blackboard: http://youtube.com/user/MisterNumbers

Multiplication by TEIREES Multiplication by SEVENS © 2009 Right Brain Math



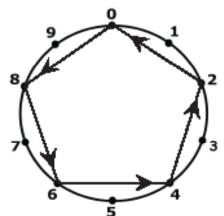
Right Brain Math 2's, 4's, 6's and 8's

Create	your or	vn Twos	3		_
2	4	6	8	0	<b>35</b>
2	4	6	8	0	*18
2	4	6	8	0	<b>±15</b>
2	4	6	8	0	<b>128</b>



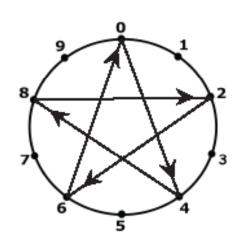
### Create your own Eights Resemble on

				1	_
8	6	4	2	0	35
8	6	4	2	0	<b>218</b>
8	6	4	2	0	*15
8	6	4	2	0	<b>328</b>



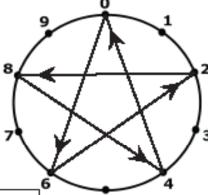
### Create your own 4's

		1		1	_
4	8	2	6	0	<b>15</b>
4	8	2	6	0	ж
_4	8	2	_6	_0	<b>x1</b> 5
4	8	2	6	0	129



### Create your own 6's e 2009 Thomas Biesanz

					_
6		8	_4	_0	ıς
6	2	8	4	0	<b>x30</b>
6	2	8	4	0	<b>385</b>
6	2	8	4	0	129



The ones-digits repeat for each factor set. Start the tens-digits with 0 and add 1 each time the column has a smaller number to its left, indicated by an 👚 above

# Creating the Twos from Fun Patterns

See EZ Times Table

RightBrainMath.com pp 54-58 H's FEZ

An Arrow above a column increases the tens-digit by 1

O  $\infty$  . £ (¥45) ¥ (0) E £ EG £ ŒS દ The last number of each row will be 5 times 2, 10

Directions for Making the Twos Time Table from Patterns to 100

Twos (2, 4, 6, 8, and 0), and are repeated. These are, of course, the even numbers The numbers on this page are the pattern for the

We will use a simple pattern to create the tens-digit numbers to go in front of the Ones-ies. These are the ones-digit numbers, that we can call the Ones-ies. They repeat as the Twos get larger.

repeat the tens-digit number (Tens-ies) before it If there is an 👚, add one to the previous Tens-is. unitess the columns bass an T over at (the 0 columns) Start tens-digits with 0. The simple pattern is to

times 2, 15 times 2, up to 50 times 2 (100).

Starts out 02, 04, 06, 08, and 10. It ends with 92, 94, 96, 98, and 100.

http://RightBrainMath.com WiskerNumbers on Youtube

© 2009 Thomas Biesanz, Right Brain Math

ILS II OIII I AUCIIIS RAS K8EE. RightBrainMath.com		Describers for Making the Lights Time Table from Patterns to 400			<del>-</del> -			Together these two numbers will make up the sequence of the Eights. The last number of each row will be 5 times 8, 10 times 8, 15 times 8, etc			DOS RightBrainMath
=======================================	[	<u>3</u>	(Ell)	(ta)	(§)	(E)	(E)	(E3)	0	(mg)	(§3)
)	≺	_	0				)		)	)	)
	<b>4</b>	7	2	2	2	2	2	2	2	2	2
	≺	4	4	4	4	4	4	4	4	4	4
m gun	<	9	9	9	9	9	9	9	9	9	9
CICa		∞	∞	∞	∞	8	∞	8	8	<b>%</b>	8

Starts out 08, 16, 24, 32 and 40. It ends with 368, 376, 384, 392, and 400. © 2008 Right Brain Math. http://RightBrainMath.com. MisterNumbers on Youtube.

# Creating the Fours from Fun Patterns

An errow above a column

4	4	4	4	4	4	4	4	4	4	ing
<b>∞</b>	8	8	8	8	8	8	8	8	∞	increases tens-digits by 1
2	2	2	2	2	2	2	2	2	2	by1
6	6	6	6	6	6	6	6	6	6	
0	0	0	0	0	0	0	0	0	0	
£	(¥.	(£	(£35) 1	(£36)	(22)		<b>(£15</b> )	(±10)	Ē	_
10 tie 1		realun Present Puers	We w	ट्यो th ोबहुध	the Fo	Ħ				=

Directions for Making the Sixes l'ime l'able from Patterns



e cambers on this page are the pattern for ours (4, 8, 2, 6, and 0), and are repeated

vill use a sample pattern to create the be Ones-ies. They repeat as the Fours get to are the ones-digit nambers, that we can

digit numbers to go in front of the Ones-ies

at the tens-digit number (Tens-ie) before it is the column has an Tower it. If there is an ens-ues es "same, up, same, up, up" nce to the previous Tens-ie. The pattern for trans-digits with 0. The sample pattern is to

mes 4, 15 times 4, up to 50 times 4 (200) last number of each row will be 5 times 4,

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Starts out 04, 08, 12, 16, and 20. It ends with 184,188, 192, 196 and 200.

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See EZ Times Table

RightBrainMath.com лр54-58 № EZ

# Creating the Sixes from Fun Patterns

Right Brain Math. com

Se EX Thes Table

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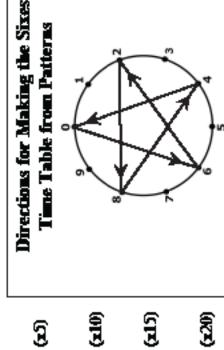
An arrow above a column increases tens-digit by 1. 3

4

 $\infty$ 

す

 $\infty$ 



The numbers on this page are the pattern for the Sixes (6, 2, 8, 4, and 0), and are repeated

g

4

 $\infty$ 

4

 $\infty$ 

(

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 $\infty$ 

These are the ones-digit nambers, that we can call the Ones-ies. They repeat as the Sixes get

3

4

 $\infty$ 

tens-digit numbers to go in front of the Ones-ies We will use a sample pattern to create the

£

4

 $\infty$ 

9

4

 $\infty$ 

number (Tens-ie) befine it unless the column has arroious Tens-ie. The pattern for the Tens-ies is: See EZ Times Table, pp 54-58 for more info on Say them out load The last number of each row will be 5 times 6, saw and why this works and the Rule of Teas m Tover it. If there is many, and one to the The sample pattern is to repeat the tens-digit 10 times 6, 15 times 6, up to 50 times 6. 'सम्मार, प्या, 'समार, प्या, प्या,

£

4

 $\infty$ 

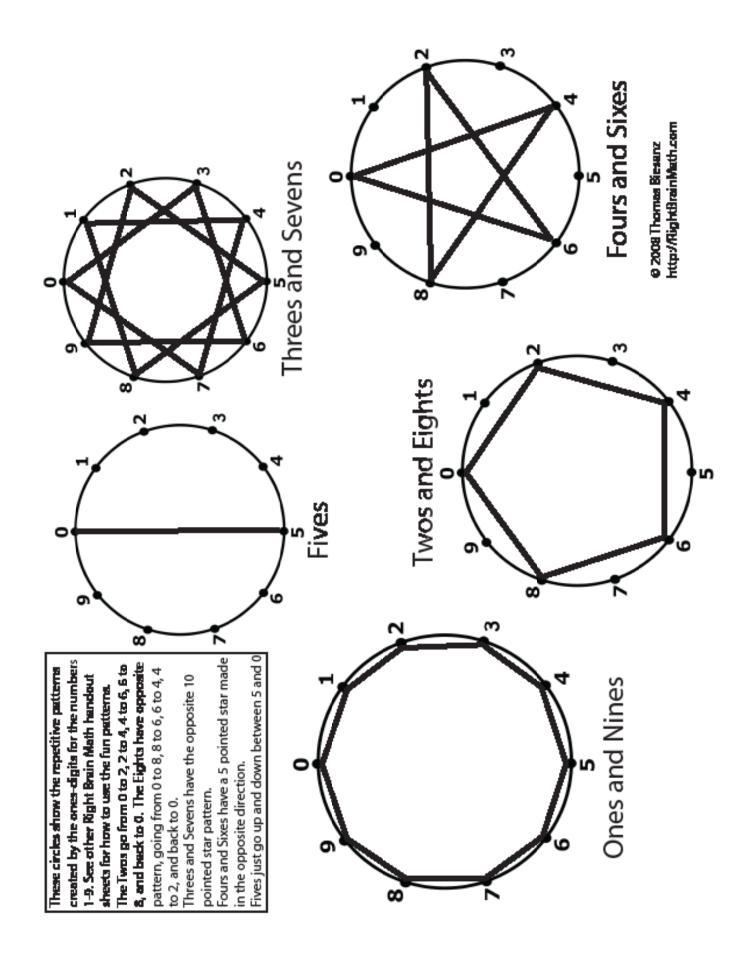
2

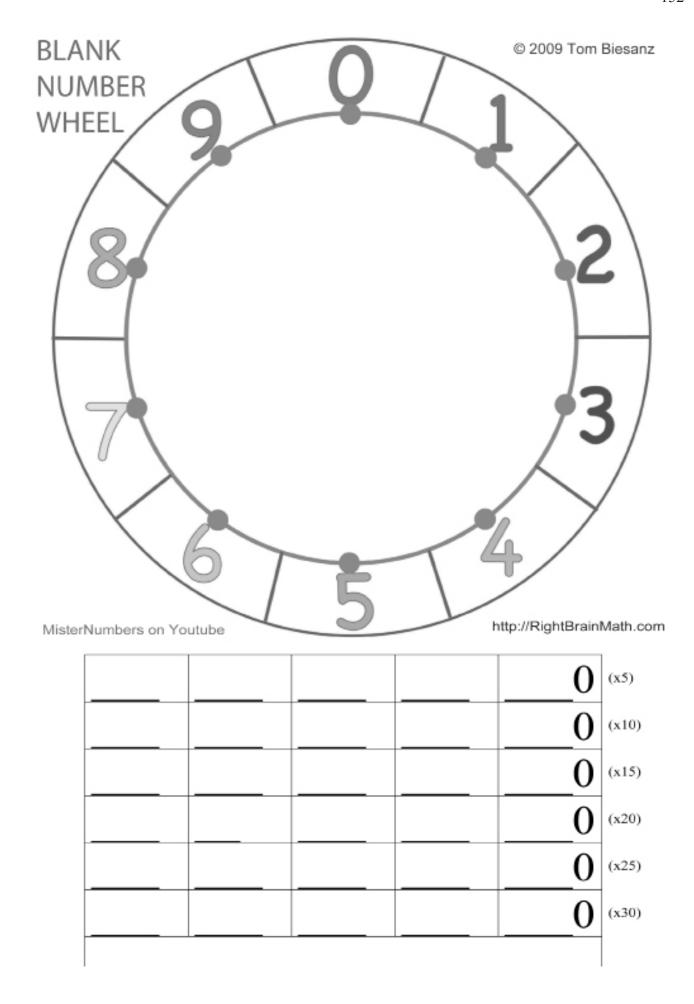
3

4

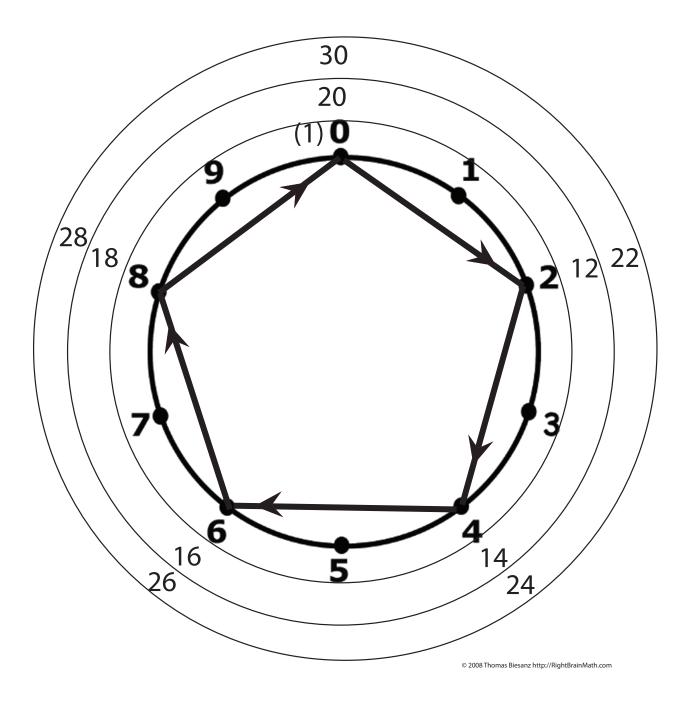
 $\infty$ 

© XXR8 Right Brain Math Inter/RightBrainMath.com MeterNumbers on Youtube: http://www.youtube.com/watch?v=mvOuSYPd0Y Starts out 06, 12, 18, 24, and 30 and ends with 276, 282, 288, 294, and 300.





# Twos on a Number Circle: An Atomic Pentagon



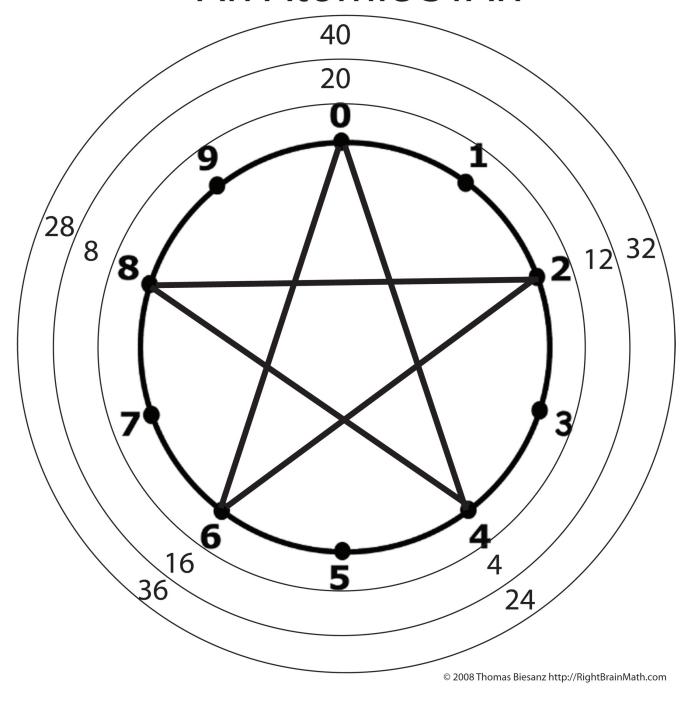
Go around the numbers 2, 4, 6, 8, and 0 in the circle and make a pentagon. Each time you reach 0, jump out one ring and go around again clockwise. The rings keep getting bigger and bigger and contain all the Twos.

E	Z	T	I N	ΙE	S	T	A l	ΒI	. I	3
Cha	rt fo	r mu	ltipl	ving	Nega	ative	e Nu	ımb	ers	3
-10.8	-84	-60	-3m	-12	-2 4	426	-finst	-Ba2		2 0
-9:9	-77	-55	-	-1.1	-22	•	•	•	-11	1 0
-9:0	-70	-50	-	-1.0	-20	4=	•	•	-10	0 0
-8 1	-63	-45	-322	-0.9	-18	٠	-6 <b>x</b> s	•	۷,	0 (
-7.2	-56	-40	•	-0.8	-16	424	•	-8an	-6	3:0
-6:3	-49	-35	•	-0:7	-14	٠	•	•	-7	7:0
-5 4	-42	-30	-3az	-0.6	-12	42	-6 <del>12</del> 2	•	-6	0 6
-4 5	-35	-25	-	-0.5	-10	٠	•	-	4/	0
-3 6	-28	-20	•	-0.4	-0 8	-422	•	-8112	-4	10
-2 7	-21	-15	-3a1	-0.3	-0 6	٠	-6x1	•	Ÿ	3 0
-1.8	-14	-10	•	-02	-0 4	-4x1	•	•	-2	2 0
-0.9	-7	-5	•	-0.1	-02	•	•	-	-1	0
				4	0					
0.9	7	5	•	1	2	٠	•	•	1	0
1.8	14	10	-	2	4	4x1	•	-	2	0
2.7	21	15	3an	3	6	٠	(ize	•	3	0
3:6	28	20	-	4	8	422	•	Bart	4	0
4:5	35	25	•	5	10	•	•	•	5	
5.4	42	30	312	:6	12	4±	linz	•	6	
6.3	49	35	•	7	1 4	•	•	•	7	
7.2	56	40	•	8	16	424	•	Bazz	8	
8:1	63	45	312	9	18	•	6ma	•	9	
9:0	70	50	•	1:0	2 0	4±5	•	•	10	
9 9	77	55	-	1:1	22	•	•	• D -	11	
10 8	84	60	324	12	2 4	4∞	fint	Выз	12	D

EZ Times Table Chart for Negative Numbers Copyright 9 200 by Thomas Brown: <u>Number State Com</u>
Multiplying with negative numbers just means more friends to play with. Face them (like the child above) if you are multiplying by a negative number and then go forward if multiplying that by a positive number or step backward (negative direction) if multiplying by a negative number.

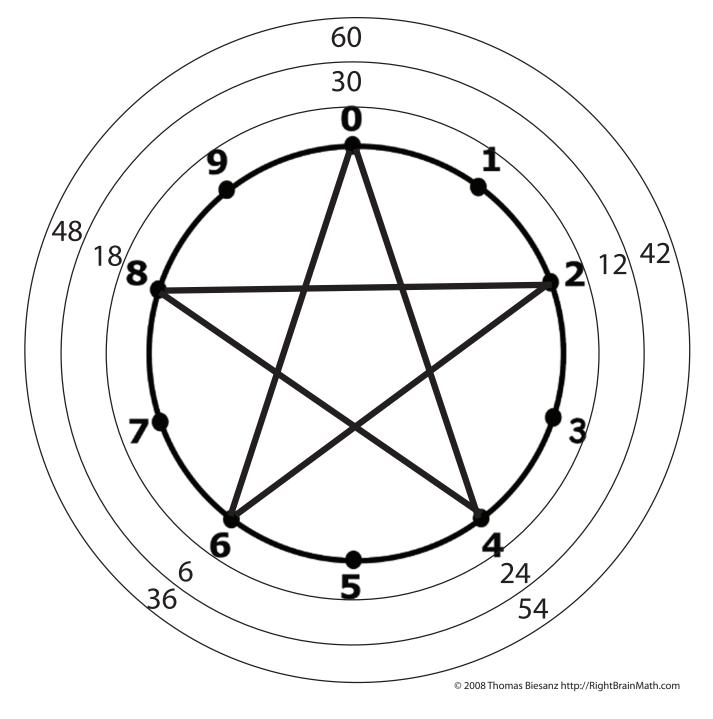
Can you see that multiplying a negative number (facing them) by a positive number (going forward) will take you into the negative numbers (Plus times Minus = Minus. Multiplying negative numbers (facing them) by a negative number (stepping backwards) will take you into the positive numbers (Minus times Minus = Plus).

# Fours on a Number Circle: An Atomic STAR



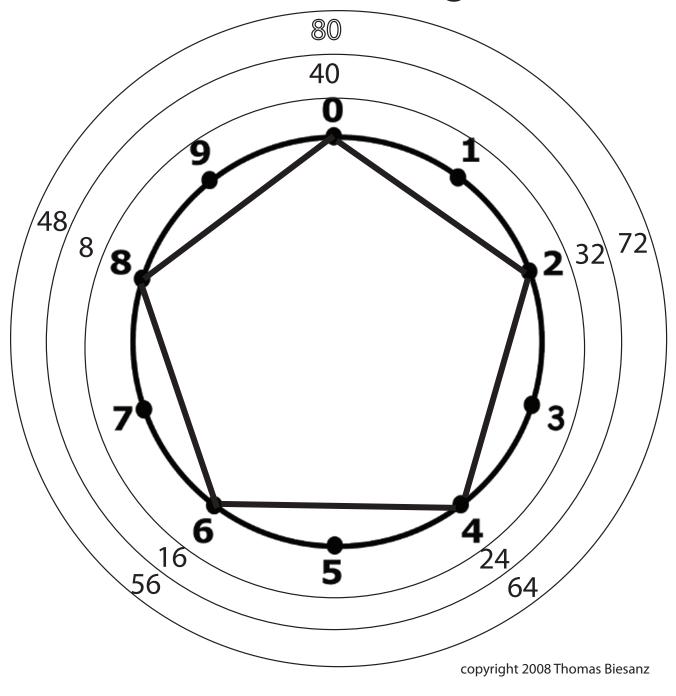
Go around the numbers 4, 8, 2, 6, and 0 in the circle and make a STAR. Each time you reach 0, jump out one ring and go around again clockwise. The rings keep getting bigger and bigger and contain all the Fours.

# Sixes on a Number Circle: An Atomic STAR



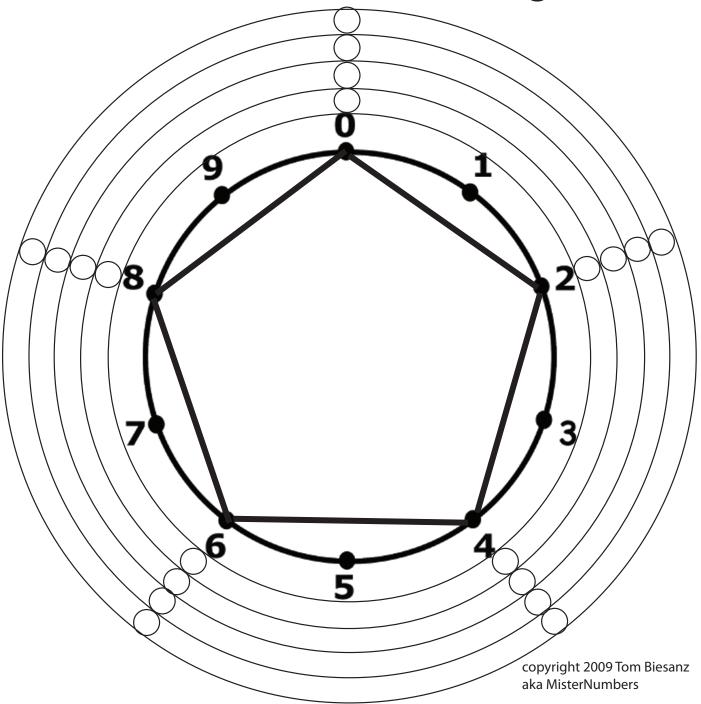
Go around the numbers 6, 2, 8, 4, and 0 on the circle and make a STAR. Each time you reach 0, jump out one ring and go around again clockwise. The rings keep getting bigger and bigger and contain all the Sixes.

# Eights on a Number Circle: An Atomic Pentagon



Go around the numbers 8, 6, 4, 2, and 0 in the circle and make a pentagon. Each time you reach 0, jump out one ring and go around again counterclockwise. The rings keep getting bigger and bigger and contain all the Eights.

## Twos & Eights on a Number Circle: Fill in the Atomic Pentagons



Go around this number wheel clockwise and fill in the first ring of circles to create the TWOS. The first ring will be **2**, **4**, **6**, **8**, and 10. Continue to the next ring. The last ring will end at forty. Now on another copy, go around counter-clockwise to create the EIGHTS. The first ring will be **8**, 16, 24, 32, and 40. The last ring will end at 160. See the Eights worksheet for a demo(http://www.eztimestable.com/EZImages/Eights\_AtomicWorksheet.pdf)

# Odd Numbers **Even Numbers** Complete EZ Table copyright©Thomas Biesanz www.eztimestable.com

### $\mathbf{E}$ **Odd Numbers** Even Numbers 10 5 8 6 0.9 7 10 5 12 4 18 20 4<sub>x1</sub> 14 10 • 3 27 3x1 6 3 0 21 6x1 15 • 4 8 4x28<sub>x1</sub> 4.0 3 6 28 20 15 4 5 35 10 5 0 • 25 6 12 3x2 • 6 0 5 4 42 30 4x3 6x2 49 ;7 14 7:0 63 • 35 8 7 2 8 0 16 • 4<sub>x4</sub> 8x2 56 40 9 18 3хз 63 6x3 8;1 45 9,0 1:0 20 70 • 90 4<sub>x5</sub> **10** 0 50 22 1 1 • 12 3x4 2 4 6x4 8x3 4x6 1|3 2 6 1|4 218 • 4x7 • 15 30 3x5 • 6x5 16 3 2 4x8 • 8x4 1 7 3 4 3x6 118 3 6 4x9 • 6x6 19 3 8 • • 4 0 20 4x10 8x5 • 2 1 4 2 3x7 • 6x7 2|2 4 4 4 • 2|3 4 6 • • • 24 48 3x8 4 6x8 8x6 25 50 2|6 5 2 • 4 • 2|7 3x9 5 4 6x9 28 5 6 4 8x7 29 58 30 6.0 4 3x10 6x10 3|1 6 2 • 6 4 4 8x8

 $0 \times any number = 0$ 

Color EZ Times Table ©2007byThomas Biesanz http://EZTimesTable.com

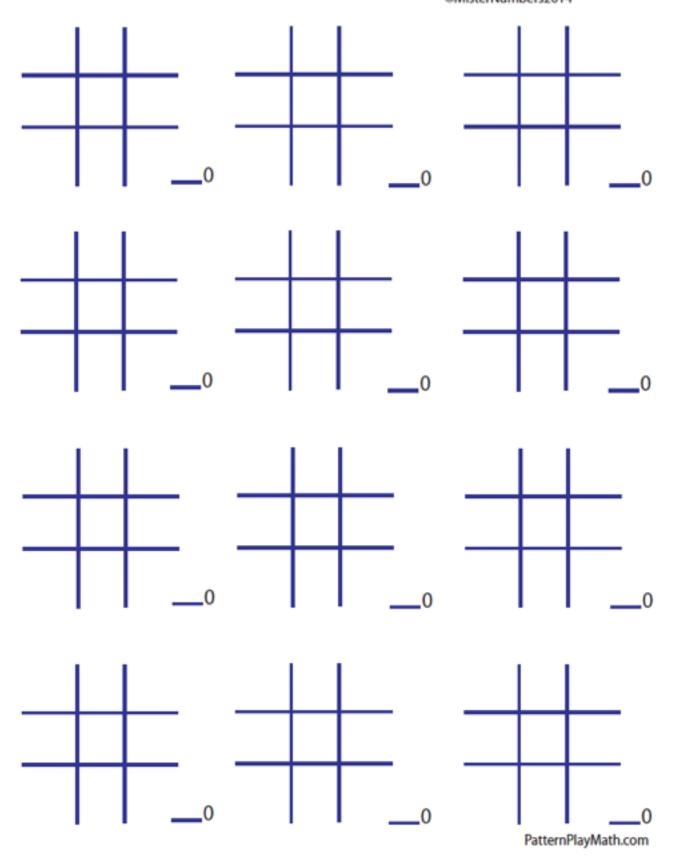
# Thanks to all my friends and contributors for helping me help kids

-MisterNumbers

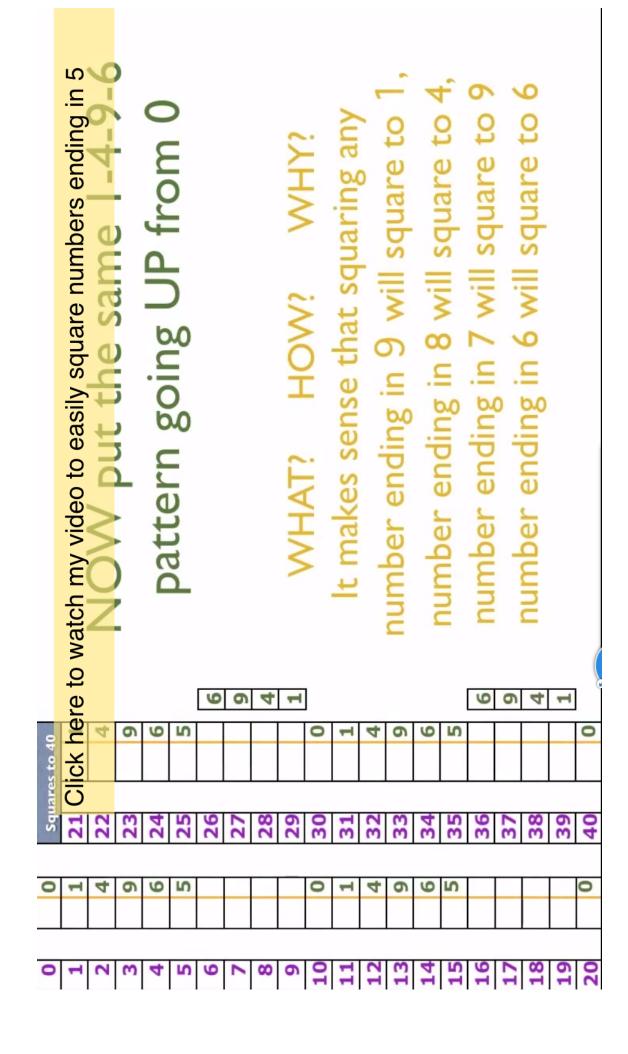
a few MisterNumbers images included below

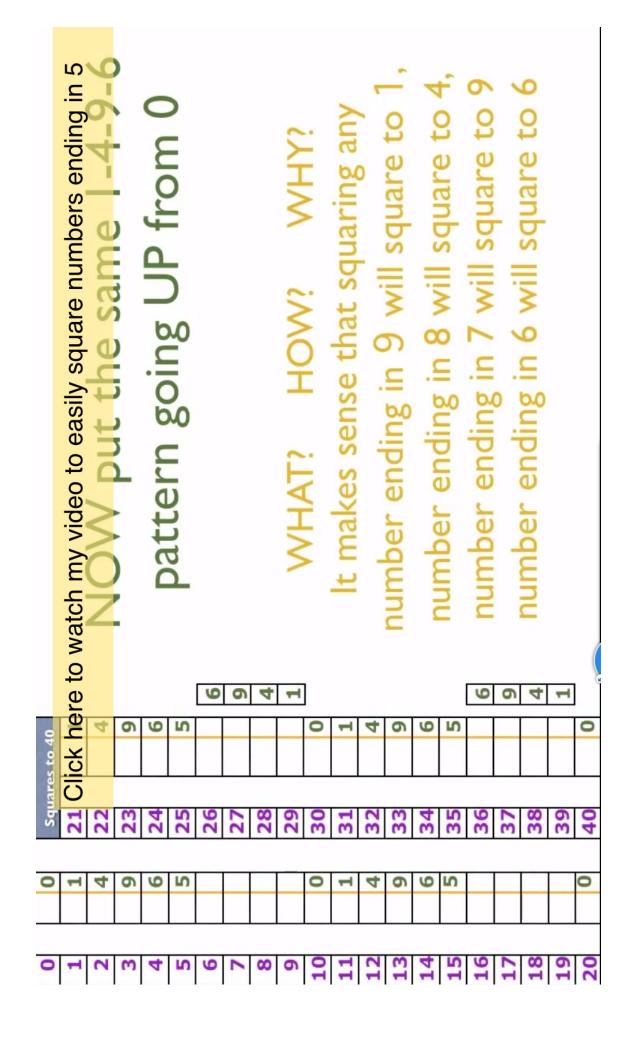
### MisterNumbers TicTacToe Squares for 1s, 3s, 7s, and 9s

©MisterNumbers2014



ANGL	es.	PR	I-NUMBER DICE	PATTEURYS, ADD 25405?	
S			pot	0-1	
L	2	11/7	LINE	2 1-1 -	ALL
	3		TRANC	12 1-1-1 3 2-1 1-2	NUMBERS
	4		26 NAUE	2-1) 4	
5	5		PENTINEN	1-2-1 2-2-1 1-1-2-1-1	APLE CO1
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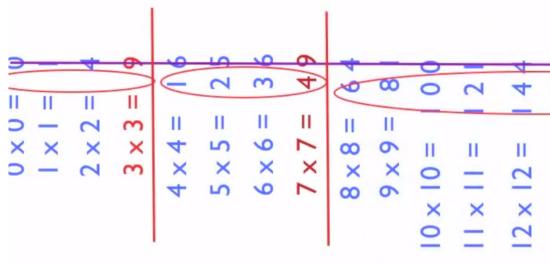




They are 0 (go up 0) until the 9

They go by I until the second 9: I-2-3-4

hey go by 2 until the third 9 6-8-10-12-14-16



A C. C. A+b II. C. 40.00	Aiter the Oth line, tens go		خ <u>حا</u>	, / L	0+0 UZI CZI VVI	144, 134, 160, etc		(notice all multiples of 8)	() .) )).L;;;;;;;;;;)						creating   444   52     600	CI Catilig 1 11, 1041, 1000,		Continue as high as you like	Watch this video to square ANY number: CLICK HERE	
0																			>	
4	1	4	6	9	Ŋ	9	6	4	1	0	1	4	6	9	2	9	0	4	1	C
5	44 1	48 4	52 9	57 6	62 5	9 29	72 9	78 4	84 1	0 06	96 1		6 80		.22 5	129 6	36 9	44		C
ares to	44 1		52 9	57 6		67	72 9		84 1			102 4	108 9	115 6	122 5		1369	_	1	C
Squares to 40	1 44 1		3 52 9		25 <sub>+5</sub> 62 5	29	72 9	78		0 06 7			108 9	115		+7 129	136 9	144	1	0
Squares to	21 44 1		23 52 9	24 57 6		67	27 72 9		29 84 1				33 108 9		35 122 5		37 136 9	44	1	0
O Squares to	1 21 44 1		9 23 52 9			29	9 27 72 9	78		0 30		4 32 102	33	6 34 115	22	6 36 +7 129	9 37 1	4 38 144	1 39 +8 1	40 0
0 0 Squares to	0 1 21 44 1	22 48	0 9 23 52 9	24		26 67	27 7	28 78		10 0 30	121 31		33	34 115	22 5 35	25 6 36 +7 129	289 37 1369	144	1	0
0 0 Squares to	1 21	22 48	9 23	24	5 25 <sub>+5</sub>	6 26 67	9 27 7	4 28 78	1 29	0 30	121 31	4 32 102	33	6 34 115	22	25 6 36 +7 129	9 37 1	4 38 144	1 39 +8 1	40 0

		100	20	
N		75	15	
22		09	12	
	H	20	10	
ike	numbe	40	8	
a number like	5. f that r	30	9	
mp	iple of 1/5 o	25	2	2
na	y mult	20	4	222
	nearb d or su	15	3	
Square	Go to a nearby multiple of 5. igits add or subtract 1/5 of th	10	2	
Squ	) gib-su	2	1	
	Go to a nearby multiple of 5. The Tens-digits add or subtract 1/5 of that number.	Start from	Up or Down	

$7 \times 7 = 49$	Click Here to	Subscribe
number like 17 <sup>2</sup> 28 9	32 4 36 1 40 0 44 1 48 4 52 9	
0	$   \begin{array}{r}     18^{2} \\     19^{2} \\     20^{2} \\     21^{2} \\     22^{2} \\     23^{2}   \end{array} $	
Square Three 4s= 12	20/5=4	



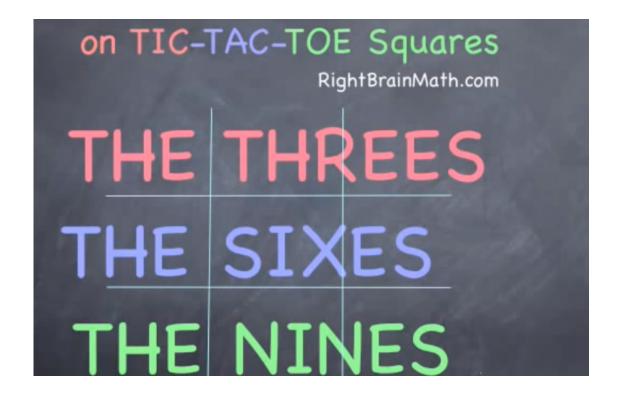
## Amazing Calendar Math Magic



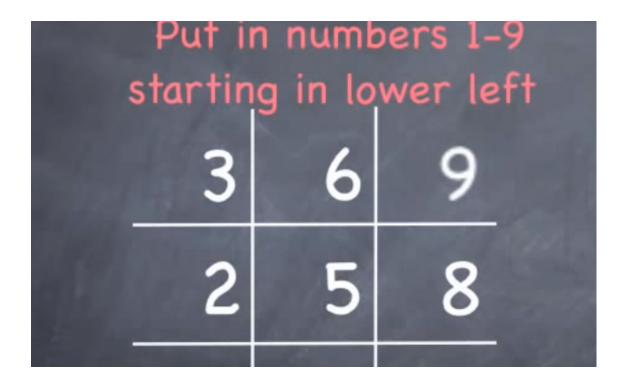
An ingenious trick and practical math tool to help you know what day any date falls on

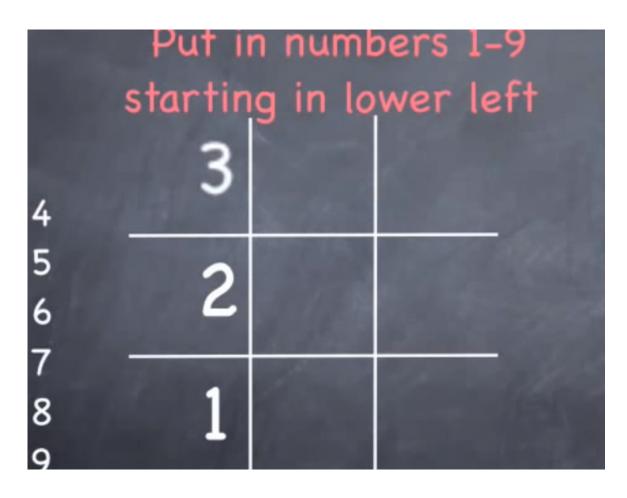
Thomas Biesanz aka MisterNumbers (over a million video views)

## Threes, Sixes, Nines on TicTacToe Squares

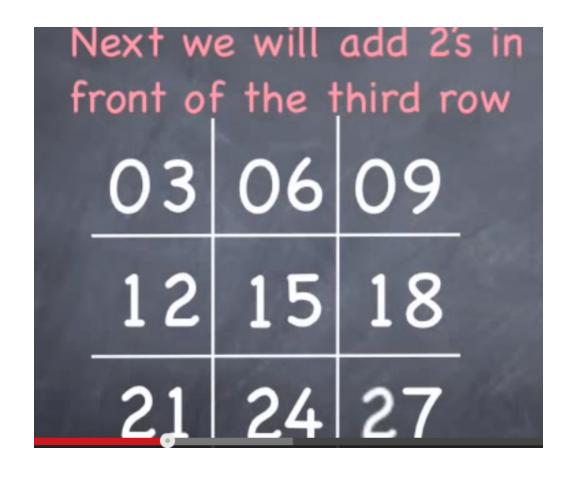


1	Put in numbers 1-9
2	starting in lower left
3	
4	
4 5 6	
6	
7	The state of the s
8	





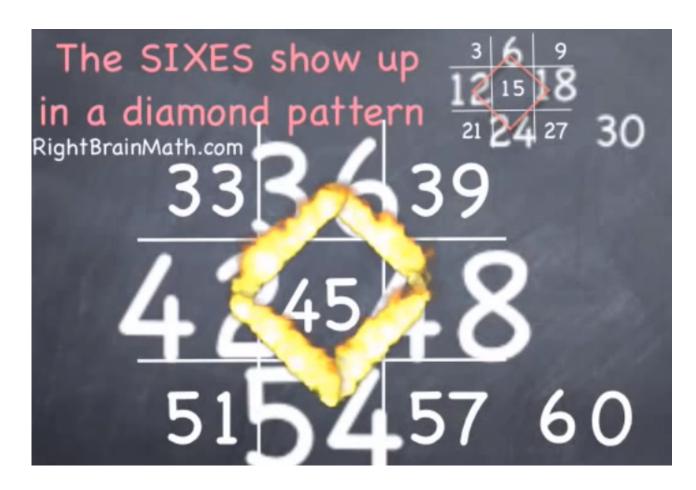
Now we will add 1's in front of the second row					
03	06	09			
2	5	8			
1	4	7			



Start agai	n	with	1-	9		06		-
RightBrainMath.co	m				100	15		
1994					21	24	27	30
	3		Ý.					
	2		-					
A A LOS			+			N.		

10000	time v 444,	ve add & 555	3 6 12 15		
	33	36	39	27	30
444	2	5	8		
5 5 5	1	4	7		

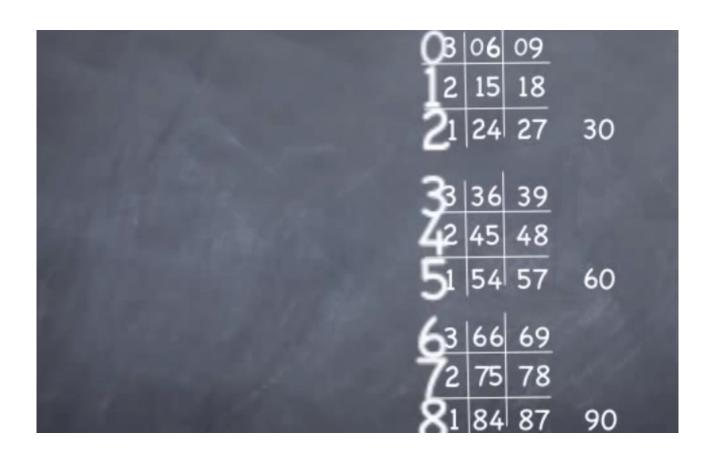
We take ou (6) and ac		12	6 15		
RightBrainMath.com			24	27	30
-		7			
42	45	48	Ę		
51	54,	57		6	0



A th	nird squ	uare	3	6	9	
adds RightBrainMath.com	6's 7's	& 8'5	12	15	18	20
RightBrainMath.com	00, 10	~ 00	21	24	27	30
		K SEL				6
72240 ES	X / 1		33	36	39	
100	The same	The same	42	45	38	
1/2000			51	54	57	60
A STATE OF THE PARTY.	2 3					
A STATE OF THE STATE OF	100	-	and Unit			
44000		ALC: G	2.42			Click He Subscr

RightBrain	add	third s s 6's, 7	quare 's & 8's		6 15 24	9 18 27	30
6	63	66	9	33	36	39	
777	2	5	8	1000		38 57	60
888	1	4	7				Tick V.

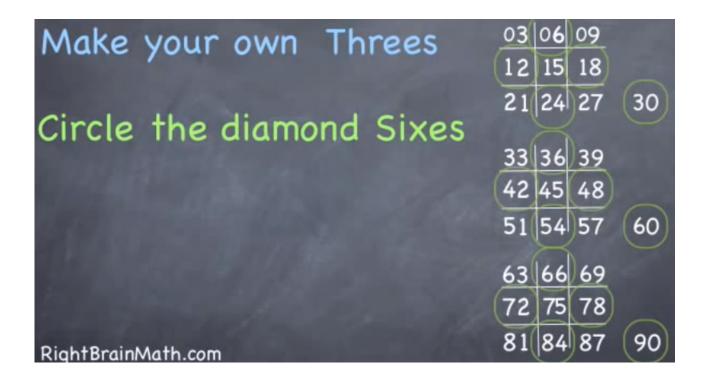
A	third s	quare		3 6	9	
		's & 8's		2   15	18	
RightBrainMath.com	3 0 3, 1	3 00 00	2	1 24	27	30
63	66	69				
05	00	0)	3	3 36	39	50
1000				2 45		96
72	75	78		51 54	57	60
01	01	07	0			
X I	84	87	9			



Nines show up too.  • Right 3 of 1st square	03 06 d <b>9</b> 12 15 <b>18</b> 21 24 <b>27</b>	30
Middle 3 of 2nd square	33 36 39 42 45 48 51 54 57	60
DightBrainMath.com	63 66 69 72 75 78 81 84 87	90

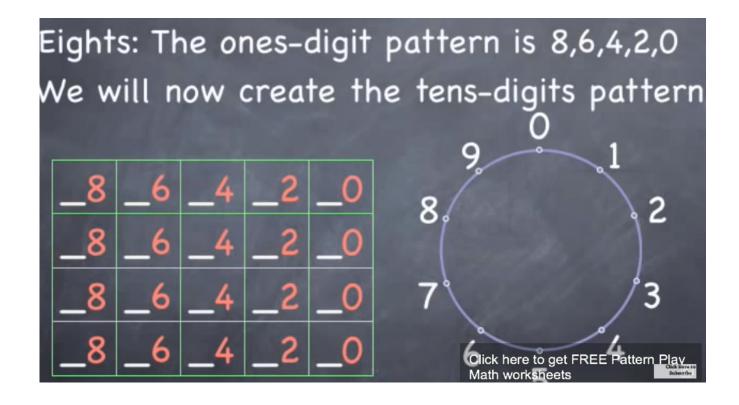
Nines show up too.  • Right 3 of 1st square	03 06 0 <b>9</b> 12 15 <b>18</b> 21 24 <b>27</b> 30
	33 <b>36</b> 39 42 <b>45</b> 48 51 <b>54</b> 57 60
●left 3 of 3rd square	63 66 69 72 75 78 81 84 87 90

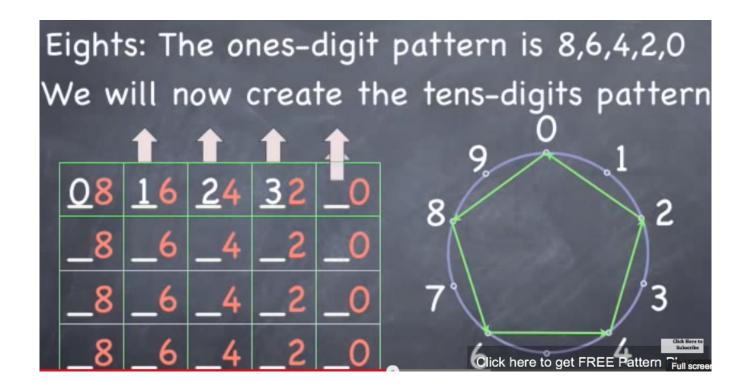
Nines show up too.	03 06 0 <b>9</b> 12 15 <b>1 8</b>
	21 24 27 30
	33 <b>36</b> 39 42 <b>45</b> 48 51 <b>54</b> 57 60
●left 3 of 3rd square	63 66 69 72 75 78 81 84 87 90

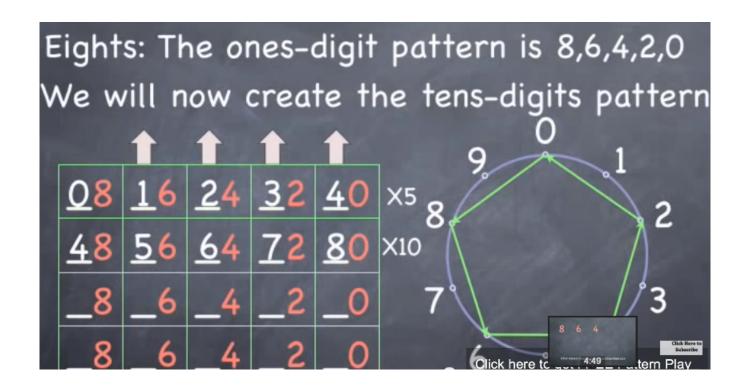


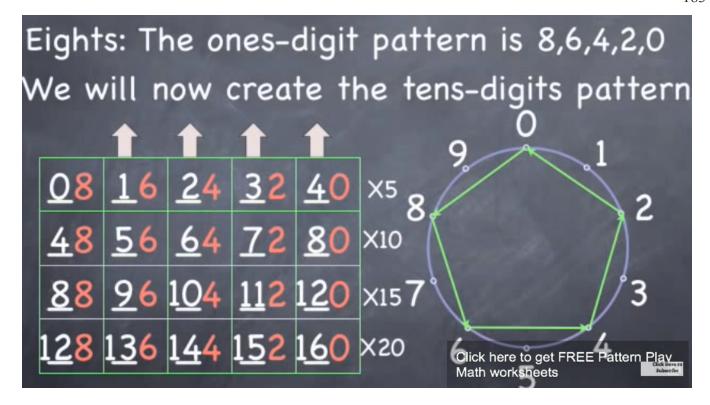
Make your own Threes	03 06 09	
7000 0000	12 15 18	58
	21 24 27	30
Circle the diamond Sixes		
THE RESERVE OF THE PARTY OF THE	33 36 39	6367
Circle the sets of Nines	42 45 48	300
	51 54 57	60
	63 66 69	
	72 75 78	
RightBrainMath.com	81 84 87	90

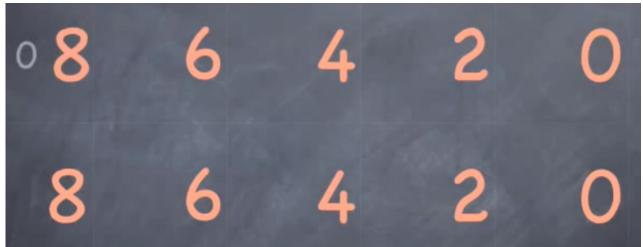
### Eights on a Number Wheel w/ Table

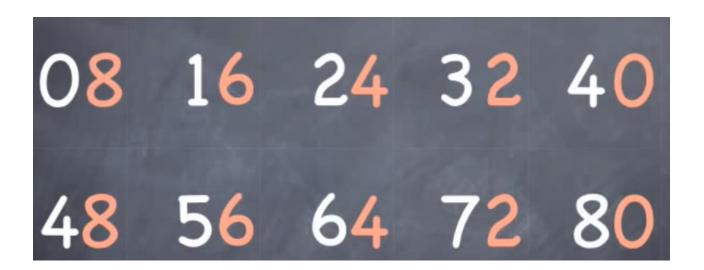




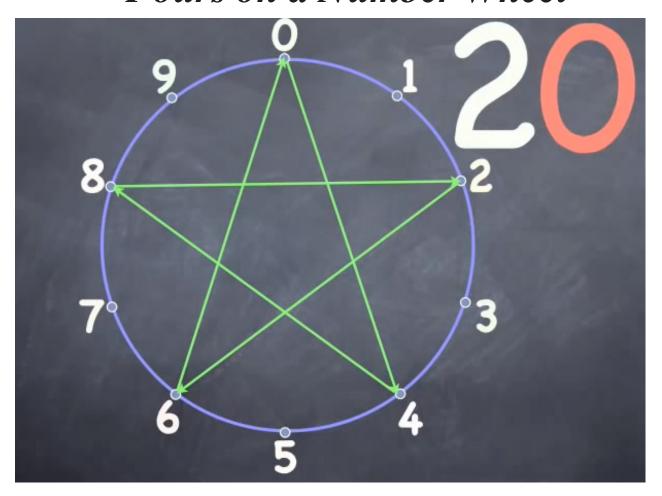


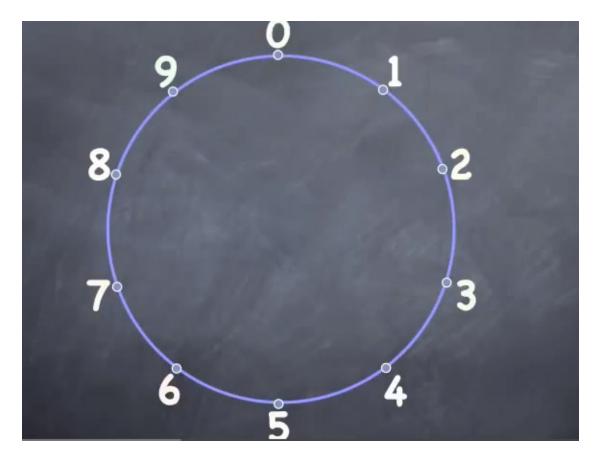


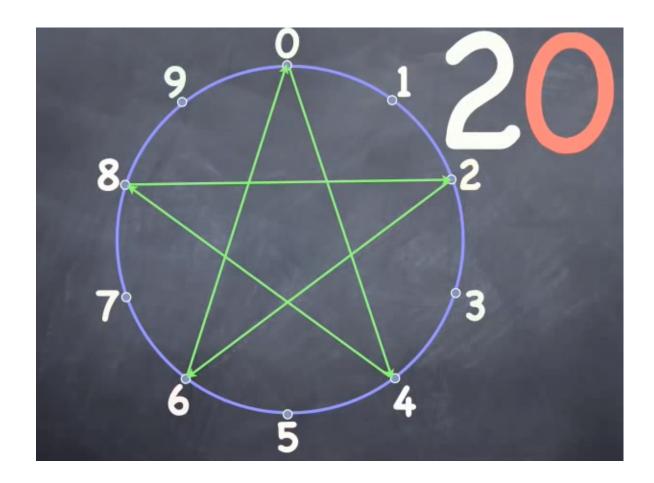


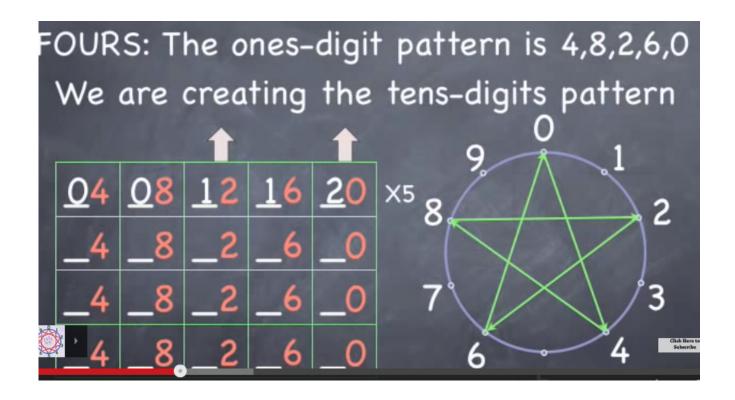


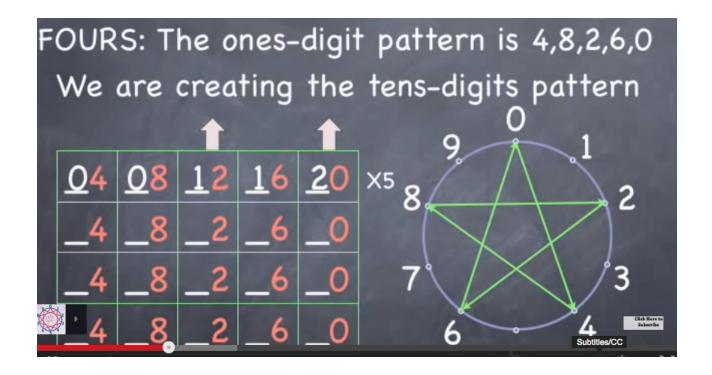
## Fours on a Number Wheel

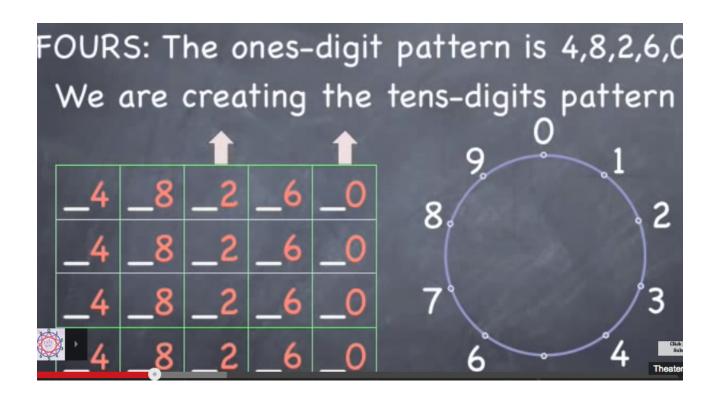


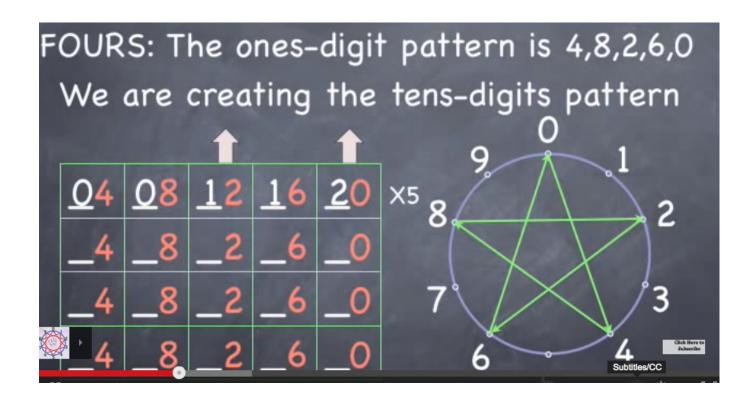


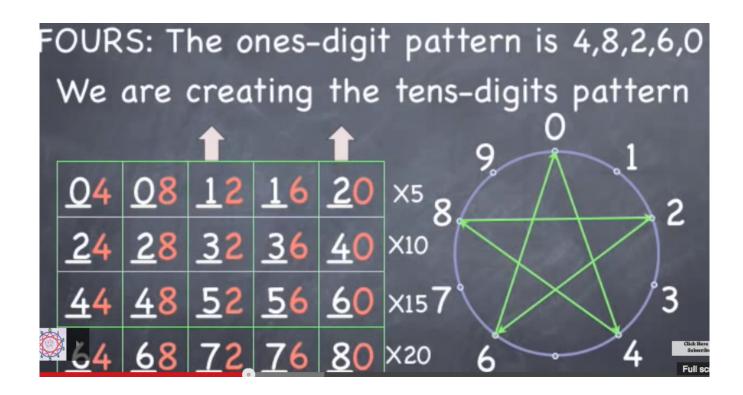


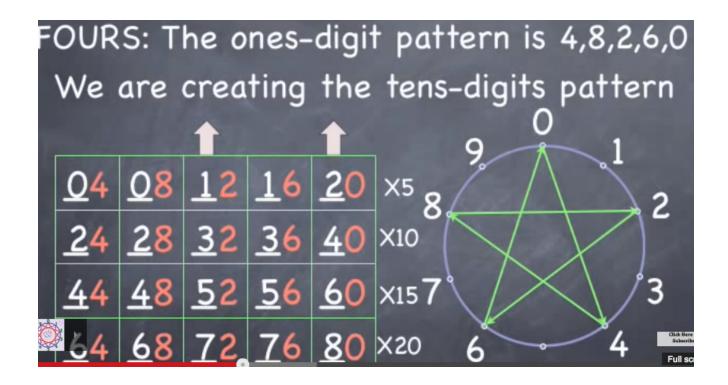


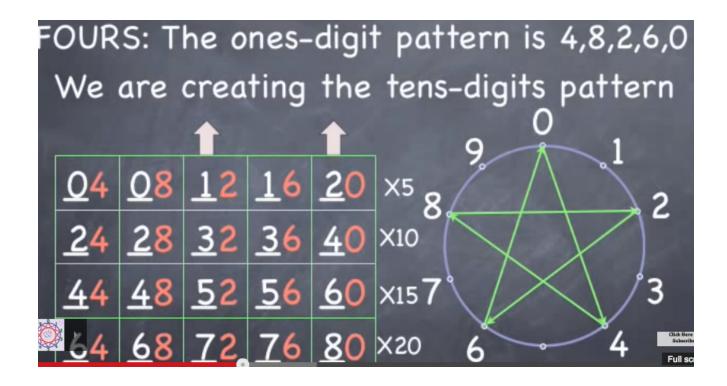








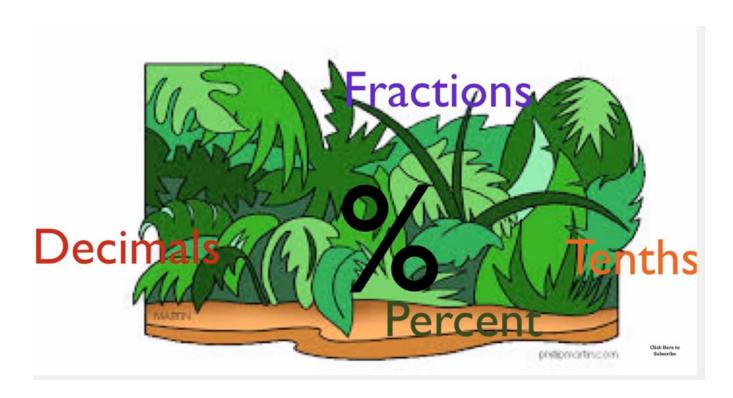


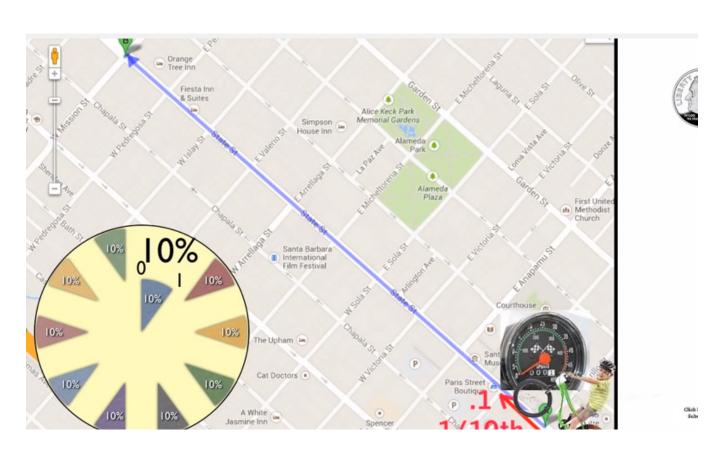




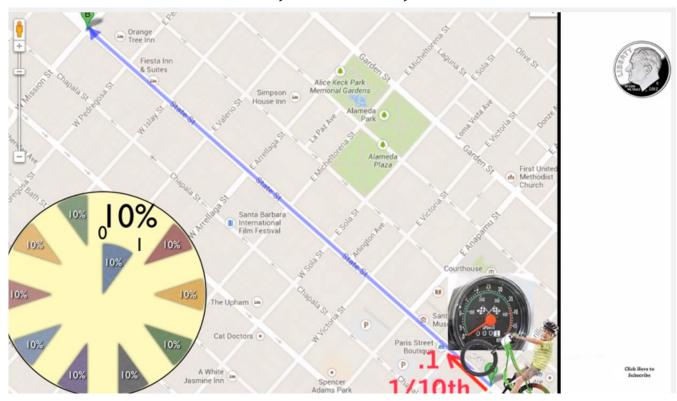


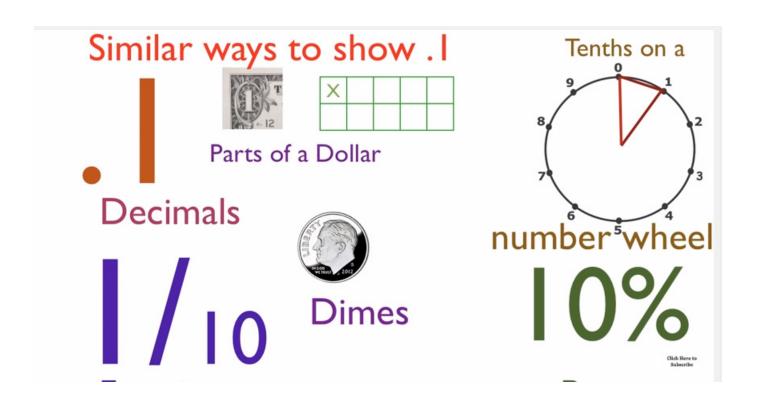
## Fractions, Decimals, PerCent



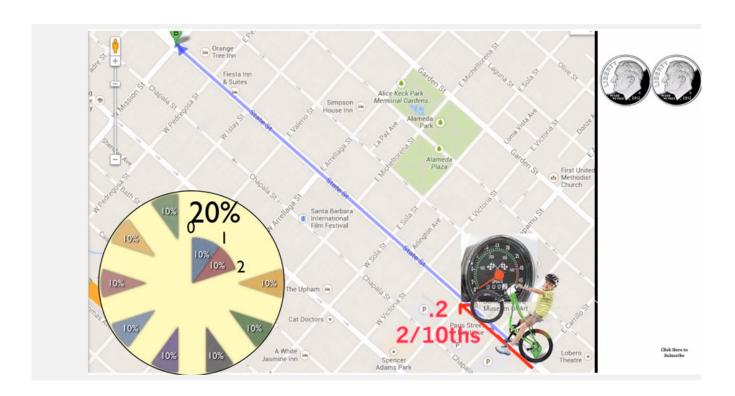


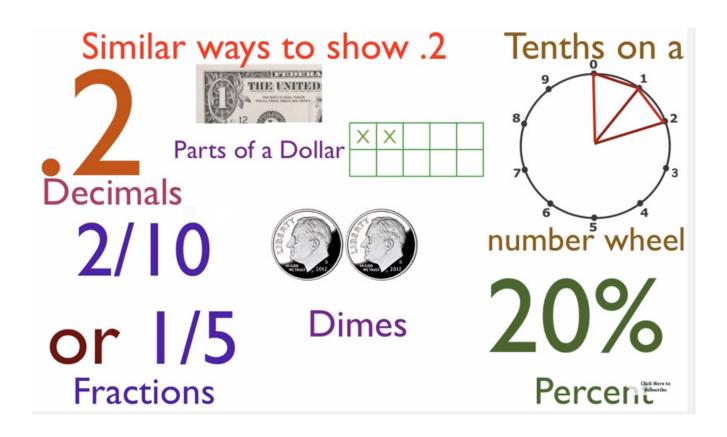
# Ten PerCent, 1/10th, one dime



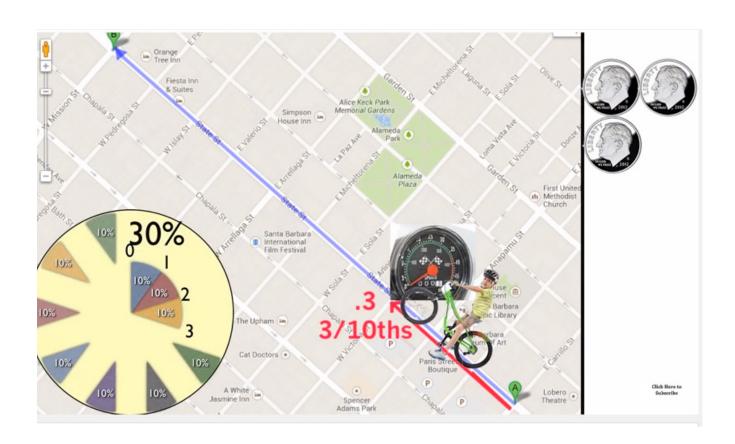


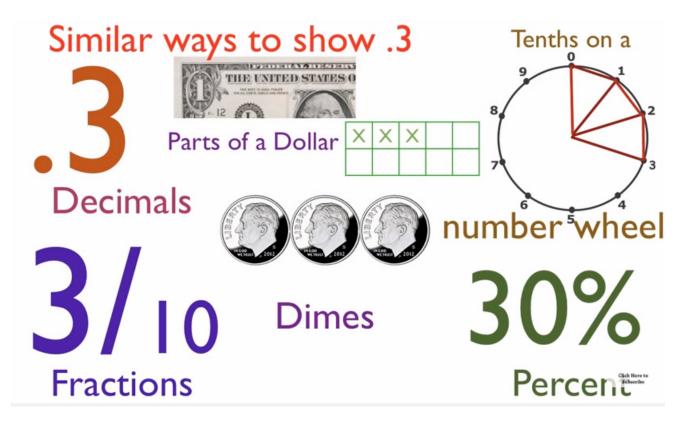
## Twenty PerCent, 2/10th, two dimes 19.



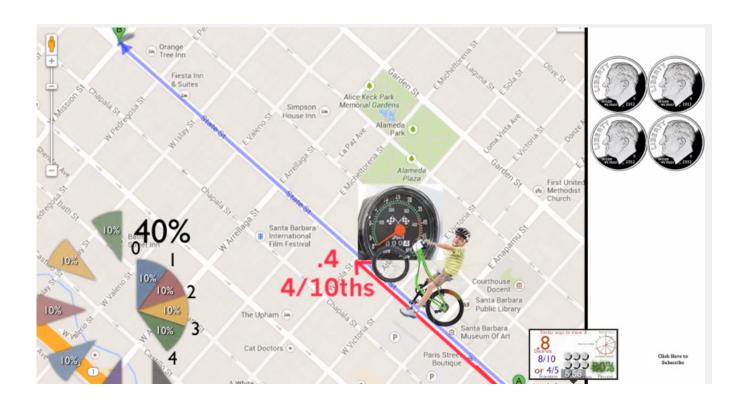


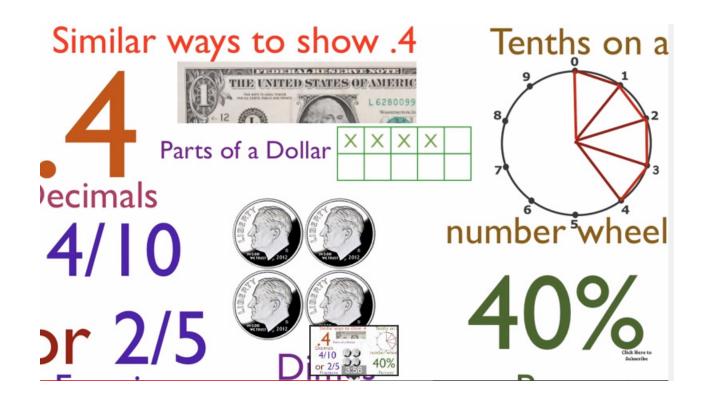
### Thirty Per Cent, 3/10th, three dimes

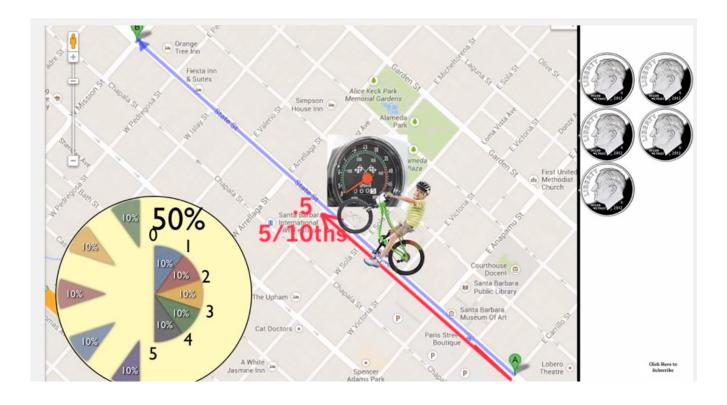




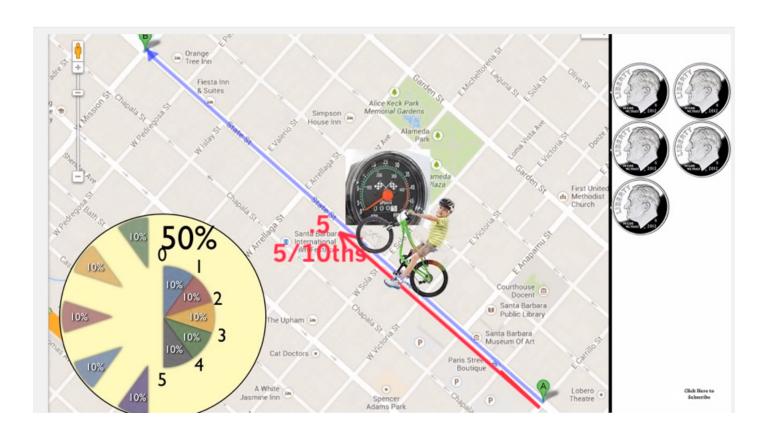
### Forty Per Cent, 4/10th, Four dimes

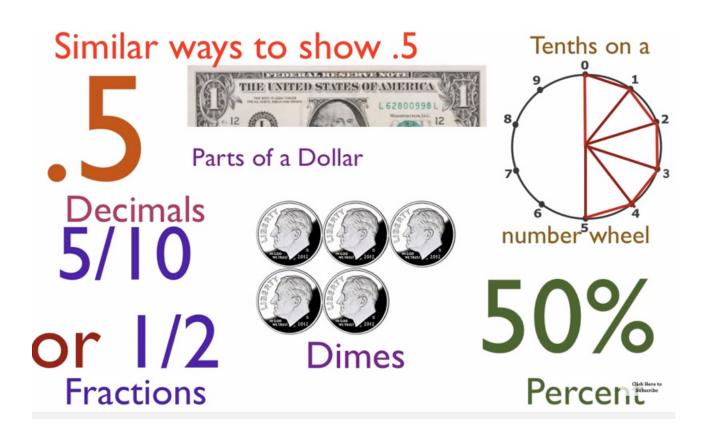






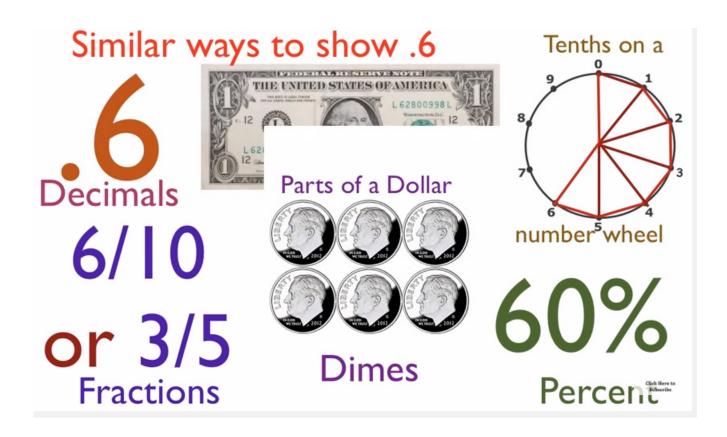
### Fifty Per Cent, 5/10th, Five dimes





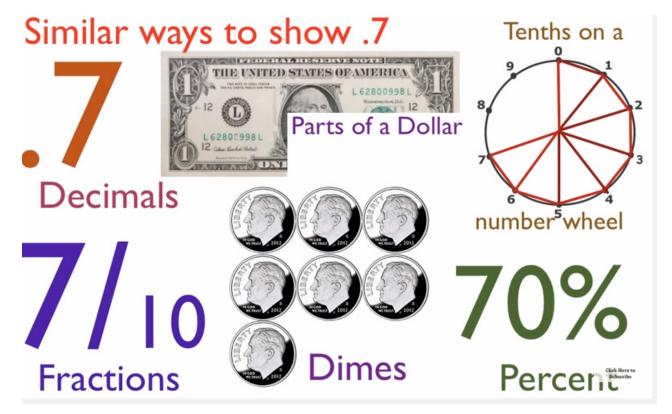
### Sixty Per Cent, 6/10th, Six dimes





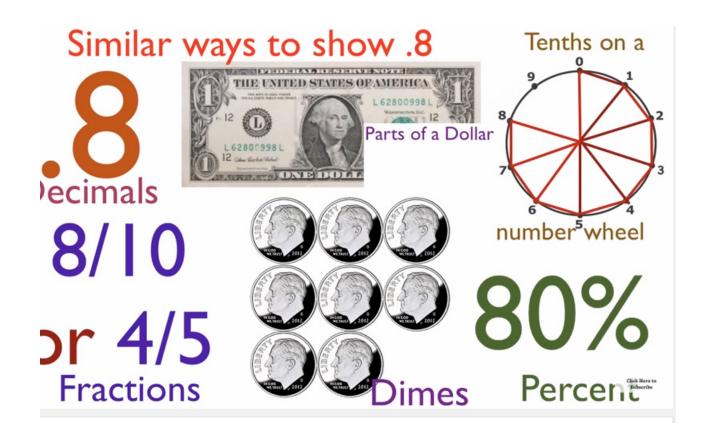
### Seventy Per Cent, 7/10th, Seven dimes



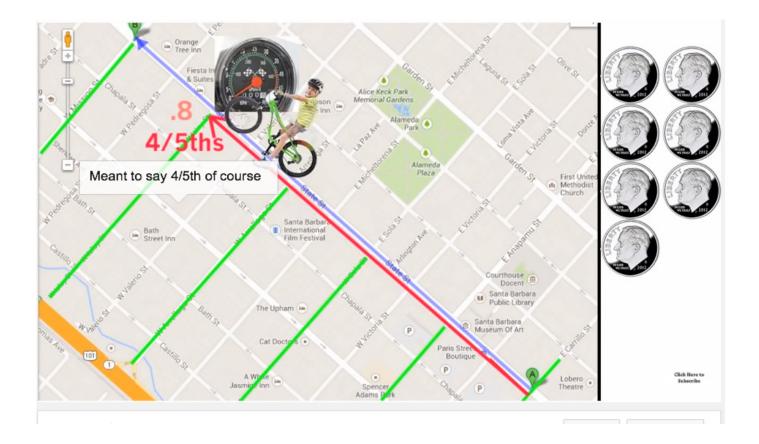


#### Eighty Per Cent, 8/10th, Eight dimes

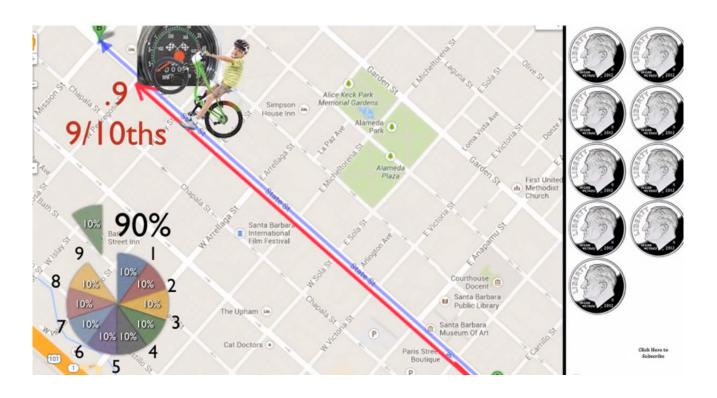




# Eighty Per Cent, 4/5th, Eight dimes

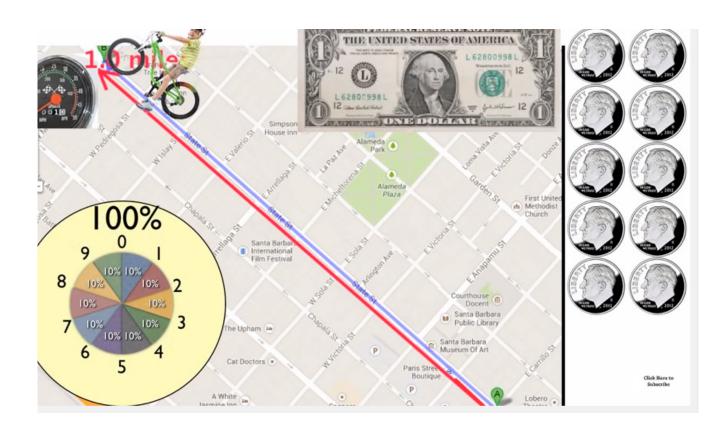


### Ninety Per Cent, 9/10th, Nine dimes





#### One Hundred Per Cent, 10/10th, Ten dimes

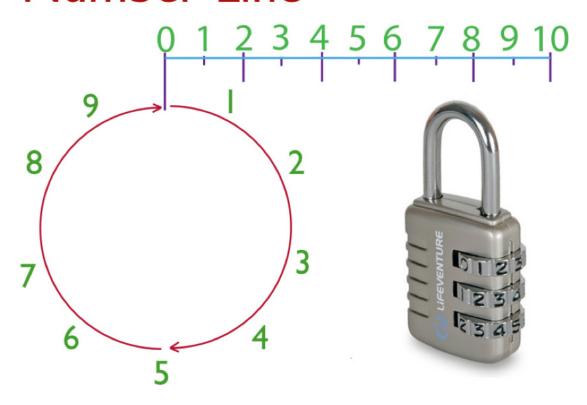


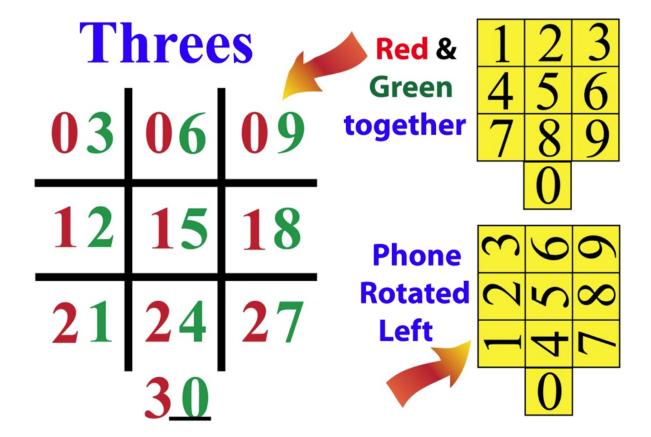




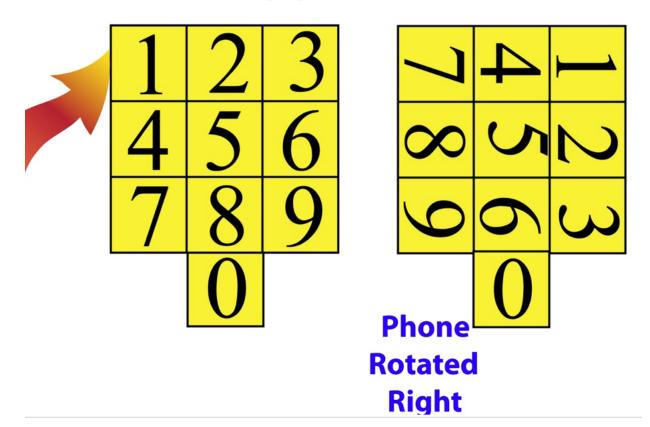
Rule of Tens
Numbers that add up to 10
use the same patterns
1 and 9 3 and 7
2 and 8 4 and 6

## Number Line





# 7s are opposite of 3s



#### **Testimonials**

My daughter absolutely loves it! I think all children would benefit from this approach to math whether they are right or left brain learners. This approach offers a different way of looking at numbers and the way they work. You are actually able to see patterns, which makes learning addition, subtraction, multiplication, and division easier.

—Shannon Mendez, Homeschooler

#### **Testimonials**

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—Shannon Mendez, Homeschooler

#### **Testimonials**

LOVE IT, LOVE IT, LOVE IT, LOVE IT... I have a third grader and this is working like a charm. I, myself have learned the times tables better. Thank you so very much.

—Tiffany Larkin

#### **Testimonials**

My child responded to the right brain math DVD the same way I did, with absolute amazement. Everyone I have shown it to has been amazed. The visual presentation of times tables in patterns was so powerful to me as an adult who has been through the old school method of just memorizing.

- Cheryl Rafferty, mom of 3 elementary students

#### **Testimonials**

I received your book yesterday, It's totally amazing, I'm 34 years old and for the first time in my life I am finally understanding how numbers work and slowly my fear of numbers is lessening... Thank you Mister Numbers, You have just opened up a whole new world to me and I am so grateful.

-Clare Price

#### **Testimonials**

Everything about your program is just fantastic! We have thoroughly enjoyed learning Right Brain Math. I teach 3rd and 4th graders at a small school for children with learning differences: dyslexia, ADD, processing issues. I couldn't believe their reaction the first time we did a number wheel. Their eyes lit up and they were so excited to see the pattern they created! "WOW and AWESOME" were two words used a lot during that math lesson. They immediately wanted to do more and had the same reaction to each one.

-Donna Talbot

#### **Testimonials**

I strongly recommend EZ Times Tables created by Tom Biesanz as an innovative way to teach multiplication and division. This wonderful visual tool helps students make friends with numbers. Both students who have had trouble memorizing their multiplication tables and students who are just being introduced to multiplication and division respond with enthusiasm to this system.

-Bev Abrams, Santa Barbara Charter School principal

#### **Testimonials**

I love it! I got the DVD and EZ times tables for my daughter. She'll pause a math video game and reference her EZ times tables for the answer. She no longer has tantrums when learning math! 5 stars all the way!

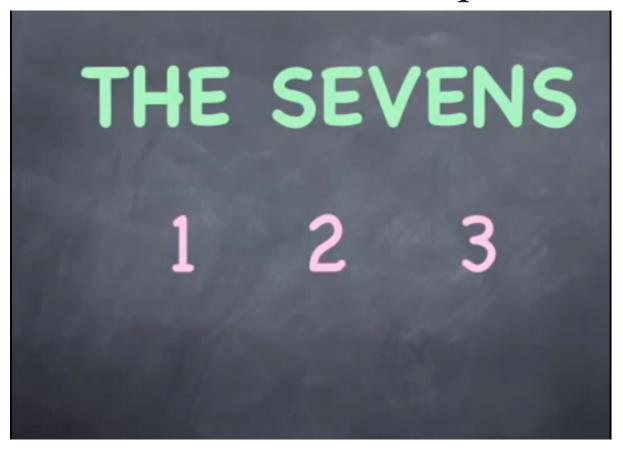
-Mary Dearborn

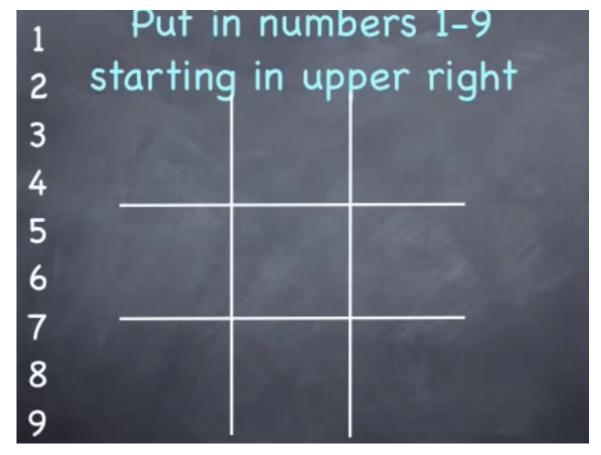
#### **Testimonials**

Tic-Tac-Toe was a HIT!!!! My daughter writes them quickly on the math homework sheets. This DVD and Workbook (Right Brain Math Book) could be a great tool to add in Math TEXTBOOKS.

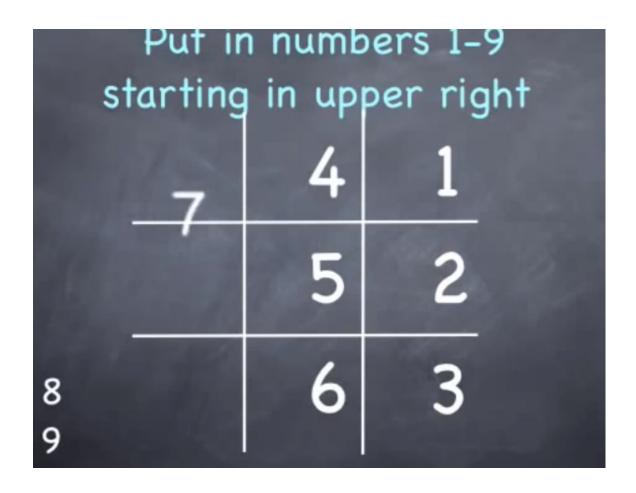
—Judy Reston

## Sevens on Tic Tac Toe Squares





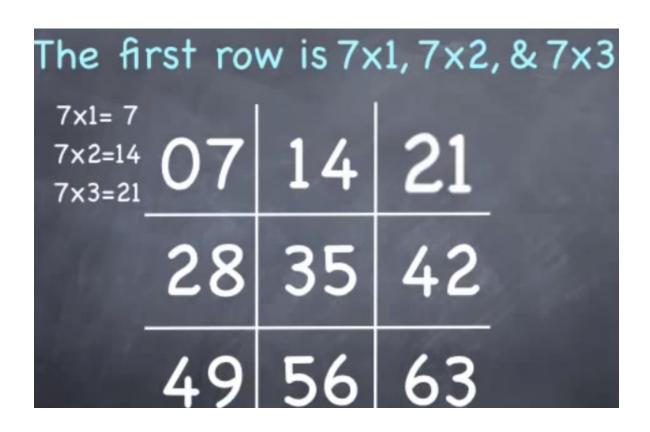
Put in numbers 1-9					
starting in upper right					
100	17/8				
4			Street, or other Designation of the last o		
4 5 6 7 8	1	4			
6	The said		2		
7	7 10		Alexander -		
8			3		
9					



W in	We add the 0-1-2 in front of the first row.					
0	1	2	7	4	1	
2	3	4	8	5	2	
4	5	6	9	6	3	

We add the 4-5-6 n front of the third row.				
07	14	21		
28	35	42		
5 4 9	6	3		

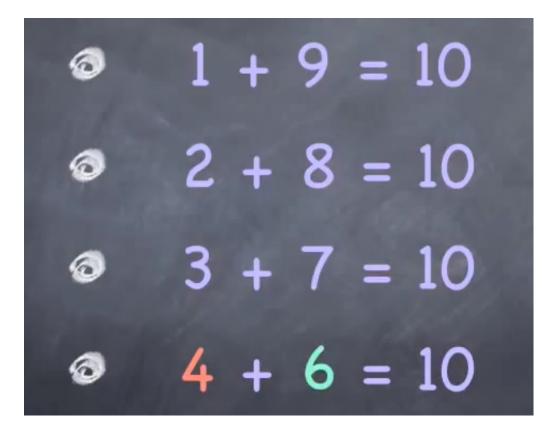
We add the 4-5-6 n front of the third row.							
-30	07 14 21						
	28	35	42				
40/4	49	56	63				

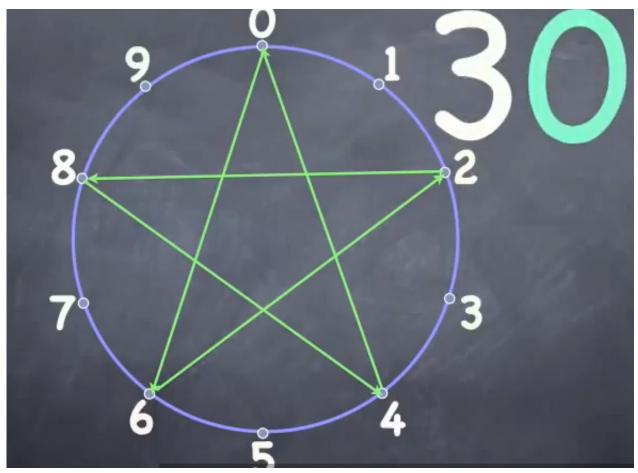


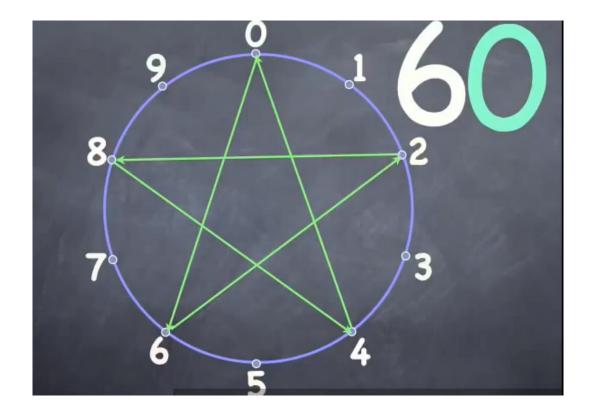
Drop	the 7	down	from 1s	t box
7×1= 7	100	-		36
7×2=14	07	174	21	
7×3=21	01			300
7×4=28	20	25	12	100
7x5=35 7x6=42	20	35	46	
7~7-49			What he	
7x8=56	49	56	63	

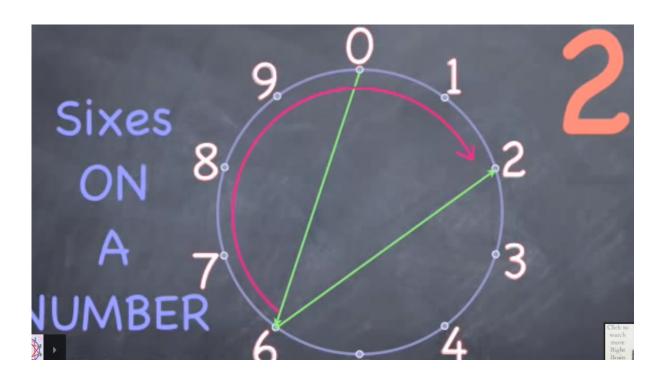
Drop	the 7	down	from	1st box
7×1= 7				
7×2=14	07	14	21	1000
7×3=21	01	-		63000
7×4=28	20	35	1.2	196
7x5=35 7x6=42	20	၁၁	42	1000
7x7=49	1.100	-	11.5	
7x8=56	49	56	63	70
7x9=63 7x10=70	4			

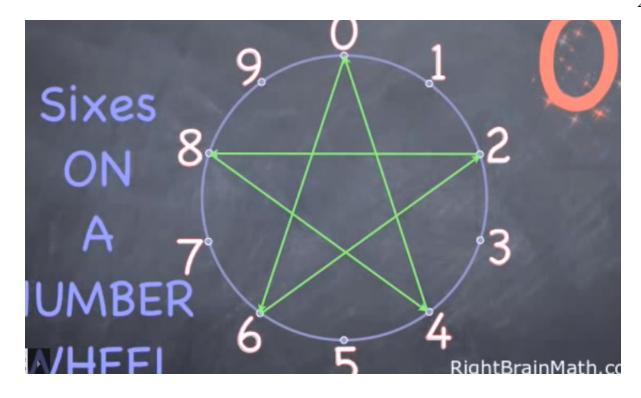
#### Sixes on a Number Wheel

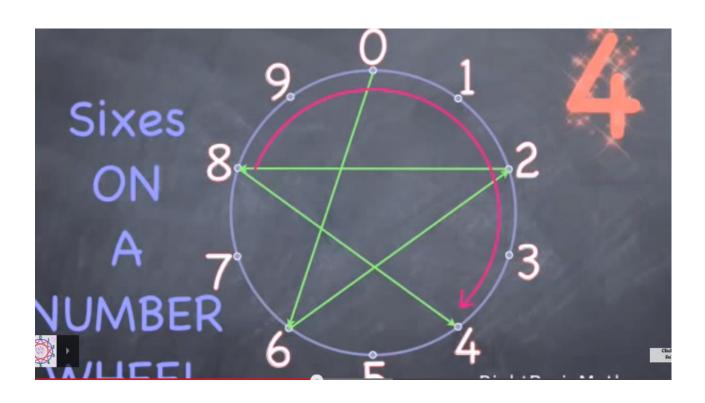












## Squares

$$0 \times 0 = 0$$
 $1 \times 1 = 0$ 
 $2 \times 2 = 4$ 
 $3 \times 3 = 9$ 
 $4 \times 4 = 16$ 
 $5 \times 5 = 25$ 
 $6 \times 6 = 36$ 
 $7 \times 7 = 49$ 
 $8 \times 8 = 64$ 
 $9 \times 9 = 81$ 
 $10 \times 10 = 100$ 

I believe that YOU can create the squares from I-40 or higher in a couple minutes

Citch Hora

$$1 \times 1 = 1$$
 $2 \times 2 = 4$ 
 $3 \times 3 = 9$ 
 $4 \times 4 = 16$ 

All you need to know is the squares of 1, 2, 3, 4

And be able to add a 1-digit-number to another number: like 152 +8

You can do that!

lick:

Let's look at the patterns, the big picture, in 1-10 on the right are the Onesies

- starts and ends with 0, with 5 in the middle
- After 0, the first tensies are 1-4-9-6

Watch this video to square any number: CLICK HERE Glad Reve 19 Subscribe Subscribe

```
0 x 0 = 0

1 x 1 = 1

2 x 2 = 4

3 x 3 = 9

4 x 4 = 1

5 x 5 = 2

6 x 6 = 3

7 x 7 = 4

8 x 8 = 6

9 x 9 = 8

10 x 10 = 1 0
```

Let's look at the patterns, the big picture, in 1-10 on the right are the Onesies

- starts and ends with 0, with 5 in the middle
- After 0, the first tensies are 1-4-9-6

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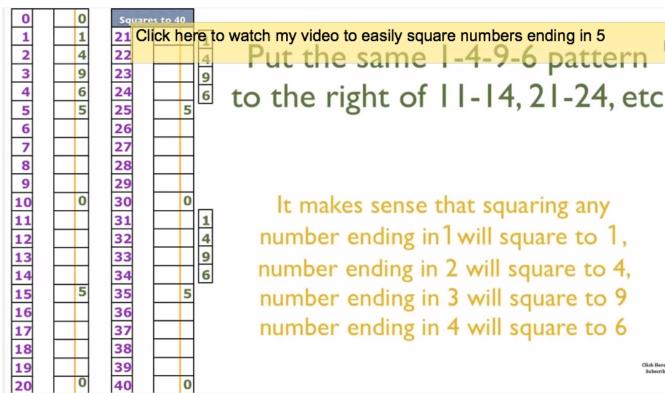
Subtitles/CC

0	0	Square	s to 4	0	
0 1 2 3 4 5 6 7 8 9 10 11 12		21 Cl	ick h	er	е
2		22			
3	H	23			
4	H	24		Н	
5	5	25		5	
6		25 26 27	$\vdash$	_	
1 2	++	27		Н	
<del>  '</del>	++	20	$\vdash$	Н	
8	$\vdash$	28 29 30		Н	
9		29	$\vdash$		
10	0	30	$\vdash$	0	
11	$\perp$	31		Ц	
12	$\sqcup$	32		Ц	
13		33		Ц	
14		34		Ц	
15	5	35			
16		36			
17		37			
15 16 17 18		38			
19		39			
20	0	40			

#### Bring your 0s and 5s to the right of the line

to watch my video to easily square numbers ending in 5

There is an easy trick to squaring 5s, t(tensie) X t +1 and write 25 after it. SO... 15 squared is  $1 \times 2 = 2$ , so 225 25 squared is  $2 \times 3 = 6$ , so 62535 squared is  $3 \times 4 = 12$ , so 122545 squared is  $4 \times 5 = 20$ , so  $20^{12}$ 



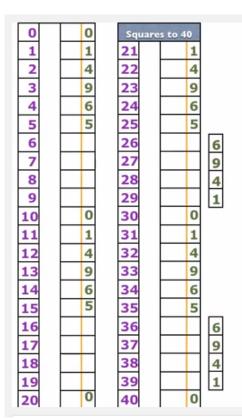
It makes sense that squaring any number ending in 1 will square to 1, number ending in 2 will square to 4, number ending in 3 will square to 9 number ending in 4 will square to 6

0	0	Square	s to 40	
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19	1	21	1	1
2	4	22	4	4
3	9	23	9	9
4	6	24	6	6
5	5	25	5	
6		23 24 25 26 27 28 29 30		
7		27		
8		28		
9		29		
10	0	30	0	
11	1	31	1	1
12	4	31 32	4	4
13	9	33	9	9
14	6	34	6	6
15	5	35	5	U
16		36	- 3	
17	$\overline{}$	37		
10	$\overline{}$	38	-	
10	+	39	-	
20	0	40	0	
20		40	U	

# Put the same 1-4-9-6 pattern to the right of 11-14, 21-24, etc

It makes sense that squaring any number ending in 1 will square to 1, number ending in 2 will square to 4, number ending in 3 will square to 9 number ending in 4 will square to 6

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# NOW put the same 1-4-9-6 pattern going UP from 0

WHAT? HOW? WHY?
It makes sense that squaring any
number ending in 9 will square to 1,
number ending in 8 will square to 4,
number ending in 7 will square to 9
number ending in 6 will square to 6

Click Here to

0	0	Square	s to 40	
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20		21	1	
2	4	22	4	
3	9	23	9	
4	6	24	6	
5	5	25	5	_
6	6	26	9 6 5 6	6
7	9	27	9	6 9 4 1
8	4	28	4	4
9	1	29	1	1
10	0	30	0	
11	1	31	1	
12	4	32	4	
13	9	33	1 4 9 6	
14	6	34	6	
15	5	35	5	
16	6	36	6	6
17	9	37	9	6 9 4 1
18	4	38	4	4
19	1 4 9 6 5 6 9 4 1 0 1 4 9 6 5 6	21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40	1	1
20	U	40	0	

# NOW put the same 1-4-9-6 pattern going UP from 0

WHAT? HOW? WHY? It makes sense that squaring any number ending in 9 will square to 1, number ending in 8 will square to 4, number ending in 7 will square to 9 number ending in 6 will square to 6

Click Her Subscri

$$\begin{array}{c}
 0 \times 0 = \\
 1 \times 1 = \\
 2 \times 2 = \\
 \hline
 3 \times 3 = \\
 \hline
 4 \times 4 = \\
 5 \times 5 = \\
 6 \times 6 = \\
 \hline
 4 \times 7 = \\
 \hline
 8 \times 8 = \\
 \hline
 8 \times 8 = \\
 \hline
 10 \times 10 = \\
 11 \times 11 = \\
 \hline
 1 \times 11 = \\
 1 \times$$

#### Let's look at the Tens pattens:

- They are 0 (go up 0) until the 9
- They go by I until the second 9: I-2-3-4
  - They go by 2 until the third 9: 6-8-10-12-14-16

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 $12 \times 12 =$ 

 $13 \times 13 =$ 

0	0	Square	es to 40
0 1 2 3 4 5 6 7 8 9 10 11	1	21	1
2	4	22	4
3	9	23	9
4	6	24	6
5	5	25	5
6	6	26	6
7	9	27	9
8	4	28	4
9	1	29	1
10	0	30	0
11	1	31	1
12	4	32	4
13	9	33	9
14	6 5	34	6
14 15 16	5	35	5
16	6	36	6
17	9	37	9
18	4	38	4
19	1	39	1
20	0	40	0

Start by drawing a line after each 9 in the Onesies, this shows where the Tensies (tens-digits) change

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After the 1st line, tens go up by 1: 1, 2, 3, 4 creating 16, 25, 36, and 49

Watch this video to square ANY number: CLICK HER Philosophia

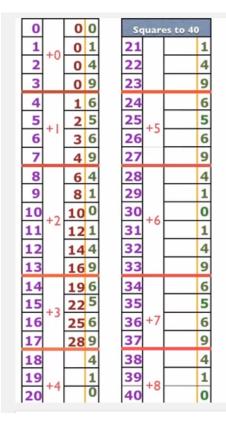
0	0	0	Squar	es to 40
0 1 2 3 4 5 6 7	$\overline{}$	1	21	1
2 +0	0	4	22	4
3	0	9	23	9
4	1	6	24	6
5	2	5	<b>25</b> +5	5 6
6	3	6	26	6
7	4	9	27	9
8	6	4	28	4
9	8	1	28 29 30	1
10 +2	10	0	30 +6	0
11		1	31	1
12		4	32	4
13		9	33	9
14		6 5	34	6
15			35	6 5 6
16		6	36 +7	
8 9 10 11 12 13 14 15 16 17		9	37	9
18		4	38	4
19		1	39	1
20		0	40	0

After the 2nd line, tens go
up by 2:
6, 8, 10, 12, 14, 16

(notice these are all multiples of 2)

creating 64, 81, 100, 121, 144, and 169

Watch this video to square ANY number: CLICK HER



After the 3rd line, tens go up by 3: 19, 22, 25, 28

creating 196, 225, 256, 289

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0	0 0	Squar	es to 40
1 +0	0 1	21	44 1
2	0 4	22	48 4
3	0 9	23	52 9
1 +0 2 3 4 5 +1	1 6	24	6
5	2 5	<b>25</b> +5	5
6	3 6	26	6
7	4 9	27	9
8	6 4	28	4
	8 1	29	1
9 10 11	10 <sup>0</sup>	30 +6	0
11	121	31	1
12	144	32	4
13	169	33	9
14	196	34	6
<b>15</b>	225	35	5
16	<b>25</b> 6	36 +7	6
17	289	37	9
18	324	38	4
19	36 1	39 +8	1
20	40 <sup>0</sup>	40	0

After the 4th line, tens go up by 4: 32, 36, 40, 44, 48, 52 (notice all multiples of 4)

creating 324, 361, 400, 441, 484, 529

Click He Subsci

0	0 0	S	quar	es to 40	
	0 1	2:	L	44	1
2	0 4	22	2	48	4
1 2 3	0 9	23	3	52	9
	1 6	24	ļ	57	6
5	2 5	25	10	62	5
6	3 6	26	5	67	6
4 5 6 7	4 9	27	7	72	9
8	6 4	28	3		4
	8 1	29	9		1
10 +2	<b>10</b> 0	30	+6		0
11	121	31	L		1
12	144	32	2		4
9 10 11 12 13	<b>16</b> 9	33	3		9
	196	34	ļ		6
14 15 16 17	225	34 35	5		5
16	<b>25</b> 6	36	+7		6
17	<b>28</b> 9	37	7		9
18	324	38	3		4
19	36 1	39	10		1
20 +4	40 0	40	) 10		0

After the 5th line, tens go up by 5: 57, 62, 67, 72

creating 576, 625, 676, 729

Click Here to

0	0 0	Sc	uare	es to 40	
1 +0	0 1	21		44	1
2	0 4	22		48	4
3	0 9	23		52	9
	1 6	24		57	6
5	2 5	25	+5	62	5
4 5 6 7	3 6	26		67	6
7	4 9	27		72	9
8	6 4	28		78	4
9	8 1	29		84	1
9 10 11	<b>10</b> 0	30	+6	90	0
	121	31	. 0	96	1
12	144	32		102	4
13	169	33		108	9
14	<b>19</b> 6	34			6
14 15 +3	225	35			5
16	<b>25</b> 6	36	+7		6
17	289	37			9
18	324	38			4
19	361	39	+8		1
20	40 <sup>0</sup>	40	. 0		0

After the 6th line, tens go up by 6: 78, 84, 90, 96, 102, 108 (notice all multiples of 6)

creating 784, 841, 900, 961, 1024, 1089

Click Here to

0	0 0	Sc	uare	es to 40	
1 +0	0 1	21		44	1
2	0 4	21 22		48	4
3	0 9	23		52	9
4	1 6	24		57	6
5	2 5	25	+5	62	5
6	3 6	25 26	, ,	67	6
4 5 6 7	4 9	27		72	9
8	6 4	28		78	4
9	8 1	29		84	1
9 10 11 12	10 <sup>0</sup>	30 31 32	+6	90	0
11	121	31	. 0	96	1
12	144	32		102	4
13	169	33		108	9
14	196	34		115	6
15	225	35		122	5
14 15 16	<b>25</b> 6	36	+7	129	6
17	289	37		136	9
18	324	38			4
19	36 1	39	٠.		1
20 +4	400	40	-0		0

After the 7th line, tens go up by 7: 115, 122, 129, 136,

creating 1156, 1225, 1296, 1369

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0	0 0		Squa	are	es to 40	
1 +0	0 1	2	21		44	1
<b>1</b> +0	0 4	2	22		48	4
3	0 9	2	23		52	9
4	1 6	2	24		57	6
5 6	2 5	2	25	5	62	5
6	3 6	2	26	_	67	6
7	4 9	2	27		72	9
8	6 4		28		78	4
9	8 1	_	29		84	1
10	10 <sup>0</sup>	3	30	6	90	0
11	121	3	31	•	96	1
12	<b>14</b> 4		32		102	4
13	169	3	33		108	9
14	<b>19</b> 6		34		115	6
15 16	<b>22</b> 5		35		122	5
	<b>25</b> 6		<del>1</del> 6	7	129	6
17	289	3	37		136	9
18	<b>32</b> 4		88		144	4
19	361	3	39	8	152	1
20	400	4	Ю		160	0

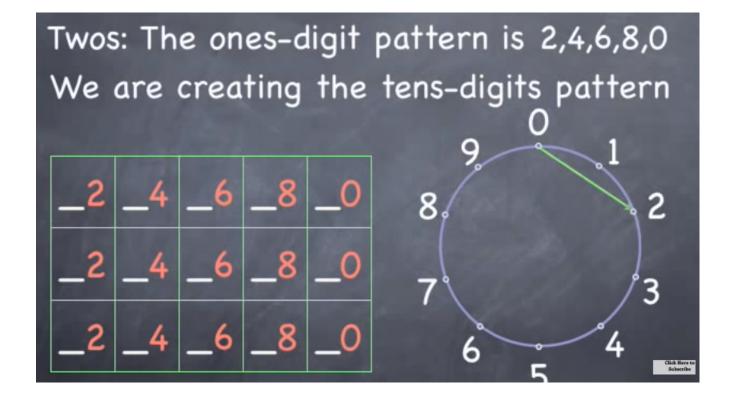
After the 8th line, tens go up by 8: 144, 152, 160, etc (notice all multiples of 8)

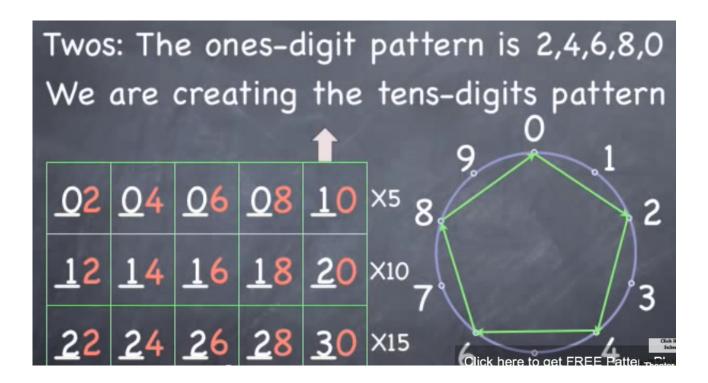
creating 1444, 1521, 1600, Continue as high as you like

#### Square Any Number up to 100

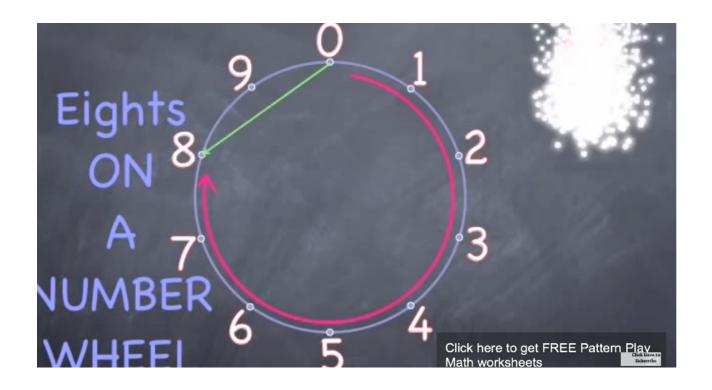
	Squ	Jar	e a	nu	mb	er l	ike		2	2	
Go to a nearby multiple of 5. The Tens-digits add or subtract 1/5 of that number.											
Start from	5	10	15	20	25	30	40	50	60	75	100
Up or Down	1	2	3	4	5	6	8	10	12	15	20
Or	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$										

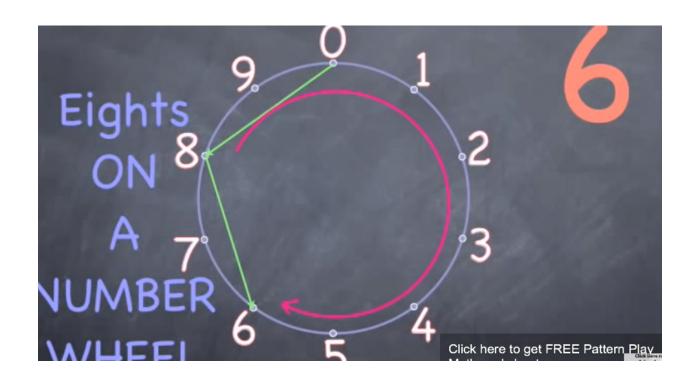
#### Twos on a Number Wheel





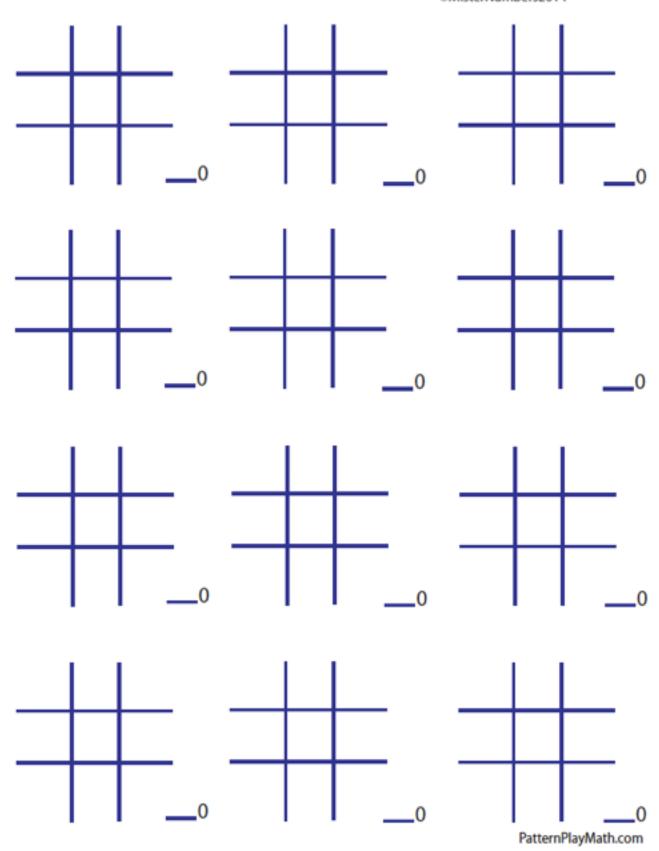
#### Eights on a Number Wheel





#### MisterNumbers TicTacToe Squares for 1s, 3s, 7s, and 9s

©MisterNumbers2014



# Odd Numbers Even Numbers Complete EZ Table copyright©Thomas Biesanz www.eztimestable.com

	_								<del></del> 1
E 7		ΓΙ	M	E		ΓΑ	B	T	$\mathbf{E}$
			umbers				Numbers		
9	7	5	3	1	2	4	6	8	10
019	7	5	•	1	2	•	•	•	1:0
1 8	14	10	•	2	4	4 <sub>x1</sub>	•	•	2 0
2 7	21	15	3x1	3	6	•	6x1	•	3 0
3¦6	28	20	•	4	8	4x2	•	8x1	4:0
4 5	35	25	•	5	10	•	•	•	5 0
5 4	42	30	3x2	6	1 2	4x3	6x2	•	6 0
6.3	49	35	•	7	14	•	•	•	7:0
7 2	56		•	8	16	4 <sub>x4</sub>	•	8x2	8 0
	63	40	Зхз		18	•	6х3	•	
8¦1 9¦0	70	45	•	9 1 0	20	4x5	•	•	9 0 <b>10</b> 0
910	70	50	•	1 1	22	•	•	•	1010
			3x4	1 2	24	4x6	6x4	8x3	
			•	13	2 6	•	•	•	
			•	14	28	4x7	•	•	
			3x5	15	3 0	•	6x5	•	
			•	16	3 2	4x8	•	8x4	
			•	1 7	3 4	•	•	•	
			3x6	18	3 6	4x9	6x6	•	
			•	19	3 8	•	•	•	
			•	20	4 0	4x10	•	8x5	
			3x7	2 1	4 2	•	6x7	•	
			•	2 2	4 2 4 4	4	•	•	
			•	2 3	4 6	•	•	•	
			3x8	2 4	4 8	4	6x8	8x6	
			•	2 5	5 0	•	•	•	
			•	2 6	5 2	4	•	•	
			Зх9	2 7	5 4	•	6x9	•	
			•	28	5 6	4	•	8x7	
			•	2 8 2 9 3 0	5 8 6 0	•	•	•	
			3x10	3 0	60	4	6x10	•	
			•	3 1	6 2	•	•	•	
			•	3 2	6 4	4	•	8x8	

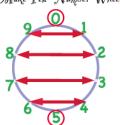
Color EZ Times Table ©2007byThomas Biesanz http://EZTimesTable.com

MisterNumbers Pattern Play Math Worksheets.indd 232

 $0 \times any number = 0$ 

#### Ten Adds and Nine Adds

Make Ten" Number Wheel



#### Importance of students learning Ten Adds

Our number system is ten base so Ten, and the numbers that add up to 10, are very important for kids when learning addition, subtraction and multiplication, They show up on the number wheel in cool ways that can help kids with basic addition. Start with the five at the bottom.

#### **Cube Numbers and Ten Adds**

Another place that Ten Adds show happens when any number is cubed.

Numbers ending in:	Cube ends in:
0	0
1	1
2	8
3	7
4	4
5	5
6	6
7	3
8	2
9	9

Most cubes end in the same number as the Ones of the root number.

The four exceptions are 2, 3, 7, and 8. All of them end in the Ten Add of the original Ones digit.

#### **Learning Ten Adds on a Number Wheel**

Start at the 5 at the bottom of the number wheel. It is all alone there. You can circle (and double an alone number. 5+5=10. We have 10 digits (fingers) and 10 digits (numbers) and our number system is ten based BECAUSE humans have 10 fingers.

To be more flexible, have five pennies in each hand. Again 5+5=10.

Now put one penny from the right hand into the left hand. We still have 10 pennies, but now 6+4=10. Now put another penny from the right hand into the left hand. We still have 10 pennies, but now 7+3=10. Now put another penny from the right hand into the left hand. We still have 10 pennies, but now 8+2=10. Now put another penny from the right hand into the left hand. We still have 10 pennies, but now 9+1=10. Now put the last penny from the right hand into the left hand. We still have 10 pennies, but now 10+0=10. On the number wheel horizontal parallel lines show us the Ten Adds.

#### Nine Adds

Look at the Ten Adds on a number Wheel. Raise all the right side up one number to create Nine Adds. Again we have parallel lines and the numbers linked not only show all the numbers adding up to 9: 0-9, 1-8, 2-7, 3-6, 4-5, 5-4, 6-3, 7-2, 8-1, 9-0 as we go around, but they also are revealing the Nines times table: 9-18-27-36-45-54-63-72-81-90. See the Nines Add Wheel

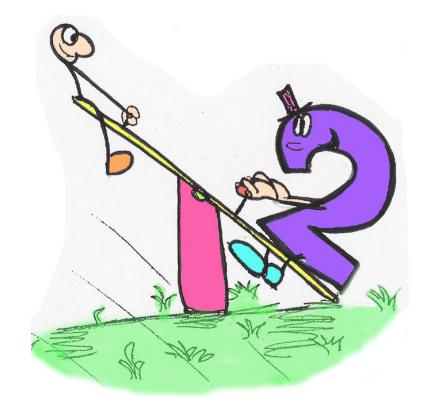
# Coloring Numbers: Single and Ten-Adds

Originals by Jacob Marsh

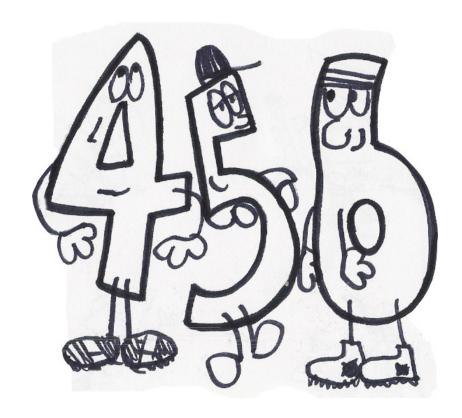


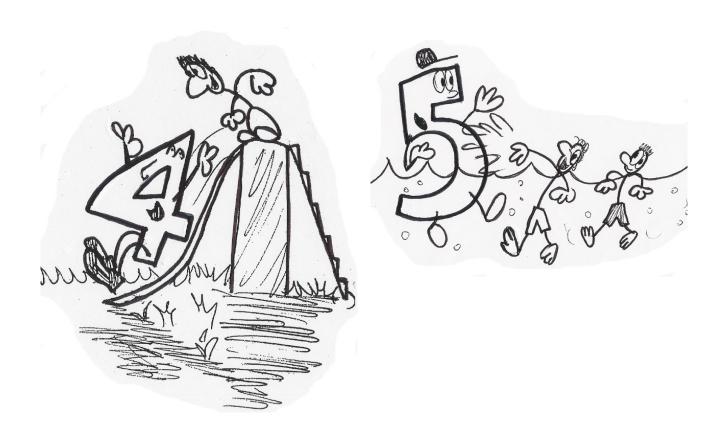




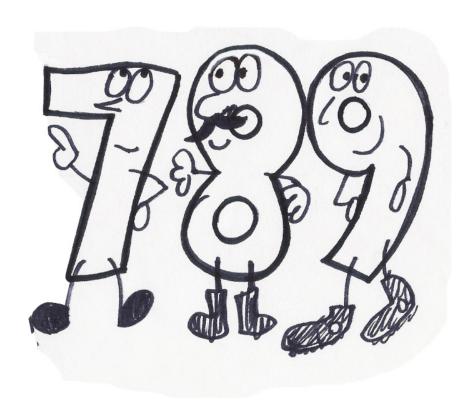


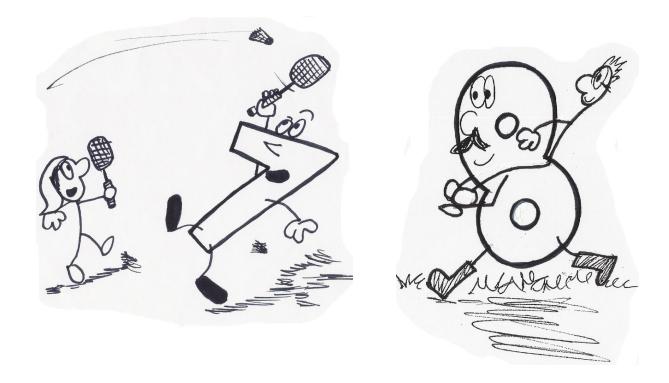


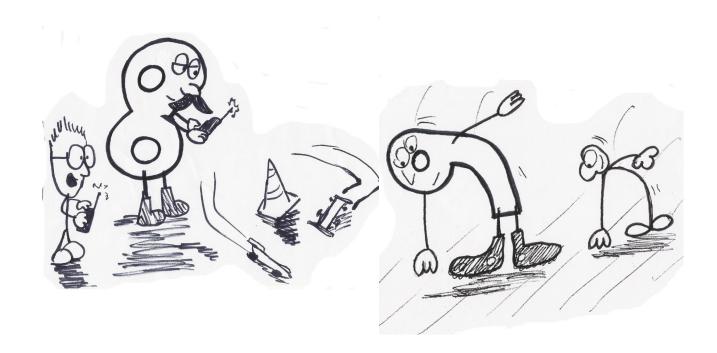




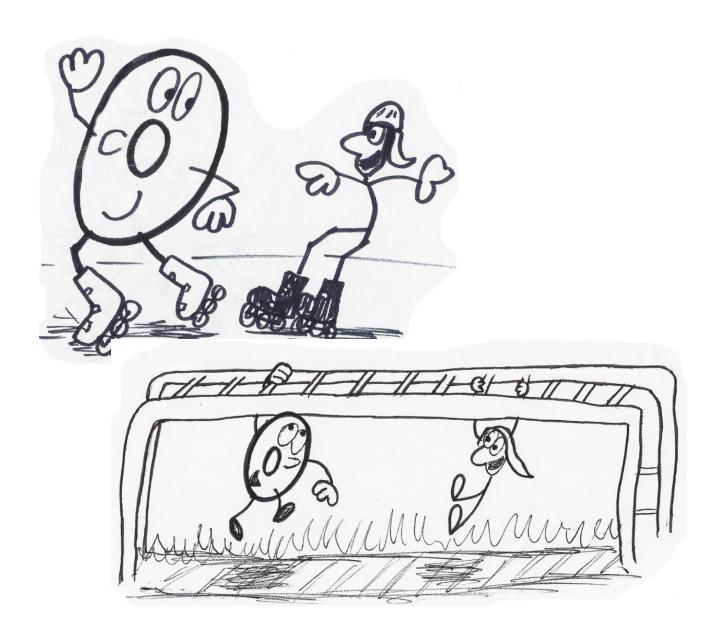


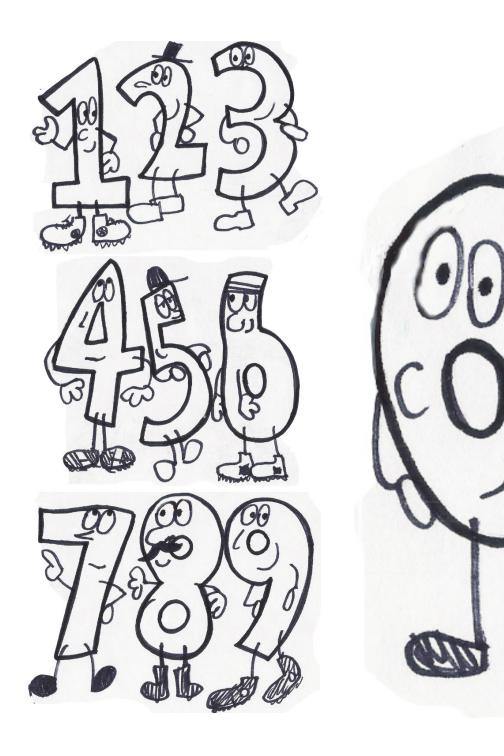


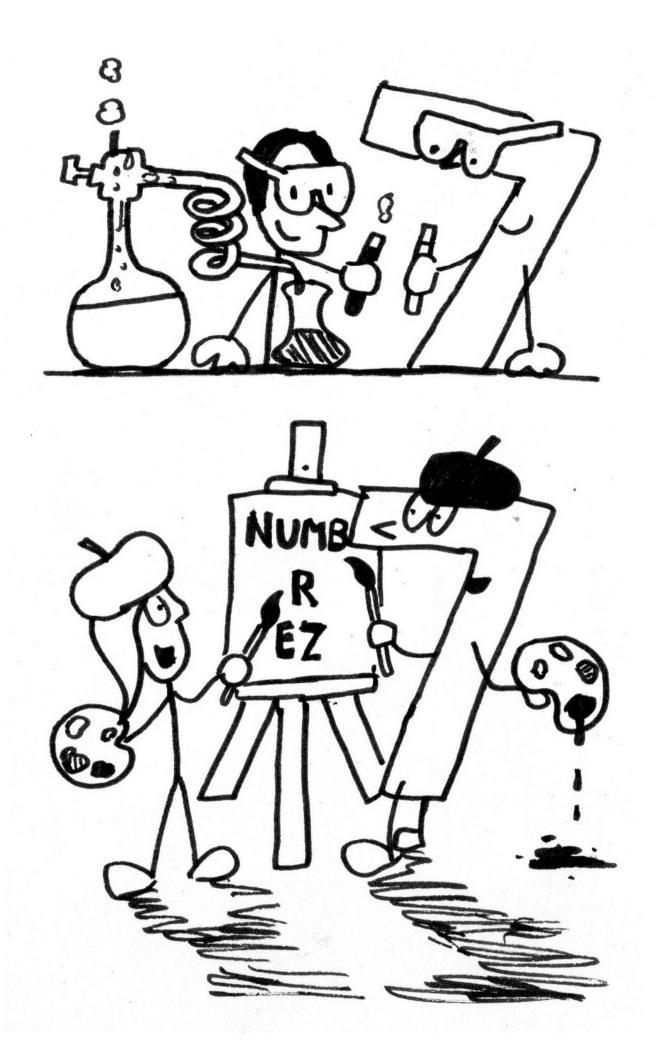










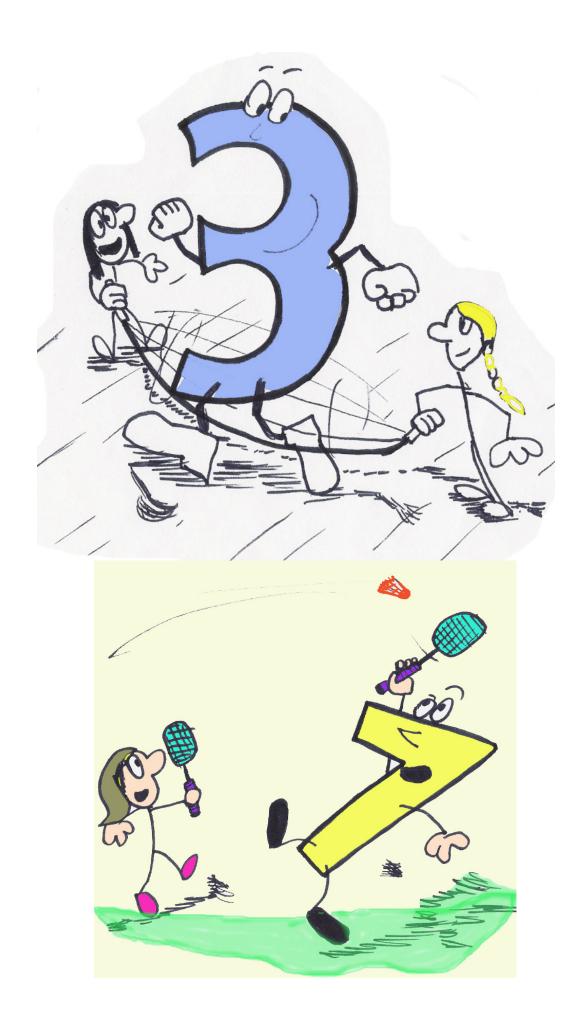


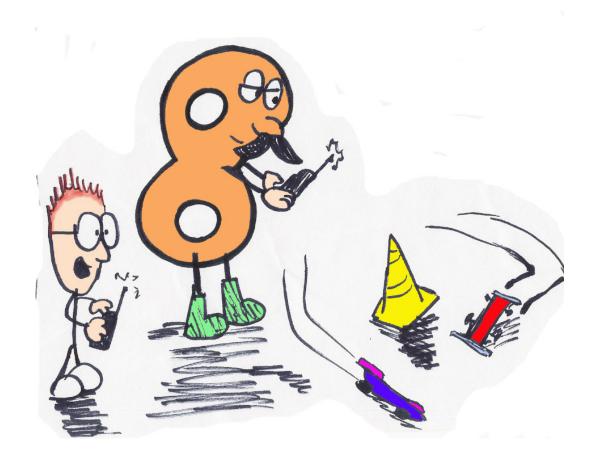


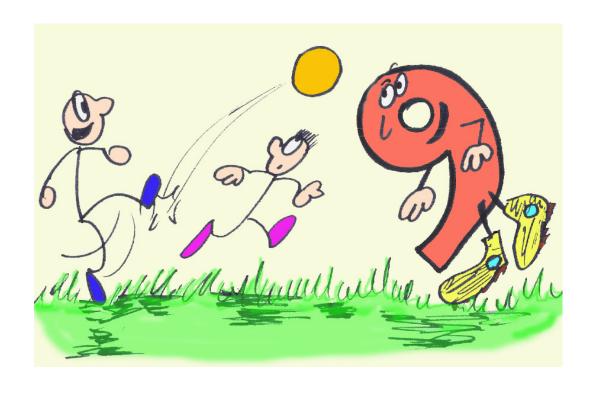












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